Deaf intermarriage does not increase the prevalence of deafness alleles

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15 **Abstract**

16 The idea that deaf intermarriage increases deafness was forcefully pushed in the late 19th century
 17 by Alexander Graham Bell, in proceedings published by the National Academy of Science.
 18 Bell's hypothesis was not supported by a 19th century study by Edward Allen Fay, which was
 19 funded by Bell's own organization, the Volta Bureau. The Fay study showed through an analysis
 20 of 4,471 deaf marriages that the chances of having deaf children did not increase significantly
 21 when both parents were deaf. In light of an apparent increase in non-complementary pairings
 22 when a recent dataset of Gallaudet alumni was compared with the 19th century Fay dataset,
 23 Bell's argument has been resurrected that residential schools for the deaf, which concentrate
 24 signing deaf individuals together, have promoted assortative mating and increased the prevalence
 25 of both phenotypic deafness and the commonest recessive deafness allele. Because this
 26 hypothesis persists, even though it contradicts classical models introduced by R.A. Fisher and
 27 Sewell Wright, it is critically important that this hypothesis be thoroughly re-investigated. In this
 28 study, we used an established forward-time genetics simulator with parameters and
 29 measurements collected from the published literature. Compared to mathematical equations,
 30 simulations allowed for more complex modeling, operated without assumptions of parametricity,
 31 and captured ending distributions and variances. Our simulation results affirm predictions from
 32 classical equations and show that assortative mating only modestly increases the prevalence of
 33 phenotypically deaf individuals, with this effect mostly completed by the third generation. Most
 34 importantly, our data show that even intense assortative mating does not increase allelic
 35 frequency under reported conditions. These results are not locus-specific and are generalizable to
 36 other forms of recessive deafness. We offer alternative explanations for the higher rate of non-
 37 complementary pairings measured in the contemporary Gallaudet alumni sample as compared to
 38 the Fay dataset.

39 **Introduction**

40 In an 1883 presentation to the National Academy of Sciences, Alexander Graham Bell delivered
 41 an ominous warning about the intermarriage of deaf individuals [1]. If intermarriage was left

unchecked, Bell argued, this would lead to a “deaf variety of the human race.” Bell delineated the costs of educating deaf individuals and argued that the residential schools were an economic burden to state governments funding the schools [1]. Following this address, Bell conducted research on hereditary deafness on Martha’s Vineyard in the late 1880s. Bell persisted in efforts to better understand the transmission of genetic deafness, although he ultimately never understood it [2,3]. To this end, he hired Edward Allen Fay, who was the vice-president at Gallaudet College and editor of the *American Annals of the Deaf*. Bell’s Volta Bureau funded Fay’s landmark study of 4,471 deaf marriage pedigrees, collected from alumni of Gallaudet University, whose students are predominantly deaf, and alumni from residential schools for the deaf throughout the United States. Although the Fay study eventually concluded that deaf intermarriage did not much increase the chances of having deaf children [4], Bell remained vocal in his beliefs that the ideal marriage was a marriage between a deaf and hearing person. As the wealthy inventor of the telephone, he remained highly influential in the scientific community and in the nascent eugenics movement.

The results of Fay’s study were not well understood at the time because they were published in 1898, before the rediscovery of Mendel’s work [5] and the many discoveries in experimental and theoretical genetics that followed. In those days, the understanding of the heredity of deafness and heredity in general was based on observation, such as those recorded by the otologist William Wilde in 1857, or by tallying summary statistics, like Fay’s work [6].

We now know that genetic deafness [OMIM 220290] accounts for the majority of deafness in children and is caused by mutations in >140 already mapped genes [7]. Of these, genetic deafness due to connexin 26 (*GJB2*) variant alleles [OMIM 121011] is by far the most common, accounting for more than a quarter of congenital deafness [8]. Three *GJB2* frameshift variants account for most severe to profound congenital deafness, and are associated with specific ethnic groups: c.35delG in European ancestry, c.167delT in Ashkenazi Jewish ancestry, and c.235delC in Asian ancestry [9-11]. These three variants are inherited in an autosomal recessive fashion, and cause nonsyndromic deafness, meaning that there are no other discernible physical characteristics.

In fact, most deaf intermarriage produces hearing children mainly because of the complementation between the many recessive genes causing deafness, and also because

deafness often occurred or was observed after birth and was usually attributed to injury or childhood morbidity. Fay [4] termed these cases as “adventitious.”

