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5

- 2 Supplementary Methods
- 4 *Historical Background*
 - Beyond the important role of the phytochemical landscape driving insect herbivore diet breadth,
- 6 herbivorous insects are subject to a list of general factors that affect the diet breadth of foragers.
- 7 Originally broadly conceptualized for hunting animals by MacArthur & Pianka⁷, this list was adapted for
- 8 application to a pollinator diet by Wasser et al⁸. These factors are listed in Table S1 with common factors
- 9 between the two treatments.
- 10 11

12

- **Table S1:** Factors favoring specialization in foraging as detailed in MacArthur & Pianka⁷ and their
- corresponding construction in Waser et al's⁸ study on pollinator specialization. The third column describes the common factor in each treatment. The factor noted in green highlights the work which
- 13 14

Factors favouring specialisation of	Factors favouring generalisation of	Common factor
diet for hunting animals (MacArthur	diet for pollinators (Waser et al.	
and Pianka 1966)	1996)	
Greater food density	Pollinator lifespan is long relative to	The density of resources, as
	the flowering of individual plant	measured relative to the foraging
	species	range/period of the animal
Increased mobility of animal, or	Travel is costly	The cost associated with travelling to
decreased environmental resistance		many or few resources
to movement		
Increased differences between prey	Floral rewards are similar across plant	The inherent differences in resource
types, or increased specialisation of	species	quality
pursuing behaviour		
Increased mobility of prey, or greater	Constraints of behaviour and	The inherent difficulty involved in
difficulty in pursuit	morphology are minor	accessing different resources

15 16

21

17 Baseline model

18 As with recent studies of ecological networks¹⁰³¹, the makeup of the overall network model used

19 here has two major fundamental components: the structure of the pollination networks themselves and the

20 dynamics occurring on the networks.

- 22 plants (*p*) and animal pollinators (*a*) are present or absent, regardless of the strength of the link. Typical
- 23 ecological network studies have a collection of unique topological connections across different networks,
- 24 meaning only certain links of the possible links between plants and pollinators can potentially be realized

The structure of a network describes which links (representing species interactions) between

25 (Fig S1a). However, the networks we used in the models/simulations here were fully connected, meaning 26 all connections are possible (Fig S1b). The baseline of these networks in our study are sourced from an empirical pollination network³². Using a real-world pollination network as a basis ensured a plausible 27 28 ratio of flowering plant populations to pollinator populations, which in this case was 58 plant species to 29 100 pollinator species. The network was then fully connected (see Figure S1) such that each pollinator had potential access to all plant species and vis-versa. Fully connecting the plant-pollinator network was 30 31 done in order to give each pollinator population the maximum within-model range of dietary options. Doing so allows us to test the ability of the phenological mechanism to drive plasticity in pollinator 32 33 specialization without a priori constraints on pollinator behavior and network structure. The size of this 34 basic network framework was then modified to test effects of species richness, resulting in 3 network size 35 classes (N_p =plant richness, N_a =animal pollinator richness): $N_p = 58 \& N_a = 100, N_p = 48 \& N_a = 71$, and $N_p = 30$ plants & $N_a = 50$. While only these 3 network frameworks were used, the exact topology of 36 each changed with thousands of permutations of phenological parameters (see below). 37

38



Empirical Network

Fully Connected Network b)

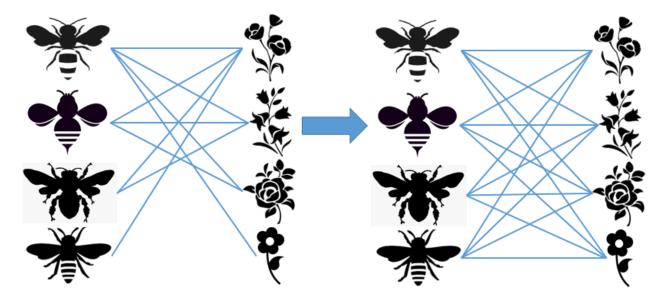


Figure S1: Underlying network structure. Example diagram describing the creation of the baseline network structure. Pictures of bees represent populations of pollinators and pictures of flowering plants 41 represent populations of flowering plants. Blue links between them represent a potential pollination 42 interaction between plants and pollinators. a) Example of a starting empirical network. b) Example of 43 44 fully connecting the empirical network to use in simulations.

45 46	The dynamics occurring on the networks refer to the internal population demographics (birth and
47	death) and species interactions taking place amongst the species in the network. In the case of our model,
48	species interactions refer to competition for resources, consumption of resources, and pollination events.
49	Dynamics were simulated based on the work of Valdovinos et al9 which mechanistically modeled
50	pollination as a consumer-resource interaction by separately accounting for vegetative abundance and
51	floral rewards consumed by pollinators. The model tracks the adaptive dynamics of each plant species'
52	population dynamics (p_i) , each animal pollinator species population dynamics (a_j) , each plant species'
53	pool of floral rewards (R_i) , and the adaptive dynamics of the per-capita foraging effort preferences of
54	each pollinator species for each plant species (α_{ij}). Model parameters are described in Table S2.
55 56 57 58 59 60 61 62 63 64 65 66 67 68 970 71 73 74 75 77 78 980 81 82 83 84	

		of interactions of animal <i>j</i>	
Definition	Symbol	Dimension	Mean Value
Density of plant population <i>i</i>	$p_i(t)$	individuals area ⁻¹	0.7*
Density of animal population <i>j</i>	$a_j(t)$	individuals area ⁻¹	0.7*
Density of floral resources of plant population <i>i</i>	$R_i(t)$	mass area ⁻¹	0.7*
Foraging Effort of pollinator <i>j</i> on plant <i>i</i>	$\alpha_{ij}(t)$	none	$\frac{1}{k_{\alpha_j}}^*$
Visitation Efficiency	$ au_{ij}$	visits area time ⁻¹ individuals ⁻¹ individuals ⁻¹	1
Expected number of seeds produced per pollination event	e _{ij}	individuals visits ⁻¹	0.8
Per capita mortality rate of plants	μ_i^P	time ⁻¹	0.002
Conversion efficiency of floral resources to pollinator births	C _{ij}	individuals mass ⁻¹	0.2
Per capita mortality rate for pollinators	μ_j^A	time ⁻¹	0.003
Pollinator extraction efficiency of resource R_i in each visit	b _{ij}	individuals visits ⁻¹	0.4
Max fraction of total seeds that recruit to plants	g_i	none	0.4
Intra-specific competition coefficient for plants	u _i	area individuals ⁻¹	1.2
Inter-specific competition coefficient for plants	w _i	area individuals ⁻¹	0.002
Production rate of floral resources	β_i	mass individuals ⁻¹ time ⁻¹	0.2
Self-limitation parameter for resource production	ϕ_i	time ⁻¹	0.04
Adaptation rate of pollinator foraging effort	Gj	none	2

Table S2: Baseline model state variables and parameters. In Mean Value column, * indicate initial conditions, k_{aj} is the number of interactions of animal j

Changes in population density of plant species (p_i) are calculated through:

89

90

$$\frac{dp_i}{dt} = \gamma_i \sum_{j \in A_j} e_{ij} \sigma_{ij} V_{ij} - \mu_i^{p_i} p_i \qquad \text{Eq (1)}$$

The second term in the equation describes background mortality, where μ_i^p is the constant

91 density-independent per-capita mortality rate of plant *i*. The first term describes plant population growth

92 where γ_i describes the realized fraction of seeds that successfully recruit to adults:

93
$$\gamma_i = g_i (1 - \sum_{l \neq i \in P} u_l p_l - w_i p_i) \qquad \text{Eq } (2)$$

94 where g_i is the maximum fraction of seeds that can potentially recruit to fecund adulthood. The

95 recruitment is subject to both interspecific (u_l) and intraspecific (w_i) competition with $u_l < w_i$. The

96 parameter e_i in Equation (1) is the constant max seed set induced by a pollination event between plant

97 and pollinator. The quality of each pollination event is determined by the fraction of pollen from

98 conspecific plants on a pollinator compared to other plant species pollen. This fraction is proportional to 99 the visits each animal pollinator (a_j) makes on each plant species (p_i) . We label this term, σ_{ij} and define 100 it as follows:

 $\sigma_{ij} = \frac{V_{ij}}{\sum_{k \in P_j} V_{kj}} \qquad \text{Eq (3)}$

101

where V_{ij} is the frequency of visits by animal species *j* to plant species *i* and it defined by:

103
$$V_{ij} = \alpha_{ij}\tau_{ij}T_{a_i}(t)a_jp_i \quad \text{Eq (4)}$$

104 Visits from pollinator *j* to plant species *i* are zero ($V_{ij} = 0$) if the two do not interact. Pollinator 105 *j*'s visitation efficiency on plant *i* is determined by the parameter τ_{ij} and is fixed at 1 for this study so as 106 not to bias any pollination interaction over others and affect visitation preferences a priori. The function 107 $T_{a_j}(t)$ is the phenological determinant of activity of pollinator a_j , in this case controlling the flight period 108 of a_j . See Phenology section below for more. The dimensionless function $0 \le \alpha_{ij} \le 1$ is the foraging 109 preference of pollinator *j* on plant *i* and changes over time as defined by:

