

1 **Title**

2 Review and performance evaluation of trait-based between-community dissimilarity measures

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10

11 **Abstract**

- 12 1. In the recent years a variety of indices have been proposed with the aim of quantifying
13 functional dissimilarity between communities. These indices follow different
14 approaches to account for between-species similarities in the calculation of
15 community dissimilarity, yet they all have been proposed as straightforward tools.
- 16 2. In this paper we reviewed the trait-based dissimilarity indices available in the
17 literature, contrasted the approaches they follow, and evaluated their performance in
18 terms of correlation with an underlying environmental gradient using individual-based
19 community simulations with different gradient lengths. We tested how strongly
20 dissimilarities calculated by different indices correlate with environmental distances.
21 Using random forest models we tested the importance of gradient length, the choice of
22 data type (abundance vs. presence/absence), the transformation of between-species
23 similarities (linear vs. exponential), and the dissimilarity index in the predicting
24 correlation value.
- 25 3. We found that many indices behave very similarly and reach high correlation with
26 environmental distances. There were only a few indices (e.g. Rao's D_Q , and
27 representatives of the nearest neighbour approach) which performed regularly poorer
28 than the others. By far the strongest determinant of correlation with environmental
29 distance was the gradient length, followed by the data type. The dissimilarity index
30 and the transformation method seemed not crucial decisions when correlation with an
31 underlying gradient is to be maximized.
- 32 4. *Synthesis*: We provide a framework of functional dissimilarity indices and discuss the
33 approaches they follow. Although, these indices are formulated in different ways and
34 follow different approaches, most of them perform similarly well. At the same time,

35 sample properties (e.g. gradient length) determine the correlation between trait-based
36 dissimilarity and environmental distance more fundamentally.

37

38 **Keywords**

39 beta diversity, dissimilarity index, distance metric, community ecology, functional traits

40

41 **Abbreviations**

42 CDF = cumulative distribution function, CWM = community-weighted mean, FDissim =

43 functional dissimilarity, VIS = variable importance score

44

45 **Introduction**

46 Understanding and explaining the variation of living communities along dimensions of space

47 and time have been in the focus of ecological research ever since. The widely applied scheme

48 by Whittaker (1960, 1972) to tackle questions of different aspects of community variation

49 divides community diversity into alpha (within-community), beta (between-community) and

50 gamma (across-community) components. It is no exaggeration to say that among these three,

51 beta diversity sparked the most controversy due to the multitude of ways how it can be

52 formulated (Tuomisto 2010a,b, Anderson et al. 2011, Podani & Schmera 2011, Baselga &

53 Leprieur 2015). One of the most popular approaches to beta diversity builds upon

54 quantification of variation between pairs of communities using dissimilarity indices

55 (Anderson et al. 2006, Legendre & De Cáceres 2013, Ricotta 2017). A broad spectrum of

56 such dissimilarity indices are available for many specific purposes providing elementary tools

57 for different fields of ecology and beyond (see reviews by Legendre & Legendre 1998, Podani

58 2000). Nevertheless, choosing from such many options requires a more or less subjective
59 decision from the researcher which may affect the final result of the analysis. Comparative
60 reviews of dissimilarity indices (Faith et al. 1987, Koleff et al. 2003) and evaluations of
61 effects of methodological decisions (Lengyel & Podani 2015) are inevitably helpful in making
62 these decisions.

63 The most popular, yet not exclusive, interpretations of diversity for long time considered
64 species as variables which are unrelated with each other. In the last two decades, however, the
65 functional approach to ecological questions gained unprecedented attention (Díaz & Cabido
66 2001, McGill et al. 2006). This approach relies on the fact that species are not all maximally
67 different from each other, rather they can be considered related with respect to similarities in
68 their traits thought to represent their roles in ecosystems (Violle et al. 2007). The need for
69 explicitly accounting for between-species relatedness generated a wave of methodological
70 improvements that introduced new methods in the calculation of diversity. Next to a lively
71 scientific discussion on how functional alpha diversity can be appropriately quantified (Mason
72 et al. 2005, Petchey & Gaston 2006, Villéger et al. 2008, Mouchet et al. 2010), suggestions
73 were made also for the expression of functional beta diversity (Swenson 2011, Botta-Dukát
74 2018, Chao et al. 2019). Among them, a large variety of indices for calculating dissimilarity
75 between pairs of communities on the basis of the traits of their species have been proposed
76 (e.g. Ricotta & Burrascano 2008, Cardoso et al. 2014, Ricotta & Pavoine 2015). Although
77 these indices have been introduced as straightforward measures for revealing between-
78 community dissimilarity on the basis of traits, they have very different concepts behind, and
79 we still lack a comparative review of them.

80 In this paper we aim to provide an overview and a conceptual framework for the pairwise
81 functional dissimilarity (hereafter called FDissim) measures available in the literature to our
82 best knowledge. We start with a (1) short overview of the concept and indices of ecological

83 (dis-)similarity without accounting for relatedness of species, then (2) we review and classify
84 FDissim indices according to their conceptual basis, and (3) we test the performance of
85 FDissim indices.