In the early 20th century, R.A. Fisher [12] and Sewell Wright [13] introduced a mathematical model for inbreeding that could be applied to assortative mating, reworked by Crow and Felsenstein [14]. In a large population and in the absence of selective pressure, assortative mating increases the phenotypic expression of recessive alleles, but the allelic frequencies themselves do not change. Therefore, deaf intermarriage could be expected to cause an initial and limited increase in phenotypic deafness, and would have no effect on the allelic frequency [14].

In contradiction to Fisher’s and Wright’s classical model, recent authors have posited that assortative mating between signing deaf individuals who socialized together in residential schools over slightly more than 200 years in the United States has increased both phenotypic and allelic frequencies for recessive deafness [15,16]. Termed “linguistic homogamy,” it is reasoned to be motivated by an innate human need for easy and effective communication. Signing deaf individuals would find linguistically compatibility in one another and intermarry. This hypothesis was used to explain results from a pedigree study by Arnos *et al.* [17] which had shown that non-complementary pairings in a contemporary Gallaudet alumni dataset were occurring more often than non-complementary pairings in the original Fay dataset, which had been collected more than 100 years earlier.

The degree of assortative mating among deaf Americans has been measured, and has been relatively stable over the past 200 years. Fay [4], in 1898, initially reported an uncorrected measure of 72.5%. From the 1970 National Census of the Deaf Population (NCDP) in the United States, Schein and Delk [18] calculated a figure of 80-90%. Most recently, Blanton *et al.* [19] calculated a figure of 79% from a sample of Gallaudet alumni, who are predominantly white Americans.

The reproductive fitness of deaf individuals has also been investigated through fertility. All reports from the literature report markedly depressed relative fitness. Values normalized against the general population range from 0.31 to 0.91. The highest measured fitness of 0.91, which is still depressed, was reported from an educated American deaf sample from Gallaudet University [18-22].

This continuing question of whether assortative mating between deaf individuals affects the incidence of phenotypic deafness and the prevalence of deafness alleles is important because it has potential implications for policy and funding decisions. This includes popular support for funding of residential deaf education programs, which bring deaf people together into social groups. It may also alter opinions about eugenics, which was popular in fairly recent history, particularly in Germany and in Scandinavian countries. Discussion about the ethics of eugenics is moving to the forefront again, given the recent use of gene-editing technologies (CRISPR) in humans [23,24]. It is therefore critically important that the question “does deaf intermarriage (assortative mating) increase the prevalence of deafness” is carefully examined using a variety of approaches.

In this study, we performed thousands of forward-time evolutionary simulations using an established package [25,26]. We simulated assortative mating and measured the changes in phenotypic deafness and allelic frequencies, using parameters scoured from the published literature. We tested the hypothesis that assortative mating influences the gene pool and used statistical analyses to compare median results and ending distributions. This approach allowed us to capture the variance in end results without any underlying assumptions of parametricity. We further compared these results with mathematical modeling.

Results

We initially ran 5,000 simulations following parameters established by Nance and Kearsey [15] so that we could directly compare our simulation results with theirs. First, the initial allelic frequency of the recessive deafness allele was set to 1.304%. This frequency is approximately at the midpoint of the 0.6% to 3.5% reported range of carrier frequencies for the c.35delG variant in *GJB2* in white Americans and Europeans [9,27,28]. Simulations were run over 20 generations (400 years), which reflects the approximate time frame that signed languages are believed to have existed, deaf individuals have formed close social ties, and assortative mating among deaf individuals has been occurring [15]. The constant population size was set to 200,000 simulated individuals [15]. At each generation, a proportion of simulated hearing individuals were randomly selected (of which a small proportion, by random choice, carried a single recessive deafness allele), and assigned phenotypic deafness at a conservative rate of 0.8 per 1,000 simulated individuals, which is a measured frequency of profound deafness at birth [29,30]. This

assigned deafness, biologically, reflects genetic deafness due to other, complementary genes, deafness from epigenetic causes, and/or perinatal morbidity. Although the prevalence of identified deafness continues to increase throughout childhood to approximately 3.5 per 1,000 [30], this higher figure was not used in our simulations. Genetically deaf simulated individuals and simulated individuals with assigned deafness from other causes were mated together in the same pool. For our initial analysis, assortative mating was set to 0% and 90% to create two datasets for endpoint comparison; in subsequent analyses, simulations were run over a range of degrees of assortative mating. The 90% assortative mating figure is per Nance and Kearsy [15]; see Background for further detail.