110
$$\frac{d\alpha_{ij}}{dt} = T_{aj}(t)G_j\alpha_{ij}\left(c_{ij}\tau_{ij}b_{ij}R_i - \sum_{k\in P_j}\alpha_{kj}c_{kj}\tau_{kj}b_{kj}R_k\right) \qquad \text{Eq (5)}$$

where G_i is the basal adaptation rate of foraging preference. Higher or lower rates of G_i produce faster or 111 slower rates of adaptation based on changes seen inside the parentheses of Eq (5). c_{ii} represents the 112 constant per-capita conversion efficiency of pollinator i converting plant i's floral resources into j's 113 114 births. b_{ij} is the constant efficiency of pollinator j extracting plant i's floral resources (R_i). Pollinator j 115 allocates more foraging effort to plant species i whenever such reallocation increases j's food intake. 116 Such reallocation causes a commensurate reduce in foraging effort from other plant species. For every animal pollinator species $j, \sum \alpha_{ij} = 1$ for all plant species. Finally, the function $T_{\alpha_i}(t)$ appears here to 117 limit the adaptation of foraging preference only to periods when pollinators are actively flying. 118 119 Each plant *i*'s floral resources, R_i , changes over time as defined by:

120
$$\frac{dR_i}{dt} = T_{p_i}(t)\beta_i p_i - \phi_i R_i - \sum_{j \in A} V_{ij} b_{ij} \left(\frac{R_i}{p_i}\right) \qquad \text{Eq (6)}$$

121 where β_i is plant *i*'s per-capita resource production rate and ϕ_i is a constant self-limitation parameter. 122 Rewards of plant *i* are removed with an efficiency b_{ij} by pollinator *j* in proportion to the amount of visits, 123 V_{ij} . The function $T_{p_i}(t)$ controls the phenological expression of resource production in each flowering 124 plant *i*. Further details are provided below in Phenology section. The population dynamics of the animal 125 pollinators are then defined by:

126
$$\frac{da_j}{dt} = \sum_{i \in P} c_{ij} V_{ij} b_{ij} \left(\frac{R_i}{p_i}\right) - \mu_j^A a_j \qquad \text{Eq (7)}$$

where c_{ij} , V_{ij} , and b_{ij} are as defined above. Pollinator population growth is driven by the sum of resources gathered from pollination visits while death occurs at a constant rate μ_i^A .

129

130 Incorporating phenology into baseline model

131 Creating temporal plasticity in network connectivity is implemented by modifying the rates 132 controlling interactions between plants and pollinators in the network. In other words, the expression of 133 certain species' rates/behaviors are modified by time dependent functions which activate and deactivate 134 said rates across time. In flowering plant species, this is implemented by modifying the production of 135 floral rewards (R_i) that drive pollinator foraging preference (α_{ij}) and reproductive benefit for both plants 136 and pollinators. In Eq (6), the rate of floral reward production (β_i) is regulated across time steps by the 137 phenology function $T_{p_i}(t)$, Eq (8). Parameter definitions are given in Table S3.

138

139
$$T_{p_i}(t) = \left| f(b_{bv}) * \sin(b_{pt}\pi t - b_{w_s}) * \frac{\left(1 + square\left(\frac{b_{pt}}{2b_{bt}}\pi t - \frac{b_{w_s}}{2}, \frac{25}{b_{w_a}, b_{bt}}\right)\right)}{2} \right| \quad \text{Eq (8)}$$

Table S3: Phenology parameter definitions for $T_{p_i}(t)$

Phenology Parameter	Description	Definition
Bloom Period (b_p)	No. of time steps with floral resource production ($\beta > 0$)	Defined by user
Bloom Period translated (b_{pt})	Transforming b_p into useable form for T_{p_i}	$\frac{1}{b_p}$
Bloom break value (b_{bv})	No. of cycles between subsequent blooms	Defined by user
Bloom Break Translated (b_{bt})	Transforming b_{bv} into useable form for T_{p_i}	$\frac{b_{bv}}{2} + 0.5$
(d)	% of maximum separation between T_{p_i}	1
Separation distance (p_{sd})	Distance on the timeline between consecutive T_{p_i} , here N_p is the number of plant species	$\frac{\left(\frac{2\pi b_{bv}}{N_p}\right)}{d}$
Wave Shift (b_{w_s})	Separation distance assigned to each plant species in sequence.	$\{p_{s_d}*n\}_{n=0}^{N_p-1}$
Wave Augment (b_{w_a})	Augment to save shift in the square wave	$b_{bv} + 1$
$f(b_{bv})$	Function mitigating lost resources with higher break value by increasing floral reward production	<i>b</i> _{<i>bv</i>} + 2

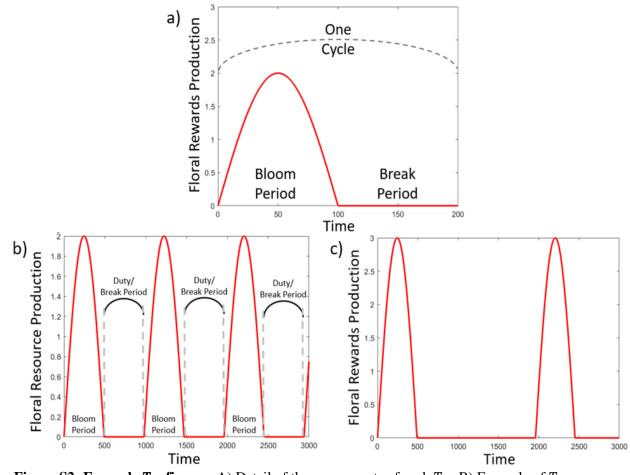
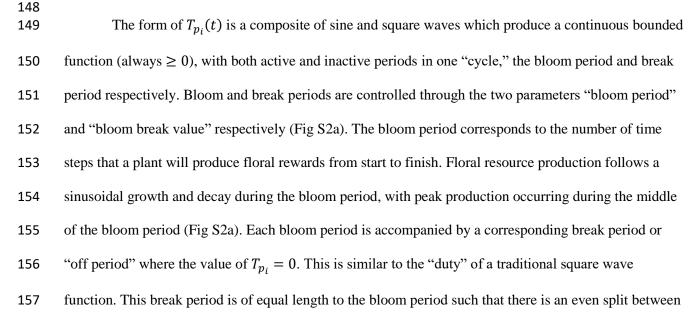
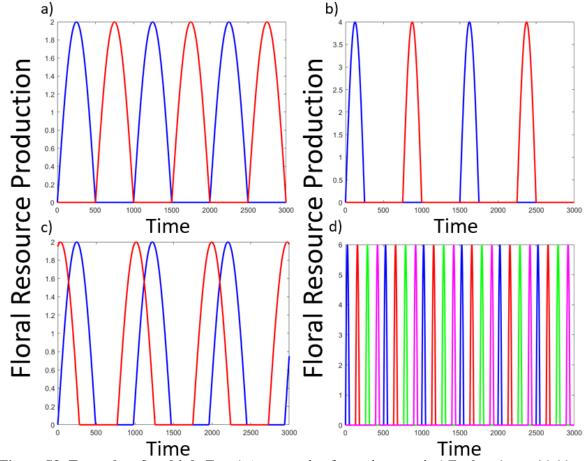


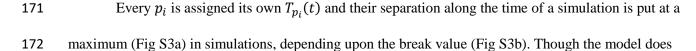
Figure S2: Example T_{p_i} figures. A) Detail of the components of each T_{p_i} . B) Example of T_{p_i} run across time. Bloom Period = 490, Break Period = 0. C) Example of T_{p_i} run across time. Bloom Period = 490, Break Period = 1.



active and inactive parts of a single cycle when the break value is 0. In this default formulation, T_{p_i} will cycle through active and inactive periods (Fig S2b), thereby modifying the production of floral rewards. When break value > 0, then T_{p_i} will skip the number of cycles assigned to the break value before the ensuing bloom period (Fig S2c). For the purpose of parity in comparing across different bloom periods, the length of a cycle's break period scales with its bloom period. This facilitates normalizing available resource quantities between bloom period.



164 **Figure S3: Examples of multiple** T_{p_i} . a) An example of two plant species' T_{p_i} functions with bloom 166 period of 500 and break values of 0. b) An example of two plant species' T_{p_i} functions with bloom 167 periods of 250 and break values of 2. c) An example of two overlapping plant species' T_{p_i} functions with 168 bloom periods of 500 and break values of 0. d) Example of multiple T_{p_i} for $i \in (1,4)$ with bloom periods 169 of 125 and break value of 4.



allow for more direct overlap (Fig S3c). This all then scales with the number of plant species, p_i , in the system (Fig S3d).

Phenology in bee species, T_{a_i} , is formulated similarly across visits (V_{ij}) in Eq (4) and G_j , the basal adaptation rate of foraging preference (α_{ij}), in Eq (5). Both visitation and adaptation are modified by T_{a_i} because foraging preference should not change when there is no active foraging. The formulation of T_{a_i} is given in Eq (9) and its parameter definitions are given in Table S4. Similar to $T_{p_i}(t)$, overall control of the specific form of T_{a_i} is governed by two parameters, "flight period" and "flight break value." The general form of $T_{p_i}(t)$ and $T_{a_i}(t)$ was chosen heuristically based on its ability to interface with the baseline model and the ability to maintain sufficient control over the specific form of the function with only two parameters. This makes it both readily applicable from a research stand point and relatively user friendly for other interested researchers.

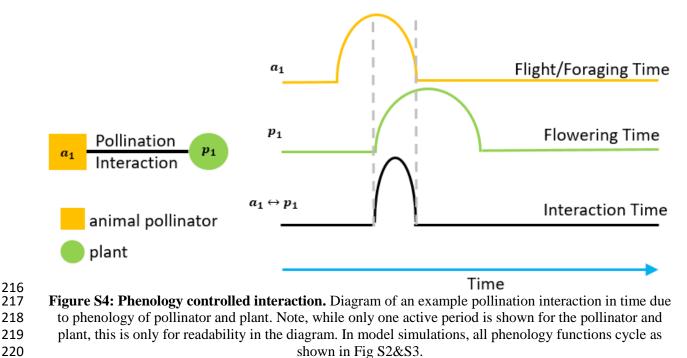
185
$$T_{a_i}(t) = \left| f(f_{bv}) * \sin(f_{pt}\pi t - f_{w_s}) * \frac{\left(1 + square\left(\frac{f_{pt}}{2f_{bt}}\pi t - \frac{f_{w_s}}{f_{w_a}'f_{bt}}\right)\right)}{2} \right| \quad \text{Eq (9)}$$

Table S4: Phenology parameter definitions for $T_{a_i}(t)$

Phenology Parameter	Description	Definition
Flight Period (f_p)	No. of time steps with active flight ($V > 0$ & $G_j > 0$)	Defined by user
Flight Period translated (f_{pt})	Transforming f_p into useable form for T_{a_i}	$\frac{1}{f_p}$
Flight break value (f_{bv})	No. of cycles between subsequent flights	Defined by user
Flight Break Translated (b_{bt})	Transforming f_{bv} into useable form for T_{a_i}	$\frac{f_{bv}}{2} + 0.5$
(d)	% of maximum separation between T_{a_i}	1
Separation distance for animal phenology (a_{sd})	Distance on the timeline between consecutive T_{a_i} , here N_a is the number of animal pollinator species	$\frac{\left(\frac{2\pi f_{bv}}{N_a}\right)}{d}$
Wave Shift (f_{w_S})	Separation distance assigned to each animal species in sequence.	$\{a_{sd} * n\}_{n=0}^{N_a-1}$
Wave Augment (f_{w_a})	Augment to save shift in the square wave	$f_{bv} + 1$
$f(f_{bv})$	Function mitigating lost flight time with higher break value by increasing peak flight activity	<i>f_{bv}</i> + 2

With both plant and animal phenology integrated into the model, the temporal plasticity of pollination interactions and network topology can be realized. When a pollinator *j*'s flight/foraging time overlaps with a plant *i*'s flowering time, the pollination interaction is potentially active (depending on foraging preference α_{ij}) and counted as a "link" in the network for the duration of the overlap (Fig S4). Otherwise, the link is inactive and interactions between the plant and pollinator do not occur.

215



222

This framework scales up to multiple interactions and ultimately the network level as network

topology changes dynamically as potential interactions activate and deactivate in the network across time.

A diagram of this is provided in a small example plant-pollinator network is provided in Fig S5. Given

foraging preference (α), even a potentially active interaction may not be particularly active, but only

during phenological overlap can the interaction potentially occur.

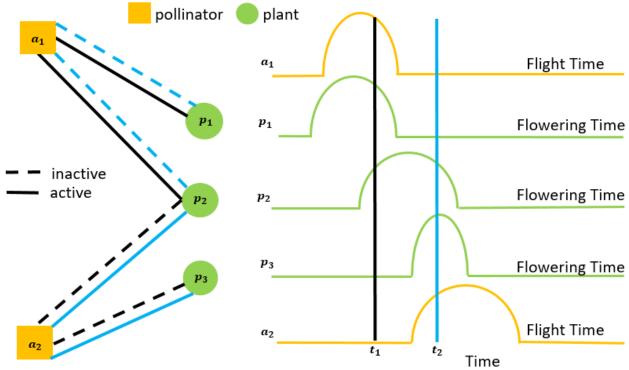


Figure S5: Diagram of example network with phenology. Example diagram of interacting phenologies changing the active topology of a small example network. At different times, as indicated by the black (t_1) and blue bars (t_2) , different links in the network at active. This scales up to the networks used in simulations and analysis here. Note, while only one active period is shown for each pollinator and plant, this is only for readability in the diagram. In model simulations, all phenology functions cycle as shown in Fig S2&S3.

236 Experimental simulation design

237 Without phenology induced oscillations, baseline model simulations generally achieve reach asymptotic dynamic behavior in approximately 3000 time steps. In order to ensure that transient dynamics 238 239 minimally affect measured model output, models here were run for 6000 time steps to reach asymptotic dynamics. No burn in period without phenology is used in simulations as that would produce preceding 240 241 bias to foraging preference before phenology functions are activated. All plant and pollinator species experience their phenological changes in rates from the beginning of simulations. 242 243 Baseline parameters for plants (non-phenological), including competition coefficients, floral reward productivity, reward self-limitation, and mortality differ among plant species by assigning unique 244 245 values stochastically varied within 0.1% of a mean value (Table S2). Competitive coefficients of plants are kept low (e^{-3}) in order to reduce effects on pollinator diet breadth through abundance loss and 246

247 potential species loss in plants (Table S1). Our simulations intentionally produced no extinctions in plants 248 or animals. Baseline parameters for animal pollinators (non-phenological, Table S2), including extraction 249 efficiency, conversion efficiency, and mortality differ among pollinator species by assigning unique 250 values stochastically varied within 0.5% of a mean value (Table S2). Similar to using fully connected 251 networks, limiting variability in baseline parameter values across species and pollination interactions 252 within single simulations allows us to focus analysis on the effect of phenology and temporal resource 253 overlap on specialization. Distinct differences in productivity between plants or efficiencies in pollinators 254 through more varied parameter values would bias foraging preferences towards certain interactions more 255 than others. For example, a highly productive plant or a pollinator with uniquely high fundamental 256 efficiency towards one plant species over others would drive specialization by assumption alone. Keeping 257 parameter values closely centered around the mean for all possible interactions limits this bias while still 258 allowing for moderate distinction in pollinator and plant traits. Our parameter set up best allows us to test 259 the ability of phenological mechanisms to drive plasticity in pollinator specialization without a priori 260 constraints on pollinator behavior though underlying baseline model parameters. Baseline model sensitivity analysis has been thoroughly investigated by past studies^{9,10,31} allowing 261 262 us to focus analysis on effects of phenology. Parameter sweeps across phenological parameters were done 263 with 37 combinations of bloom period and bloom break values for plant species. This created a

distribution of temporal overlap in floral resources across plant species (see Metrics) that was then tested

on bee phenologies composed of 56 combinations of flight period and flight break value. Each simulation

of the 2072 possible combinations of the plant and animal phenologies was replicated 10 times using

267 varied baseline (non-phenological) parameters (see paragraph above). While baseline model parameters

vary across both plant and pollinator species within single simulations, all flowering and flight phenology

269 parameters are shared across all plant and pollinator species respectively. This allows us to test the

270 phenological mechanism against numerous baseline parameters per pollination interaction per simulation.

Across all 2072 unique phenology parameter combinations simulated in each of our 3 network

frameworks, each replicated 10 times, we simulated 62160 plant-pollinator networks representing over 22
million distinct pollination interactions.

274

275 Choice of model bee genera & regions for empirical study

276 Andrena (Hymenoptera: Andrenidae) and Lasioglossum (Hymenoptera: Halictidae) were selected 277 as two contrasting model bee genera for this analysis. These two genera are the largest bee genera in the 278 world³³, and both are well represented in Northern Hemisphere bee communities. Andrena contains 279 around 1.500 species³⁴ and is distributed principally across the Holarctic with only a small number of species extending south to the Neotropics, sub-Saharan Africa and south-east Asia. Lasioglossum is a 280 larger genus, containing nearly 1,800 species³⁵, and has a more cosmopolitan distribution being found in 281 282 every continent except for Antarctica. The use of these large, widely distributed genera allows for 283 comparisons across different biogeographical regions within two distinct bee lineages, each with a shared 284 evolutionary history amongst its constituent species.

Andrena and Lasioglossum have notably different life history strategies. Andrena are 285 protandrous, with males emerging in advance of the females but at the same time of the year. Females 286 287 mate and then build nests and collect pollen and provision their offspring before dying. The pollen foraging period is short, typically lasing only a few weeks^{36,37}. In contrast, already mated *Lasioglossum* 288 289 females emerge in the spring and found nests. They collect pollen and rear offspring that often emerge 290 and overlap with their activity period. Some species are eusocial, and will produce a brood of workers 291 before producing reproductives³⁸. *Lasioglossum* species display a range of social behaviors from solitary to eusocial³⁹⁻⁴¹, sometimes even within the same species across different parts of its range⁴². However, 292 293 importantly, both social and solitary species of Lasioglossum have longer foraging periods than Andrena, typically spanning several months^{36,37,42}. Andrena can consequently be considered a genus comprised of 294 295 species with a 'short' foraging period, and Lasioglossum can be considered a genus of species with a 296 'long' foraging period, relative to one another (see also Selection and Standardization of pollen load 297 data).