Under these parameters, after 20 generations (400 years), the median frequency of deaf individuals with our recessive allele increased by 23% relative to the simulations with no assortative mating, that is, 0.017% as compared to 0.0220%, which is statistically significant (Fig 1 and Table 1; $n = 5,000$ simulations, Mann-Whitney $U = 5.83 \times 10^6$, $p < 10^{-308}$, common language effect size $f = 76.68\%$). This statistic was identical to the calculation of 0.0220% using equation (3) from Crow and Felsenstein [14] (Table 1) and described in Materials and Methods. Most of the change occurred within the first three generations. This figure is 7-fold less than the ~0.16% frequency reported elsewhere in a comparable simulation of deaf-deaf assortative mating with essentially the same parameters [15].

The frequency of the recessive deafness allele did not increase significantly; it was 1.304% versus 1.306% after 20 generations (Fig 1 and Table 1; $n = 5,000$ simulations, Mann-Whitney $U = 1.25 \times 10^7$, $p = 0.94$, common language effect size $f = 49.96\%$). Likewise, this figure is also much less than the ~1.7% frequency reported elsewhere in a simulation of deaf-deaf assortative mating with essentially the same parameters [15].

The inbreeding coefficient, F , was different: 0 versus 0.00376, which was statistically significant ($n = 5,000$ simulations, Mann-Whitney $U = 4.98 \times 10^6$, $p < 10^{-308}$, common language effect size $f = 80.09\%$). This increase in F was small since it was being attenuated because of competition for mates between the small number of simulated genetically deaf individuals and the larger pool of simulated individuals with assigned deafness due to other causes.

Fig 1. Effect over time of assortative mating on the frequencies of genetically deaf

individuals and a recessive deafness allele. Lines, from top to bottom, represent a five-number summary: 98% percentile, 75% quartile, median, 25% quartile, and 2% percentile. To the right of each subplot is a violin plot showing the distribution of the endpoint data. The tips of the violins represent the extrema. The vertical lines within the violins show the 2% through 98% percentile. The boxes within the violins show the first through third quartile. The cross-hatches show the medians. Simulations were run with relative fitness = 1.0 and other parameters as described in Materials and Methods.

We next ran simulations over a range of degrees of assortative mating (Fig 2 and Table 1). The frequency of deafness increased proportionately to assortative mating. Most of the change occurred in the first three generations. All differences in the frequency of deafness between each endpoint were highly significant with all $p < 10^{-40}$. The results also in close agreement with calculations using equation (3) from Crow and Felsenstein [14] (Table 1) and described in Materials and Methods. The allelic frequency, however, remained invariable regardless of the extent of assortative mating, and no statistically significant difference was found between any of the endpoints ($n = 5,000$ simulations, Kruskal-Wallis $H = 1.5$, $p = 0.69$, effect size $\eta^2 \approx 0.0\%$).

Fig 2. Effect of assortative mating on the frequencies of genetically deaf individuals and a

recessive deafness allele. Violin plots show the distributions of the endpoint data after 20 generations. The tips of the violins represent the extrema. The vertical lines within the violins show the 2% through 98% percentile. The boxes within the violins show the first through third quartile. The cross-hatches show the medians. Simulations were run with relative fitness = 1.0 and other parameters as described in Materials and Methods.

Synergistic Effects of Fitness And Assortative Mating on Allelic Frequency

Because assortative mating increases the phenotypic expression of alleles, it would therefore modulate the effects of selective pressure upon those alleles. Nance and Kearsey [15] have argued that relaxed fitness would be necessary for increasing the numbers of deaf individuals. We therefore simulated assortative mating across a range of relative fitnesses.

The frequency of the recessive deafness allele was sensitive to relative fitness, which became particularly noticeable at or above fitnesses of 1.5 when combined with assortative mating. (Fig 3 and Table 1).

Fig 3. Synergy of assortative mating and fitness on the frequencies of genetically deaf individuals and a recessive deafness allele. Right: no homogamy; left: 90% homogamy. Violin plots show the distributions of the endpoint data after 20 generations. The tips of the violins represent the extrema. The vertical lines within the violins show the 2% through 98% percentile. The boxes within the violins show the first through third quartile. The cross-hatches show the medians.