Both genera are found within the major clade of short-tongued bees within Apoidea³⁵. Though 298 many species of short-tongued bees from across this clade have independently evolved elongate 299 proboscides to access nectar⁴³, morphological adaptations in Andrena or Lasioglossum bees for harvesting 300 301 pollen are almost unknown. Andrena (Scoliandrena) and Andrena (Hamandrena) possess hooked hairs on 302 the galea to pull pollen from the anthers of Cryptantha (Boraginaceae) and Anchusa (Boraginaceae) respectively, but these members of these subgenera are restricted to Western North America⁴⁴ and 303 304 southern and eastern Europe^{34,45} outside of our selected study regions of Britain and Michigan. In 305 Lasioglossum, members of the subgenus Sphecodogastra s.s. are specialists on Onagraceae, and possess a scopa comprised of unbranched and sparse hairs and bristles rather than the typical scopa of branched or 306 dense hairs³⁹. These species are restricted to North America³⁹. Although some species of Andrena and 307 308 Lasioglossum preferentially forage from more morphologically complex flowers (e.g. Fabaceae, Andrena 309 wilkella and Lasioglossum lativentre, ref 36), both genera as a whole favor shallow, open, and radially symmetrical flowers^{36,43,46}. 310

Plant species can have pollen that is difficult to digest by non-specialized bees⁴⁷, leading to 311 patterns of specialization or avoidance⁴⁸. Some plant species protect pollen physically by hiding it in deep 312 tubes (Boraginaceae), or in poricidal anthers (Ericaceae, Solanaceae), or nototribic anthers (Lamiaceae) 313 that deposit pollen on the bodies of bees⁴⁹. There is therefore considerable variation in the rewards offered 314 by different plant species. Conducting the analysis in Britain and Michigan, both of which are found in 315 316 the Holarctic biogeographic region, means that whilst the constituent species of the respective floras differ, the botanical families present are very similar^{50,51} and therefore likely to present rewards of a 317 similar composition and availability. Furthermore, the two regions provide suitable extremes in their 318 319 temporal resource overlap, making them ideal for addressing our hypothesis. The highly seasonal continental climate of Michigan²⁰ produces lower degrees of overlap and highly seasonal flowering 320 communities, while the more mild oceanic climate of the British Isles²⁰ and its consistent temperatures 321 produces longer, overlapping flowering times among plant species²¹. 322

Restricting the analysis to the same genera across two regions also controls for possible impacts of differing travel costs when gathering resources. In broad terms, bee species foraging range is influenced by body size, with larger species able to travel greater distances to forage⁵². As *Andrena* and *Lasioglossum* communities contain species of the same size across both regions, potentially interacting effects of travel costs are minimized.

The use of both *Andrena* and *Lasioglossum* within two Holarctic regions therefore controls as much as possible for the possible effects of phylogenetic structuring that may affect the cost of travel, constraints of morphology, and unequal rewards between plant families. By comparing within and between these genera across the two regions of Britain and Michigan, the relative importance of foraging period and environmental seasonality in structuring a generalized foraging response in wild bees can be determined.

334

335 Selection and standardization of pollen load data

336 Andrena are characterized as short-season bees, collecting pollen over only a period of a few weeks. However, some species of Andrena express bivoltine behavior, having two reproductive 337 338 generations in a single year. Although not unknown⁵³, bivoltinism is extremely rare in Nearctic Andrena and is not displayed by any of Andrena species in Michigan⁵⁴. In contrast, bivoltinism is displayed by 13 339 (13/60, 22%) of extant British Andrena species and nine (9/29, 31%) of species included in our British 340 dataset³⁷. In order to prevent bivoltinism affecting our categorization of Andrena as bees with a short 341 pollen foraging period, British Andrena with multiple generations were analyzed with each generation 342 343 considered a separate species.

Data on British *Andrena* and *Lasioglossum* pollen collection come from the datasets compiled in
Wood *et al.*⁵⁵ and Wood and Roberts⁵⁶. Data on Michigan *Andrena* come from Wood and Roberts⁴⁶.
These were combined with new data on Michigan *Lasioglossum*, and additional new pollen load data for
British *Lasioglossum*. Pollen was removed from these specimens and identified using light microscopy
following the same method across all specimens following the methodology of Wood and Roberts⁴⁶. The

349 size of pollen loads on individual bees was estimated, ranging from a full load to a one-eighth load. Pollen 350 grains were removed from the scopa using an entomological pin and transferred to a drop of water on a 351 microscope slide. Grains were left to absorb water for a few minutes and then the slides were gently 352 heated to allow evaporation. Molten glycerine jelly stained with fuchsin was added, and the slide was sealed with a coverslip. Following Müller and Kuhlmann⁴⁸, the percentage of the load composed of 353 354 different plant species was estimated along three randomly selected lines across the cover slip at a 355 magnification of ×400. The percentage of the load was estimated by the relative area of the slide occupied 356 by each plant species, rather than the absolute number of grains⁵⁷. Pollen species representing < 2% of the load were excluded from further analysis because their presence might have arisen from contamination. 357 358 The percentages of pollen collected were corrected according to the overall size of each load to give a 359 final weighting. Pollen loads were identified to the lowest taxonomic level possible using a reference 360 collection assembled during the project, in most cases to genus.

361 Though pollen was identified to genus, the analyses were conducted at the botanical family level. Specialist bees, or oligoleges, collect all their pollen from a single botanical family⁴⁸, and this is the level 362 at which most dietary specialization occurs in bees⁸. A minimum sample size of five pollen loads per 363 364 species was selected as the cut-off for inclusion in this study in order to maximize the number of species 365 included in the analysis. This sample size restriction meant that the first generation data for four British 366 bivoltine Andrena was excluded, resulting in an effective sample size of 34 species in the British Andrena 367 analysis (20 univoltine species, 5 species with data from both the spring and the summer generations, 4 368 species with data from the summer generation only).

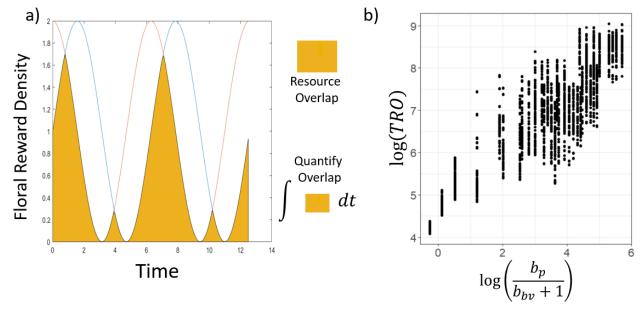
All together, these criteria produced a final dataset of 2,561 pollen loads from 120 species,
specifically 671 pollen loads from 51 Michigan *Andrena* species (63% of the *Andrena* fauna, ref 54), 355
pollen loads from 24 Michigan *Lasioglossum* species (30% of the *Lasioglossum* fauna), 815 pollen loads
from 29 British Andrena species (49% of the *Andrena* fauna, ref 37), and 731 pollen loads from 16

373 British *Lasioglossum* species (50% of the *Lasioglossum* fauna).

374	Only one species was shared between the British and Michigan datasets, the Holarctic Andrena
375	barbilabris. Because the British Andrena dataset compiled by Wood and Roberts ⁵⁶ focused on polylectic
376	species (species collecting pollen from multiple plant families), only two of the 29 species are oligoleges
377	(2/29, 7%), a significantly smaller proportion than the extant British fauna (20/59, 34%, Chi squared,
378	χ 2=7.3, p=0.007). Following Wood and Roberts ⁴⁶ , 10 species of oligolectic <i>Andrena</i> were added to this
379	dataset to bring this proportion in to line with the whole fauna (12/39, 31%, χ 2=0.1, p=0.790). Because
380	these are well-characterized oligolectic bees ³⁶ , no pollen load analysis was conducted for these species.
381	There were no differences in the proportion of specialists in the Lasioglossum datasets and the entire
382	regional fauna for Michigan ($\chi 2=0.3$, p=0.790) or Britain ($\chi 2=0.0$, p=1.000). Full details on the overall
383	Andrena and Lasioglossum faunas of Britain and Michigan, their dietary status, and species with pollen
384	load sample sizes included in this study can be found in Tables S6, S7, and S8.
385	
386	Metrics
387	In model simulations, temporal resource overlap between any two plant species is defined as the
388	shared area under each $R_i(t)$ curve (Fig S6a). The shared area can be found by:
389	1. Taking the minimum of any two R_1 and R_2 .
390	2. This will give you a new curve, $\min(R_1, R_2)$.
391	3. The area underneath this new curve $min(R_1, R_2)$ is the resource overlap between R_1 and R_2
392	(shaded region in Fig S6a).
393	4. This resource overlap can be quantified by taking the integral of $min(R_1, R_2)$. Integrals were
394	taken using the trapezoidal method with unit spacing through the trapz function in Matlab.
395	
396	Overlap per simulation was quantified as 1) total resource overlap summed across all p_i (labeled
397	<i>TRO</i>) and 2) average resource overlap experienced by each individual p_i (labeled <i>ARO</i>). Simply counting
398	overlapping shared time steps where $R_i > 0$ for two R_i would be an insufficient metric because it would

miss the quantity of resources that overlap in time. Our intuitive metric algorithm accounts for both shared time and quantity of overlapping resources. Modifying the bloom period (b_p) of plants with different bloom break values b_{bv} provided a suitably even coverage of overlap values, whether measured as total overlap (Fig S6b) or average individual plant overlap. The exact overlap of a simulation at any given value of log(bs/bbv+1) will vary depending on the pollinator community.

404



405

Figure S6: Details of overlap metrics. a) Diagram of overlap defined by two $R_i(t)$ curves. Two example 406 plant species rewards production curves across time $(R_i(t))$ are shown in red and blue. Shared area under 407 408 the curve is considered the overlapping resources and is shaded orange. Quantifying this area is done by 409 taking the integral of the shared area. b) Example from $58p \ge 100a$ web simulations of range in total resource overlap (TRO) provided by separating bloom period (b_p) values by bloom break values (b_{hv}) . 410 The denominator adds 1 to b_{bv} avoid dividing by 0 when $b_{bv} = 0$. Each dot represents overlap per 411 simulation at different b_p and b_{bv} values. The range in overlap per combination of b_p and b_{bv} comes 412 413 from the different phenology metrics tested for the pollinators. 414

Defining the confines of a specialist or generalist has been a long-running debate in ecology and evolutionary biology, with different sub-fields often using different metrics. For example, phylogenetic studies have found strong evidence of herbivorous insects specializing on plants at the family level¹³, while in other fields, such as network ecology, specialists and generalists have been defined by the number of species interactions through the degree distribution of links in the network⁵⁸. In order to

- 415 number of species interactions through the degree distribution of miks in the network . In order to
- 420 consider the range of ideas used in defining specialists and generalists, we have employed multiple

421 metrics to measured specialization that can be applied to both the foraging effort (α) based metrics of the

422 model and the pollen loads from our empirical data.

423 We label the first metric as "Deviation from Generalism" or DFG. For a single pollinator species,

424 DFG is defined as the degree away from completely even foraging efforts or pollen loads across all

425 possible resources. Specifically, DFG for a pollinator species *j* is defined as the sum of pairwise

426 differences of foraging effort across all plant species divided the number of plant species minus 1.

427 Parametrically, we can write:

428
$$DFG_{a_j} = \frac{\sum_{i,k \in p} |\alpha_{ij} - \alpha_{kj}|}{N_p - 1}$$
 Eq (10)

where DFG ranges from [0,1] with a perfect generalist scoring 0 and a complete specialist scoring 1. An

430 example is provided in Table S5.

431

Table S5: Example foraging preference matrix used to calculate DFG for pollinators from simulations (using α) or pollen load data. In the case of empirical pollen load data, the percent of pollen load is either grouped by plant family or plant genus.

Pollinators (model)	Effort on Plant 1	Effort on Plant 2	Effort on Plant 3	Effort on Plant 4	DFG
Pollinators (pollen)	Plant 1 Pollen %	Plant 2 Pollen %	Plant 3 Pollen %	Plant 4 Pollen %	DFG
Bee sp. 1	1.0	0	0	0	1
Bee sp. 2	0.5	0.5	0	0	0.667
Bee sp. 3	0.2	0.4	0.2	0.2	0.2
Bee sp. 4	0.25	0.25	0.25	0.25	0

435 436

In this example, the DFG scores would be calculated as follows:

437
$$DFG_{1} = \frac{|1-0| + |1-0| + |1-0| + |0-0| + |0-0| + |0+0|}{3} = \frac{3}{3} = 1$$

438
$$DFG_{2} = \frac{|0.5 - 0.5| + |0.5 - 0| + |0.5 - 0| + |0.5 - 0| + |0.5 - 0| + |0-0|}{3} = \frac{2}{3} = 0.667$$

439
$$DFG_{3} = \frac{|0.2 - 0.4| + |0.2 - 0.2| + |0.2 - 0.2| + |0.4 - 0.2| + |0.4 - 0.2| + |0.2 - 0.2|}{3} = \frac{0.6}{3} = 0.2$$

440
$$DFG_{4} = \frac{|0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |0.25 - 0.25| + |$$

442 When the DFG metric is used with pollen load data, the pollen amounts from each plant group in 443 a bee species' overall pollen load is broken into percentages and substituted for the model's foraging 444 effort (Table S5), under the assumption that higher pollen loads of any particular plant group generally 445 correspond to higher foraging effort on that group. The term group is used here because pollen data was 446 evaluated against both family and genus level plant data. The algorithm used to calculate our DFG score 447 is a holistic accounting for every possible interaction and compares all possible interactions amongst each 448 other to accumulate a score. However, it may not be the best option in all circumstances. While not necessarily requiring a complete accounting of all available resources, DFG's [0,1] range and attempt to 449 450 calculate specialization while considering all potential foraging options means DFG functions best when 451 available data can convincingly represent all possible foraging options. This is not necessarily guaranteed 452 in empirical surveys.

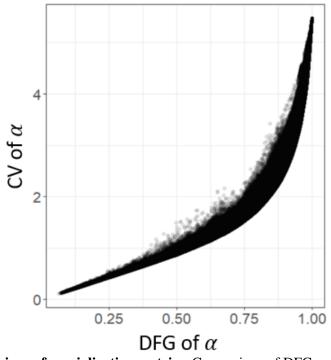
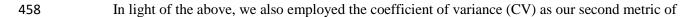
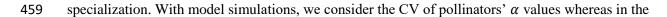


Figure S7: Comparison of specialization metrics. Comparison of DFG and CV from all model
 simulations in the 2nd largest network tested. Each dot represents a measurement from a single pollinator
 taken at the end of the simulation which in this case represents 7,061,376 data points.





empirical data we take CV of the percent of pollen load across plant groups. As a metric of specialization,
the CV will increase as when there are a limited number of extreme values. It performs the same whether
or not the full range of possible resource options for foraging pollinators is known. The relationship
between the two metrics is positive monotonic but non-linear (Fig S7) showing that the two metrics relate
to the measurement of specialization differently as desired.

465 In measuring model output, both DFG and CV metrics are measured in two ways. First each metric is taken on the α values at the end of each simulation (DFG_{End} & CV_{End} taken at t=6000). Second, 466 each metric is run on the α values averaged across the last 1000 time steps of each simulation (DFG_{Ava} & 467 CV_{Avq}). This is done to provide multiple points of comparison to our empirical pollen load data. One 468 could argue that pollen loads taken over multiple years would be better compared to model data taken 469 470 across an extended period of time steps. On the other hand, it could also be argued that foraging bees 471 collected for data are exhibiting an innate search pattern that is the end result of generations of evolved 472 behavior, better compared with the end state of simulations. Either way, the two methods are intuitively 473 correlated and using either supports our qualitative conclusions.

In measuring empirical pollen load data, we measured DFG and CV of bee species by grouping plants by either family level or genus level. Network studies in pollination ecology, including our model, tend to group plants at the species level. While, identifying pollen to species level is prohibitively difficult, genus level identifications allow for a closer approximation. However, studies focused on specialization in herbivores (particularly insects) have centered around grouping plants at the family level^{13,48,57}. Given the range, we decided to use both taxonomic levels and found that results were qualitatively similar regardless of grouping.

481

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482 Statistics
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483 Statistical analysis was done using R version 3.3.2⁵⁹. Differences in CV and DFG scores between
484 bee genera and geographic regions were tested using Kruskal-Wallis one-way analysis of variance tests.

- 485 Because both the CV and DFG scores were calculated from deeply non-normal underlying data
- 486 (necessarily so since patterns of diet breadth are decidedly non-normal at the botanical family level,
- 487 Forister *et al.* ref 13), it was not possible to transform them sufficiently to allow for parametric statistical
- 488 assessment. Regression analysis on model diet breadth results was done using the lm function and
- 489 measured with traditional R^2 metric when working with DFG_{End} results or with beta regressions (betareg
- 490 package in R) and the pseudo R^2 metric when working with DFG_{Ava} . When measuring diet breadth
- 491 results with CV_{End} or CV_{Ava} , log-linked gamma regressions were completed with the mgcv package and
- 492 measured with the for the amount of deviance accounted for by the regression model with the D^2 metric⁶⁰.
- 493
- 494 *Code availability & simulation information*
- 495 Simulation code, metric code, and simulation data are available at the repository
- 496 <u>https://github.com/fsvaldovinos/Phenology</u>.
- 497

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Supplementary Discussion

574 When considering the factors that drive specialization in insect herbivores, it is impossible not to 575 consider the role of plant chemistry. Phytochemical diversity, the diversity of plant compounds including 576 anti-herbivory defense compounds, has been strongly associated with both insect herbivore diversity and dietary specialization^{19,22,23}. For many insect herbivores, their diversity is much greater in tropical 577 578 environments. This is particularly well studied in Lepidoptera where both their species richness and 579 degree of specialization increases from temperate to tropical regions^{22,24}. However, a completely different 580 pattern is seen in the bees where tropical diversity and specialization is mediocre compared to diversity in Mediterranean and xeric environments where it is high^{8,25,26}. Indeed, tropical environments are dominated 581 582 by highly generalized and often social species that visit a huge variety of botanical families (e.g. ref 27,

583 28, 61).

584 Though the theoretical impact of variable quality between different resources is clear^{7,8}, bees have 585 an ecology that fundamentally differs from most insect herbivores. They are nest makers, and they collect 586 pollen as adults before feeding it to their offspring. Therefore, even though their larvae are immobile, they 587 are effectively mobile because they have the potential to feed on pollen collected from many botanical 588 families in a way that most larvae which must feed themselves are not, due to their limited mobility 589 during this stage of their development. In this regard bee larvae are functionally closer to those insects that are herbivorous during their adult stages such as Chrysomelid beetles⁶², and indeed these groups 590 591 show higher levels of generalization¹³.

The ability to feed their offspring from multiple combined sources has led to the suggestion that bees may adaptively pollen mix to negate the harmful properties of a particular pollen type that would be lethal if consumed as the sole source of larval nutrition⁶³. This mixing of different resources is however ultimately also affected by resource overlap, as it does not matter how much mobility an organism has if there are still limited different resources available to it during the course of its lifespan. Indeed, pollen mixing of botanical families identified as having negative pollen properties as a behavior is found in the *Andrena* of the UK but not those in Michigan⁴⁶. This is not to say that plant chemistry is unimportant for bees, and indeed there are many examples from within this group of plant chemistry driving and indeed restricting host plant choice^{47,64}. Instead, we argue that the fundamental difference in the life stage at which herbivory occurs means that for bees, inherent resource quality is relatively less important than resource availability, as defined by the balance between their inherent flight period and local flowering patterns. Clearly, despite existing in the same extremely phytochemically diverse landscapes, tropical bees have not evolved anything approaching the same high degree of dietary specialization as seen in the tropical Lepidoptera.