Deaf Individuals

	Degree of Assortative Mating			
	0%	30%	60%	90%
0.0	0.0105% (0.0050 - 0.0175%)	0.0105% (0.0055 - 0.0175%)	0.0105% (0.0055 - 0.0170%)	0.0105% (0.0050 - 0.0175%)
0.5	0.0130% (0.0070 - 0.0210%)	0.0135% (0.0070 - 0.0215%)	0.0135% (0.0075 - 0.0220%)	0.0140% (0.0075 - 0.0225%)
1.0	0.0170% (0.0100 - 0.0260%)	0.0180% (0.0105 - 0.0280%)	0.0195% (0.0110 - 0.0310%)	0.0220% (0.0125 - 0.0350%)
	0.0170%*	0.0182%*	0.0198%*	0.0220%*
1.5	0.0220% (0.0135 - 0.0330%)	0.0260% (0.0155 - 0.0400%)	0.0345% (0.0190 - 0.0575%)	0.0770% (0.0310 - 0.2845%)
2.0	0.0305% (0.0195 - 0.0440%)	0.0445% (0.0265 - 0.0690%)	0.1485% (0.0565 - 0.4425%)	29.20% (3.43- 64.1%)

Allelic Frequency

		Degree of Assortative Mating			
		0%	30%	60%	90%
Genetic Fitness	0.0	1.03% (0.908 - 1.16%)	1.03% (0.912 - 1.16%)	1.03% (0.910 - 1.16%)	1.03% (0.909 - 1.16%)
	0.5	1.15% (1.02 - 1.30%)	1.15% (1.01 - 1.30%)	1.15% (1.01 - 1.29%)	1.14% (1.00 - 1.28%)
	1.0	1.30% (1.15 - 1.47%)	1.30% (1.15 - 1.47%)	1.30% (1.15 - 1.47%)	1.31% (1.15 - 1.47%)
	1.5	1.49% (1.31 - 1.70%)	1.52% (1.33 - 1.74%)	1.56% (1.35 - 1.81%)	1.70% (1.41 - 2.22%)
	2.0	1.74% (1.52 - 2.00%)	1.86% (1.60 - 2.17%)	2.32% (1.78 - 3.41%)	36.4% (6.17 - 73.3%)

Table 1. Simulation results showing effects of assortative mating and fitness on the frequency of deafness after 200 years. Values given are medians, with 2% through 98% percentiles in parentheses. Values in bold and followed by an asterisk were calculated from equation (3) from Crow and Felsenstein [14] as described in Materials and Methods. Simulations were run as described in Materials and Methods.

Discussion

In this study, we addressed the century-old debate about whether deaf intermarriage increases the phenotypic expression of genetic deafness. We also investigated a recent claim, based on simulations, that assortative mating could increase the allelic frequency of the commonest deafness allele, which is recessive [15,16]. We ran forward-time computer simulations using the **simuPOP** package, which has been used by others for assortative mating simulations, to test the hypothesis that assortative mating among deaf Americans (deaf intermarriage; linguistic homogamy) would affect phenotypic deafness as well as allelic frequencies for recessive deafness [25,26]. For each scenario, we analyzed the results of 5,000 simulations. We used statistical analyses to compare not only median results, but also ending distributions. We used this approach in addition to mathematical modeling because it allowed us to capture the variance in results without underlying assumptions of parametricity, and allowed us to easily set up the more complex scenario of introducing individuals with acquired or complementary deafness to the mating pool.

Our simulations confirm that intense (90%) assortative mating would increase the frequency of homozygous deaf individuals by 23% over 20 generations. Most of this increase would occur within the first three generations of assortative mating. However, the simulations also confirmed

that assortative mating did not affect allelic frequencies at all (Fig 1 and 2 and Table 1). These simulation results are consistent with predictions from classical genetics models and in nearly identical agreement with mathematical calculations using Crow and Felsenstein's [14] equation (3) (Table 1). Our results did not match with the results of a computer simulation published elsewhere using essentially the same parameters, which predicted a ~7-fold increase in the number of homozygous deaf individuals, as well as a ~30% increase in the frequency of the recessive deafness allele [15].