606 This weaker relationship in dietary specialization in bees compared to other insect herbivores is illustrated by directly comparing the overall pattern of specialization at the botanical family level. Species 607 608 in Michigan adhere more closely to a power law relationship, see Supplementary Figure S11a,c, similar to Forister et al¹³, but the pattern is much looser and closer to a zero-inflated Poisson distribution 609 610 (Supplementary Figure S11b, d). Constraining the number of dietary choices available to a mobile species 611 within its lifespan by reducing flowering overlap is directly analogous to reducing its mobility. Even if it 612 can fly, if there is only one flowering plant available then it is functionally the same as being an egg laid 613 on a plant; their choices are limited. We would therefore expect that phytochemical diversity and other 614 factors that influence resource quality would show the greatest impact on bee diets in environments where their choices are limited by flowering patterns. More studies on patterns of pollen collection in bees from 615 616 a wider variety of global environments are needed, but it would seem that the biggest driver of the 617 divergent patterns of herbivory seen in bees is their highly mobile period of pollen foraging as adults. 618

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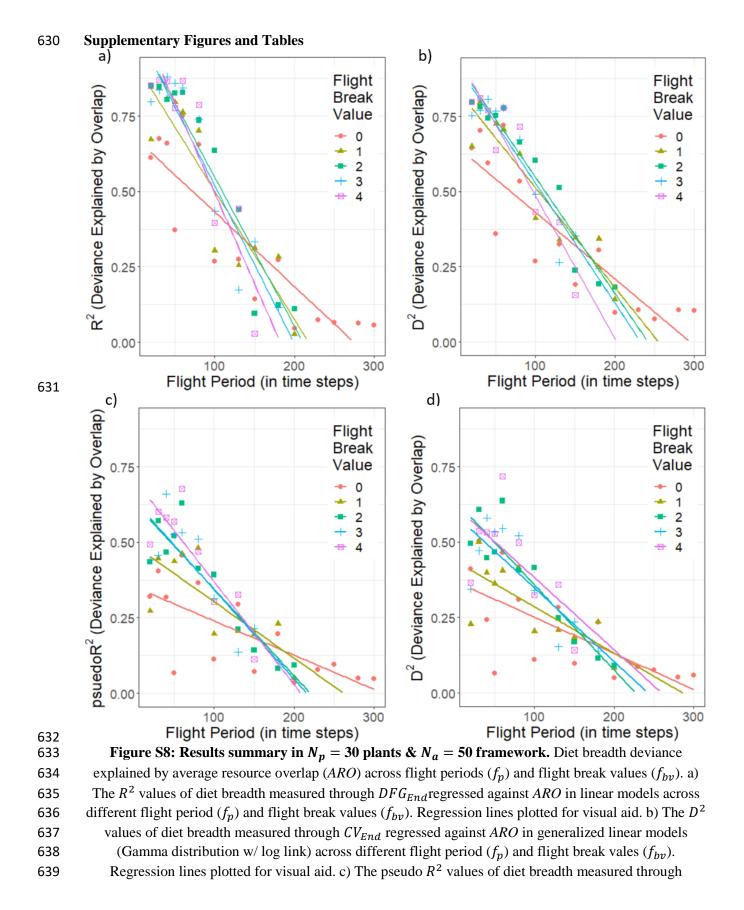
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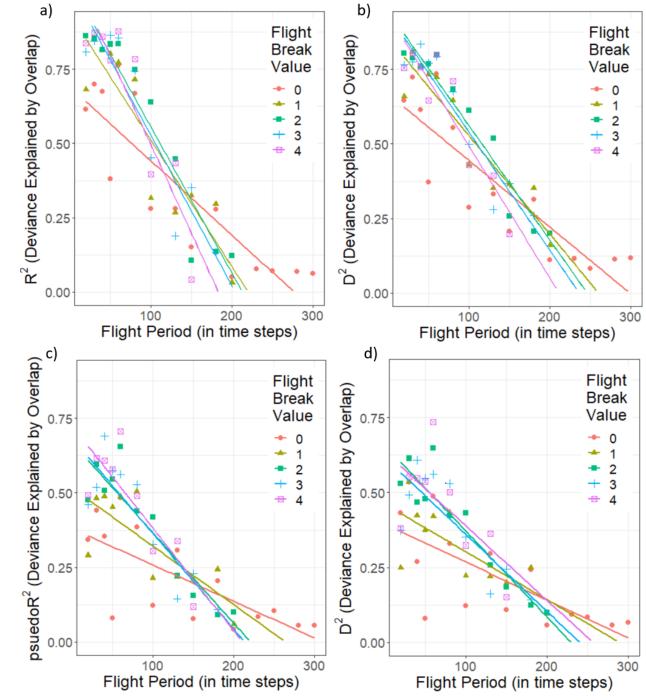
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 DFG_{Avg} regressed against ARO in beta regression models across different flight period (f_p) and flight break values (f_{bv}) . Regression lines plotted for visual aid. b) The D^2 values of diet breadth measured through CV_{Avg} regressed against ARO in generalized linear models (Gamma distribution w/ log link) across different flight period (f_p) and flight break vales (f_{bv}) . Regression lines plotted for visual aid. Overall, regardless of f_{bv} , there is a decrease in the effect of temporal resource overlap on diet breadth as the f_s of pollinators increases. Data taken from network framework w/ $N_p = 30$ plants & $N_a = 50$.

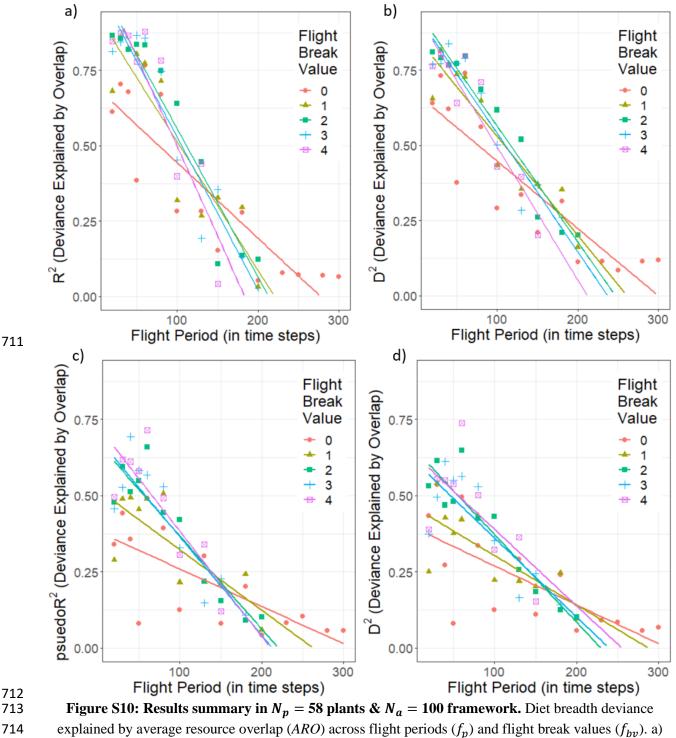


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674Figure S9: Results summary in $N_p = 48$ plants & $N_a = 71$ framework. Diet breadth deviance675explained by average resource overlap (ARO) across flight periods (f_p) and flight break values (f_{bv}) . a)676The R^2 values of diet breadth measured through DFG_{End} regressed against ARO in linear models across677different flight period (f_p) and flight break values (f_{bv}) . Regression lines plotted for visual aid. b) The D^2 678values of diet breadth measured through CV_{End} regressed against ARO in generalized linear models679(Gamma distribution w/ log link) across different flight period (f_p) and flight break vales (f_{bv}) .680Regression lines plotted for visual aid. c) The pseudo R^2 values of diet breadth measured through

681 682 683 684	DFG_{Avg} regressed against <i>ARO</i> in beta regression models across different flight period (f_p) and flight break values (f_{bv}). Regression lines plotted for visual aid. b) The D^2 values of diet breadth measured through CV_{Avg} regressed against <i>ARO</i> in generalized linear models (Gamma distribution w/ log link) across different flight period (f_p) and flight break vales (f_{bv}). Regression lines plotted for visual aid.
685	Overall, regardless of f_{bv} , there is a decrease in the effect of temporal resource overlap on diet breadth as
686	the f_s of pollinators increases. Data taken from network framework w/ $N_p = 48$ plants & $N_a = 71$.
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The R^2 values of diet breadth measured through DFG_{End} regressed against ARO in linear models across

different flight period (f_p) and flight break values (f_{bv}). Regression lines plotted for visual aid. b) The D^2

values of diet breadth measured through CV_{End} regressed against ARO in generalized linear models (Gamma distribution w/ log link) across different flight period (f_p) and flight break vales (f_{bv}) .

Regression lines plotted for visual aid. c) The pseudo R^2 values of diet breadth measured through

 DFG_{Avg} regressed against ARO in beta regression models across different flight period (f_p) and flight

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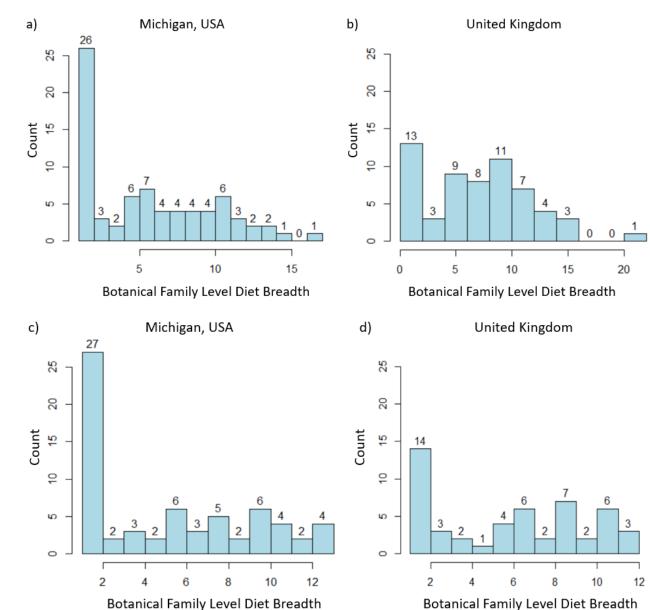
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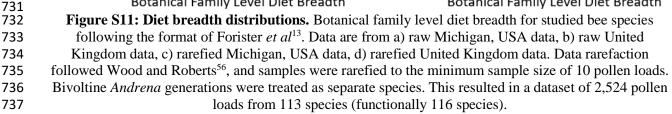
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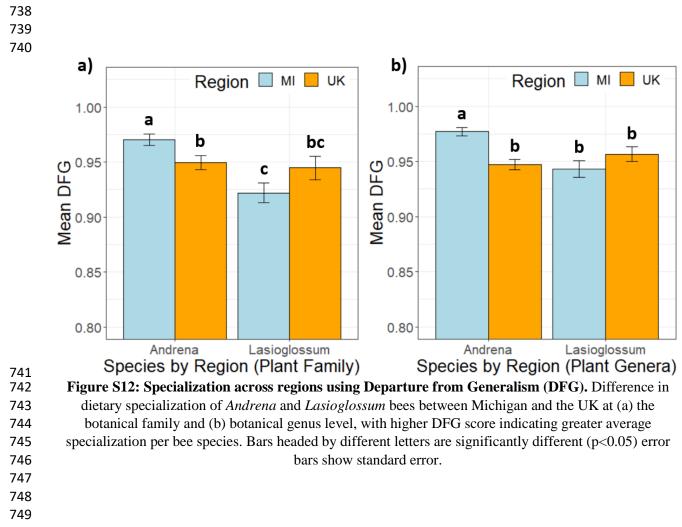
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break values (f_{bv}) . Regression lines plotted for visual aid. b) The D^2 values of diet breadth measured through CV_{Avg} regressed against *ARO* in generalized linear models (Gamma distribution w/ log link) across different flight period (f_p) and flight break vales (f_{bv}) . Regression lines plotted for visual aid. Overall, regardless of f_{bv} , there is a decrease in the effect of temporal resource overlap on diet breadth as the f_s of pollinators increases. Data taken from network framework w/ $N_p = 58$ plants & $N_a = 100$.

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Subgenus	Michigan species	Host range	British species	Host range
Andrena s. str.	carolina Viereck	Vaccinium	apicata Smith	Salix
	<i>clarkella</i> Kirby	Salix	<i>clarkella</i> Kirby	Salix
	frigida Smith	Salix	fucata Smith	
	mandibularis Robertson		<i>fulva</i> Müller	
	milwaukeensis Graenicher		helvola L.	
	rufosignata Cockerell		lapponica Zetterstedt	
	thaspii Graenicher		praecox Scopoli	Salix
	tridens Robertson		synadelpha Perkins	
			varians Rossi	
Callandrena s.l.	aliciae Robertson	Asteraceae		
	asteris Robertson	Solidago		
	gardineri Cockerell	Packera		
	helianthi Robertson	Helianthus		
	krigiana Robertson	Krigia		
	placata Mitchell	Solidago		
	rudbeckiae Robertson	Rudbeckia		
	simplex Smith	Solidago		
Charitandrena	1		hattorfiana Fabricius	Dipsacaceae
Chlorandrena			humilis Imhoff	Asteraceae
Chrysandrena			fulvago Christ	Asteraceae
Cnemidandrena	canadensis Dalla Torre	Solidago	denticulata Kirby	Asteraceae
	chromotricha Cockerell	Asteraceae	fuscipes Kirby	Ericaceae
	<i>hirticincta</i> Provancher	Solidago	nigriceps Kirby	211000000
	nubecula Smith	Solidago	simillima Smith	
	parnassiae Cockerell	Parnassia	Sinterna Sinti	
	peckhami Cockerell	Helianthus		
	robervalensis Mitchell	Solidago		
Conandrena	bradleyi Viercek	Vaccinium		
Euandrena	algida Smith	Salix	bicolor Fabricius	
Бианатена	geranii Robertson	Hydrophyllum	ruficrus Nylander	Salix
	nigrihirta Ashmead	nyuropnyuun	<i>rujierus</i> Nylandei	Sun
	polemonii Robertson	Polemonium		
Gonandrena	fragilis Smith	Cornus		
Gonunarena	<i>integra</i> Smith	Cornus		
	<i>persimulata</i> Viereck	Cornus		
	<i>platyparia</i> Robertson	Cornus		
Holandrena	<i>cressonii</i> Robertson	Cornus	labialis Kirby	
			-	
Hoplandrena			<i>bucephala</i> Stephens <i>ferox</i> Smith	Quaraus
			<i>rosae</i> Panzer	Quercus
			scotica Perkins	
Iomoliana	violas Dobantean	Viola	trimmerana Kirby	
Iomelissa Langu dugu a	violae Robertson	Viola		
Larandrena Lavoan duan a	miserabilis Cresson		ano outata Conith	
Leucandrena	barbilabris Kirby	Employ .	argentata Smith	
M 1	erythronii Robertson	Erythronium	barbilabris Kirby	D'
Margandrena Melandrena			marginata Fabricius	Dipsacaceae
	carlini Cockerell		cineraria L.	
	commoda Smith		nigroaenea Kirby	
	dunningi Cockerell		<i>nitida</i> Müller	
	hilaris Smith nivalis Smith		<i>thoracica</i> Fabricius <i>vaga</i> Panzer	Salix

751	Table S6. Extant Andrena species of Michigan and Britain and their dietary status. Species are ordered by
752	subgenus. Species without a listed host range are polylectic.

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81	42	59	<u>20</u> 33.9
		gravida Imhoff	
minimut Cocketell		flavipes Panzer	
	Salix		
virginiana Mitchell	c l:		
spiraeana Robertson			
0	Salix		
mirandra Smith			
mariae Robertson	Salix		
		haemorrhoa Fabricius	
<i>w-scripta</i> Viereck			
bisalicis Viereck	Salix		
		<i>tarsata</i> Nylander	Potentilla
			Fabaceae
			Fabaceae
wheeleri Graenicher			
nasonii Robertson		congruens Schmiedeknecht	
<i>imitatrix</i> Cresson			
	Drassicaceae		
	Brossiances		
brevipalpis Cockerell	Rhus		
erigeniae Robertson	Claytonia	0 2	
distans Provancher	Geranium	angustior Kirby	riplaceae
			<i>Bryonia</i> Apiaceae
			Bryonia
		tibialis Kirby	
			Brassicaceae
crataegi Robertson		•	Brossianasa
wellesleyana Robertson	Salix		
andrenoides Cresson	Salix		
			Apiaceae
		chrysosceles Kirby	A -
ziziae Robertson	Apiaceae	subopaca Nylander	
salictaria Robertson	Salix	semilaevis Pérez	210000000
0		niveata Friese	Brassicaceae
illinoensis Robertson	Salix	alfkenella Perkins	
	 melanochroa Cockerell neonana Viereck nigrae Robertson personata Robertson salictaria Robertson ziziae Robertson andrenoides Cresson wellesleyana Robertson crataegi Robertson distans Provancher erigeniae Robertson brevipalpis Cockerell robertsonii Dalla Torre arabis Robertson alleghaniensis Viereck imitatrix Cresson nasonii Robertson wheeleri Graenicher bisalicis Viereck w-scripta Viereck ceanothi Viereck forbesii Robertson hippotes Robertson mariae Robertson mariae Robertson mirandra Smith nuda Robertson rehni Viereck rugosa Cockerell sigmundi Cockerell spiraeana Robertson virginiana Mitchell erythrogaster Ashmead perplexa Smith wilmattiae Cockerell 	melanochroa Cockerell neonana Viereck nigrae Robertson salictaria Robertson ziziae RobertsonSalix Apiaceaeandrenoides Cresson wellesleyana Robertson crataegi RobertsonSalix Salixdistans Provancher erigeniae Robertson brevipalpis Cockerell robertsonii Dalla Torre arabis Robertson alleghaniensis Viereck imitarix Cresson wheeleri GraenicherGeranium Claytonia Rhus Brassicaceaebisalicis Viereck imitarix Cresson nasonii Robertson wheeleri GraenicherSalix salixbisalicis Viereck imitarix Cresson nasonii Robertson wheeleri GraenicherSalix salixbisalicis Viereck imitarix Cresson nasonii Robertson wheeleri GraenicherSalix salixbisalicis Viereck imitarix Cresson nasonii Robertson wheeleri GraenicherSalix salixbisalicis Viereck irreck forbesii Robertson hippotes Robertson rehni Viereck rugosa Cockerell sigmundi Cockerell sigmundi Cockerell sigmundi Cockerell sigmundi Cockerell salixSalix salixsalix wirginiana Mitchell erythrogaster Ashmead perplexa Smith wilmattiae CockerellSalix	melanochroa Cockerellfalsifica Perkinsnigrae Robertsonminutula Kirbypersonata RobertsonSalixsalictaria RobertsonSalixziziae RobertsonApiaceaesultaria RobertsonSalixwellesleyana RobertsonSalixcrataegi RobertsonSalixcrataegi RobertsonSalixcrataegi RobertsonSalixcrataegi RobertsonSalixcrataegi RobertsonSalixcrataegi RobertsonSalixcrataegi RobertsonClaytoniagrospina Thompsonpilipes Fabriciustibialis KirbyIabialis KirbylabertsonClaytoniabrevipalpis CockerellRhusrobertsoni Dalla TorreBrassicaceaearabis RobertsonBrassicaceaealleghaniensis ViereckSalixwescripta ViereckSalixwescripta ViereckSalixwescripta ViereckSalixforbesit RobertsonSalixpisalicis ViereckSalixmaraa RobertsonSalixforbesit RobertsonSalixmaraa

- **Table S6 Notes.** Wood and Roberts⁴⁶ added 11 oligolectic species to their analysis, including *Andrena lapponica* Zetterstedt. However, Müller⁶⁵ demonstrated that this species is polylectic, and so it was not
- visual result of the used in the analysis presented in the current paper.
- 757 Gibbs *et al.*⁵⁴ listed *Andrena barbara* Bouseman & LaBerge, *A. morrisonella* Viereck, *A. confederata*
- 758 Viereck and *A. wilkella* Kirby as part of the Michigan fauna. Examination of material at the University of
- 759 Michigan Museum of Zoology (Ann Arbor, Michigan) has shown that the record of *A. barbara* is based
- on a misidentification (TJW, *unpublished data*). The status of *Andrena morrisonella* is still taxonomically
- 761 uncertain and females cannot be reliably separated from A. *imitatrix*⁶⁶. Andrena confederata was recorded
- from Michigan on the basis of a single male that cannot be found⁵⁴, and repeated searching at the locality
- has not produced any more records of this species. Andrena wilkella is introduced to North America⁶⁷.
- These species have therefore been excluded from the Michigan fauna for the purposes of this study.