Our simulation results also confirm that relative reproductive fitness impacts allelic frequencies. Because assortative mating increases the expression of rare alleles, relative fitness acted synergistically with assortative mating in our simulations to accelerate changes in recessive allelic frequencies. In our simulations with greatly exaggerated relative fitness (1.5x and 2x), allelic frequencies increased. However, these results do not apply to the worldwide deaf community today because there are no reports in the literature of any population with higher-than-normal relative fitness for deaf individuals. Instead, the literature uniformly reports depressed relative fitness, ranging from 0.31 to 0.91; the highest measured fitness of 0.91, which is still depressed, was from an educated American deaf sample from Gallaudet University [18-22]. Therefore, based on our simulations, the synergy of assortative mating with depressed fitness should be expected to constrain the frequency of recessive deafness alleles to low levels (Fig 3 and Table 1).

Nance [15] forwarded a hypothesis that assortative mating based on shared language compatibility, which he termed linguistic homogamy, among early humans may have accelerated the evolution of human speech genes, particularly *FOXP2*, some 150,000 years ago. Nance argued that improved language skills in early humans likely correlated with better cooperation, better survival and higher fitness. Our simulation results support this intriguing hypothesis. Preferential mating among those with advantageous language capabilities would have increased the expression of these alleles and synergistically accelerated this evolution.

In 2008, Arnos and colleagues [17] studied contemporary pedigrees collected from Gallaudet University alumni, and compared them with pedigrees from Fay's study, which were ascertained from deaf institutions across the country. Segregation analysis comparing these two datasets showed that the proportion of non-complementary pairings were 4.2% in the 1801-1899 Fay

dataset and 23% in the 2007 Gallaudet alumni dataset. Our simulation results show that assortative mating among the larger deaf community is not a sufficient explanation to explain all of this difference in non-complementary pairings between these two datasets. Rather, we agree with the authors' deliberations that the reason may lie in the difference between how these two datasets were ascertained [17]. The original Fay dataset were collected from deaf institutions across the country, whereas the newer dataset were collected only from Gallaudet alumni. The Gallaudet dataset likely represents a special subpopulation. Gallaudet, established in 1864, is the world's only university for deaf students. Approximately 95% of its undergraduate student body are deaf. Today, Gallaudet attracts legacy students from multigenerational deaf families, whose parents and, in some cases, grandparents had previously attended Gallaudet. While deaf individuals at the time of the original Fay dataset in 1890 were usually from hearing families and were themselves discouraged from marrying others from deaf families, there is a noted preference for contemporary individuals from deaf families to attend Gallaudet and to pair with others from deaf families because of cultural and linguistic compatibility. Genetically deaf individuals with multigenerational pedigrees, concentrated into the Gallaudet community and directly seeking out one another, bypasses competition from those with acquired deafness, increases the odds of non-complementation, and accelerates the phenotypic effects of assortative mating. However, (1) this is only happening within communities like Gallaudet's which are enriched for multigenerational deaf families, and does not reflect the genetic assortment of deaf individuals in the greater population; (2) the increase in phenotypic expression had already mostly occurred after the first three generations of intensive assortative mating and would be predicted to have tapered off already; and (3) regardless of the intensity of assortative mating, it has had no effect on the prevalence of deafness alleles in the overall population.

We are left with the puzzling paradox of how the commonest *GJB2* variant alleles causing severe to profound deafness: c.35delG, c.167delT, and c.235delC, have been measured at prevalences of between 1% and 4.4%, while measurements of reproductive fitness in deaf communities have been uniformly depressed [9-11,18-22]. These three frameshift alleles account for the majority of severe to profound nonsyndromic deafness in white Americans [9-11]. One possibility is mutation-selection equilibrium: novel *GJB2* mutations are perhaps being introduced at the same rate that mutations in the gene pool are being eliminated. Evidence showing a mutational hotspot at *GJB2*, particularly for deletion mutations, would provide support for this hypothesis. A

second, and intriguing possibility is that of balancing selection. Unrelated to studying deafness, Tran van Nhieu, Clair *et al.* [31] have shown in tissue culture experiments that *Shigella flexneri* requires *GJB2* connexons for egression into the intestinal epithelia, raising the possibility that the three common *GJB2* deletions could confer resistance to dysentery.

Connexons are dimers of hexameric proteins made up of individual connexins; in individuals with *GJB2* deletions, *GJB2* is replaced by other connexons to form connexins which appear to retain normal function everywhere except for the cochlea. Dysentery has been endemic at least since the advent of urbanization, and resistance to this disease via altered connexons may have provided enough positive selection to bring the commonest *GJB2* mutations to their present frequencies. This hypothesis is intriguing and should be investigated. Further, it would be interesting to see if this advantage exists only for *GJB2* variant homozygotes, or if heterozygous carriers for recessive *GJB2* deafness would also be resistant to shigellosis.