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767	Table S7. Extant pollen-collecting Lasioglossum species of Michigan and Britain and their dietary status.
768	Species are ordered by subgenus. Species without a listed host range are polylectic.

Subgenus	Michigan species	Host range	British species	Host range
Dialictus	abanci Crawford		cupromicans Pérez	
	achilleae Mitchell		leucopus Kirby	
	admirandum Sandhouse		morio Fabricius	
	albipenne Robertson		smeathmanellum Kirby	
	anomalum Robertson			
	atwoodi Gibbs			
	bruneri Crawford			
	callidum Sandhouse			
	cattellae Ellis			
	ceanothi Mitchell			
	coeruleum Robertson			
	coreopsis Robertson			
	cressonii Robertson			
	dreisbachi Mitchell			
	ellisae Sandhouse			
	ephialtum Gibbs			
	fattigi Mitchell			
	floridanum Robertson			
	foveolatum Robertson			
	gotham Gibbs			
	hartii Robertson			
	heterognathum Mitchell			
	hitchensi Gibbs			
	illinoense Robertson			
	<i>imitatum</i> Smith			
	laevissimum Smith			
	<i>leucocomum</i> Lovell <i>lineatulum</i> Crawford			
	nigroviride Graenicher			
	novascotiae Mitchell			
	oblongum Lovell obscurum Robertson			
	oceanicum Cockerell			
	paradmirandum Knerer &			
	Atwood			
	<i>perpunctatum</i> Ellis			
	pictum Crawford			
	<i>pilosum</i> Smith			
	planatum Lovell			
	pruinosum Robertson			
	rufulipes Cockerell			
	sagax Sandhouse			
	sheffieldi Gibbs			
	smilacinae Robertson			
	subversans Mitchell			
	subviridatum Cockerell			
	taylorae Gibbs			
	<i>tegulare</i> Robertson			
	<i>tenax</i> Sandhouse			
	timothyi Gibbs			
	trigeminum Gibbs			
	versans Lovell			

	versatum Robertson				
	vierecki Crawford				
	viridatum Lovell				
	weemsi Mitchell				
	zephyrum Smith				
Evylaeus s.s.	cinctipes Provancher				
Hemihalictus	birkmanni Crawford		angusticeps Perkins		
	fedorense Crawford		brevicorne Schenck	Ast	eraceae
	foxii Robertson		<i>minutissimum</i> Kirby		
	inconditum Cockerell		<i>nitidiusculum</i> Kirby		
	lustrans Cockerell	Asteraceae	parvulum Schenck		
	macoupinense Robertson		pauperatum Brullé		
	nelumbonis Robertson	Nymphaceae	punctatissimum Schenck		
	pectorale Smith		puncticolle Morawitz		
	swenki Crawford		rufitarse Zetterstedt		
			semilucens Alfken		
			sexstrigatum Kirby		
			villosulum Kirby	Ast	eraceae
Lasioglossum	acuminatum McGinley		laevigatum Kirby		
s. str.	athabascense Sandhouse		lativentre Schenck		
	coriaceum Smith		prasinum Smith		
	forbesii Robertson		quadrinotatum Kirby		
	fuscipenne Smith		xanthopus Kirby		
	paraforbesii McGinley				
Leuchalictus			leucozonium Schrank		
			<i>zonulum</i> Smith		
Sphecodogastra	comagenense Knerer &		albipes Fabricius		
spheeouogushu	Atwood		uno ip es 1 doniends		
	oenothera Stevens	Oenothera	calceatum Scopoli		
	quebecense Crawford		fratellum Pérez		
	seillean Gibbs & Packer		fulvicorne Kirby		
	texanum Cresson	Oenothera	laticeps Schenck		
	truncatum Robertson		malachurum Kirby		
			pauxillum Schenck		
Total:	77	4	-	32	2
Proportion oligole	action	5.2			6.3

Table S7 Notes. The parasitic L. lionotum Sandhouse, L. michiganense Mitchell, and L. platyparium

Robertson⁵⁴ do not collect pollen and so were excluded from the faunal list for this study. *Lasioglossum leucozonium* and *Lasioglossum zonulum* are introduced to North America^{54,67} and so were also excluded.

Table S8. Summary of the species included in this study and the number of analyzed pollen loads per species.

Michigan dataset		British dataset	
Species	Sample size	Species	Sample size
Andrena algida	11	Andrena alfkenella	23
Andrena aliciae	5	Andrena angustior	18
Andrena alleghaniensis	13	Andrena argentata	11
Andrena andrenoides	15	Andrena barbilabris	7
Andrena arabis	10	Andrena bicolor	41
Andrena barbilabris	23	Andrena bimaculata	13
Andrena bradleyi	9	Andrena chrysosceles	39
Andrena brevipalpis	25	Andrena cineraria	16
Andrena canadensis	6	Andrena denticulata	16
Andrena carlini	21	Andrena dorsata	55
Andrena carolina	5	Andrena flavipes	74
Andrena ceanothi	16	Andrena fucata	15
Andrena chromotricha	6	Andrena fulva	6
Andrena commoda	12	Andrena haemorrhoa	49
Andrena crataegi	28	Andrena helvola	12
Andrena cressonii	21	Andrena labialis	12
Andrena distans	5	Andrena labiata	10
Andrena erigeniae	7	Andrena minutula	74
Andrena erythrogaster	14	Andrena minutuloides	53
Andrena forbesii	25	Andrena nigriceps	5
Andrena frigida	11	Andrena nigroaenea	22
Andrena gardineri	5	Andrena nitida	28
Andrena geranii	5	Andrena scotica	39
Andrena helianthi	6	Andrena semilaevis	98
Andrena hippotes	22	Andrena subopaca	16
Andrena hirticincta	13	Andrena synadelpha	9
Andrena illinoiensis	8	Andrena thoracica	10
Andrena imitatrix	15	Andrena trimmerana	18
Andrena integra	10	Andrena wilkella	24
Andrena mandibularis	13	Indicita wineita	21
Andrena miranda	19	plus 10 olioglectic species	
Andrena miserabilis	23	plus to onogleene species	
Andrena nasonii	20	Andrena ferox	
Andrena nigrihirta	6	Andrena florea	
Andrena nivalis	13	Andrena fuscipes	
Andrena nubecula	7	Andrena hattorfiana	
Andrena nuda	10	Andrena marginata	
Andrena perplexa	10	Andrena nigrospina	
Andrena placata	9	Andrena nitidiuscula	
Andrena platyparia	9 7	Andrena niveata	
Andrena platyparta Andrena robertsonii	10		
		Andrena proxima Andrena tarsata	
Andrena rudbeckiae	8	Anarena tarsata	
Andrena rufosignata	19		
Andrena rugosa	17		
Andrena spiraeana	13		
Andrena thaspii	9		
Andrena vicina	37		
Andrena virginiana	13		
Andrena wellesleyana	9		
Andrena w-scripta	16		
Andrena ziziae	11		

Total	671	Total	804
Lasioglossum acuminatum	20	Lasioglossum albipes	8
Lasioglossum anomalum	12	Lasioglossum calceatum	38
Lasioglossum cattellae	8	Lasioglossum fulvicorne	12
Lasioglossum cinctipes	12	Lasioglossum laevigatum	11
Lasioglossum coriaceum	24	Lasioglossum lativentre	18
Lasioglossum cressonii	28	Lasioglossum leucopus	11
Lasioglossum foxii	11	Lasioglossum leucozonium	26
Lasioglossum hitchensi	18	Lasioglossum malachurum	437
Lasioglossum imitatum	23	Lasioglossum morio	15
Lasioglossum laevissimum	19	Lasioglossum parvulum	12
Lasioglossum leucocomum	18	Lasioglossum pauxillum	70
Lasioglossum lineatulum	17	Lasioglossum prasinum	8
Lasioglossum lustrans	7	Lasioglossum puncticolle	13
Lasioglossum macoupinense	6	Lasioglossum villosulum	29
Lasioglossum nigroviride	7	Lasioglossum xanthopus	11
Lasioglossum oenothera	5	Lasioglossum zonulum	12
Lasioglossum paradmirandum	8	-	
Lasioglossum paraforbesii	15		
Lasioglossum pectorale	24		
Lasioglossum pilosum	25		
Lasioglossum quebecense	6		
Lasioglossum subviridatum	8		
Lasioglossum versans	7		
Lasioglossum versatum	27		
Total	355	Total	731
Grand total	1026	Grand total	1535

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Table S9: Pollen load data. The pollen load percentages and botanical family counts of sampled
 Andrena and Lasioglossum bees from both the U.K. and Michigan, USA. Please find the data attached as
 an .xls file separated by location and botanical taxonomic level.

Table S10: Simulation phenology parameters. The phenology parameters for both pollinators andplants used in simulations. All potential combinations of the listed parameters were used to give 2072unique phenological bases per network framework. Please find the data attached as an .xls file.

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