We hope that this study can put to rest the century-long argument put forth by Alexander Graham Bell [1] that deaf intermarriage increases deafness in the gene pool. Using simulations, and drawing upon mathematical modeling, with measurements and parameters collated from the published literature over more than a century of data, our results unequivocally affirm the classical models introduced by R.A. Fisher [12] and Sewell Wright [13]. That is, our data show that while deaf intermarriage initially had some effect on the incidence of phenotypic deafness, this effect was mostly completed by the third generation of assortative mating. In the time frame of American deaf institutions, this effect would have completed approximately around the end of the 19th century, when Fay [4] collected and reported his data. However, deaf intermarriage and assortative mating did not, and will not, change the prevalence of recessive deafness alleles unless there is strong positive selection present. Therefore, Alexander Graham Bell's [1] "deaf variety of the human race" will not happen even if deaf intermarriage and assortative mating continue at this rate.

Materials and Methods

Code and Dataset

The source code and dataset created for this study are publicly available from <https://github.com/derekbraun/homogamy.git> so that anyone can replicate our experiments and build upon our work.

Simulations

Simulations were performed using **simuPOP 1.1.10.8** which is a forward-time population genetics package, scriptable via Python, that has been used to simulate assortative mating [25,26]. Simulations were scripted with **Python 3.7.4** on a computer running **macOS 10.14.6**. Simulations were parallelized on a 16-core Intel Xeon workstation. It required 80 hours of CPU time to complete the final simulations shown in this manuscript. We modeled both assortative mating (homogamy) and reproductive fitness using a non-monogamous mating scheme. Non-monogamous mating was chosen, after some experimentation with code, because this allowed for better stability in the final proportion of homogamy per generation given the small number of deaf individuals in the simulated population. Sexes were not assigned to individuals; this was decided, after some experimentation with code, because it simplified coding and sped up execution time.

After each generation, the following was calculated: the frequencies of the dominant and recessive alleles A and a; the frequencies of the homozygous dominant, heterozygous, and homozygous recessive genotypes AA, Aa, and aa; the number of individuals with each genotype; the number and frequency of deaf individuals (including acquired deafness); and the inbreeding coefficient (*F*) calculated as follows:

$$F = \begin{cases} 1 - \frac{P(Aa)}{2pq}, & P(Aa) \leq 2pq \\ 0, & \text{otherwise} \end{cases}$$

The frequency of deafness alleles from simulations were also compared to those calculated from equation (3) of Crow & Felsenstein [14]. The effective assortative mating fraction, *r*, was derived from the % assortative mating (homogamy) and re-estimated after each generation by adjusting it by the size of the mating pool. This calculation matches the logic used in the forward

simulation script which is that the initial mating pool size included all forms of profound deafness at the rate of 0.8 per 1,000 individuals [29]. Therefore, initially and before assortative mating, q^2 individuals have genetic deafness due to connexin 26, and $0.008 - q^2$ individuals have acquired or complementary genetic deafness. At t_0 , $R_t = q^2$, so at t_0 , the expression for the mating pool size, $0.008 - q^2 + R_t$ simplifies to just 0.008. As assortative mating progresses in successive generations, R_t increases, and the mating pool size becomes slightly larger, as follows:

$$P(aa) = R_{t+1} = (1-r)q^2 + r \left[\frac{q^2 + R_t(p-q)}{1-R_t} \right], r = \text{homogamy\%} \left[\frac{R_t}{0.0008 - q^2 + R_t} \right]$$

Statistical Testing and Graphing

Statistical comparisons between datasets were performed using **SciPy 1.3.0**. We performed the Shapiro-Wilk test of normality on ending frequencies. Since these ending frequencies were often not normally distributed, and because we additionally wished to test for significant differences in both medians and variances, we used nonparametric tests: the Mann-Whitney U test for two independent groups or the Kruskal-Wallis test for k independent groups. Significant Kruskal-Wallis p -values were followed by *post hoc* pairwise Mann-Whitney tests without Bonferroni correction, which is more sensitive than Dunn's test [32]. Figures were generated in Python using **matplotlib 3.1.1**.

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