86

87 **Short overview of taxon-based (dis-)similarity methods**

88 Most FDissim measures are generalizations of simple indices which were originally designed
89 for expressing dissimilarity based on species composition (that is, omitting similarities
90 between species). We start the review of trait-based (dis-)similarity measures with a brief
91 summary of these species-based indices. Then, we present a framework of approaches
92 including several families of trait-based dissimilarity indices.

93 *Species-based indices*

94 Most indices can be written in either similarity (s) or dissimilarity ($d=1-s$) form but when we
95 do not see necessary to specify the form, we call them ‘resemblances’. In the case of
96 presence/absence data, these indices are based on the well-known 2×2 contingency table
97 whose cells represent the number of species shared (denoted by a), as well as the number of
98 species occurring only in one of the communities (b and c). The fourth cell of the contingency
99 table quantifying the number of shared absences is disregarded by these indices and rarely
100 used in ecological analyses (but see Tamás et al. 2001). All these indices agree that they
101 express similarity as the proportion of shared diversity to total diversity. Hence, all of them
102 range between 0 and 1. In the case of presence/absence data the number of shared species, a ,
103 in the numerator stands for shared diversity for all indices, while the denominators are
104 different. In the Sørensen index (s_S) the denominator is the arithmetic mean of the species
105 numbers of the two communities, in Ochiai index (s_O) it is their geometric mean, in
106 Kulczynski (s_K) it is their harmonic mean, while in Simpson index (s_{Si}) it is the richness of the

107 species poorer community. If the two communities are equally species-rich, then these indices
108 are equal, otherwise $s_S < s_O < s_K < s_{Si}$. In the Jaccard index (s_J), the denominator is the total
109 number of species in the two communities, while in Sokal & Sneath index (s_{SS}) species
110 occurring in a single community are taken into account with double weight. There is a direct
111 and monotonic relationship between Jaccard, Sørensen, and Sokal & Sneath indices (see
112 Appendix S1). Table 1 summarizes the similarity and dissimilarity forms of the above indices.
113 For abundance data, the resemblance of two communities is derived from the summation of
114 species-wise differences, with the simplest interpretation being the Euclidean and the
115 Manhattan distances, respectively:

116 Eq. 1.
$$d_{Euclidean} = \sqrt{\sum_{i=1}^{S_{jk}} (x_{ij} - x_{ik})^2}$$

117 Eq. 2.
$$d_{Manhattan} = \sum_{i=1}^{S_{jk}} |x_{ij} - x_{ik}|$$

118 where x_{ij} and x_{ik} are the abundance of species i in communities j and k , S_{jk} is the total number
119 of species in j and k . For both indices, the minimum is 0 but the maximum of Euclidean
120 distance is the square-root of the sum of squared abundances, while for Manhattan distance
121 the maximum is the sum of abundances. Obviously, their dependence on total abundance
122 makes these index values difficult to compare across samples; therefore, indices including a
123 standardization have become more popular in ecological studies. The standardization is
124 possible in several ways. The first option is to standardize raw species contributions to
125 between-community dissimilarity ($x_{ij}-x_{ik}$), and then to sum them. Therefore, each species-level
126 difference in abundance should be divided by a scaling factor in a way that maximal species-
127 level difference is 1 and this difference is maximal if species present only one of the
128 compared communities. Summing x_{ij} and x_{ik} in the denominator satisfies this requirement and
129 gives a well-known distance measure, the Canberra index:

130 Eq. 3.
$$d_{Canberra} = \frac{\sum_{i=1}^{S_{jk}} |x_{ij} - x_{ik}|}{\sum_{i=1}^{S_{jk}} (x_{ij} + x_{ik})}$$

131 However, Canberra index still ranges between 0 and S_{jk} . According to Ricotta & Podani
132 (2017), the normalized Canberra index can be derived by unweighted averaging of species
133 contributions:

134 Eq. 4.
$$d_{NCanberra} = \frac{1}{S_{jk}} \sum_{i=1}^{S_{jk}} \frac{|x_{ij} - x_{ik}|}{(x_{ij} + x_{ik})}$$

135 Alternatively, species-level differences can be divided by $\max(x_{ij}, x_{ik})$. It also results unity, if
136 species occur only either of the plots. Ricotta & Podani (2017) called this modified Canberra
137 index, whose normalized version follows:

138 Eq. 5.
$$d_{NMCanberra} = \frac{1}{S_{jk}} \sum_{i=1}^{S_{jk}} \frac{|x_{ij} - x_{ik}|}{\max(x_{ij}, x_{ik})}$$

139 Calculating from binary data, both normalized Canberra and normalized modified Canberra
140 result in Jaccard dissimilarity.

141 A different way of standardization is possible if raw species-level differences are summed and
142 divided by the sum of their theoretical maxima. In this case, the denominator can follow the
143 logic of Canberra index, thus leading to the Bray-Curtis index:

144 Eq. 6.
$$d_{BC} = \frac{\sum_{i=1}^{S_{jk}} |x_{ij} - x_{ik}|}{\sum_{i=1}^{S_{jk}} (x_{ij} + x_{ik})}$$

145 Analogously with the normalized modified Canberra index, instead of the sum, the
146 denominator may contain the maximum of abundance, resulting in the formula known as
147 Marczewski-Steinhaus index:

148 Eq. 7.
$$d_{MS} = \frac{\sum_{i=1}^{S_{jk}} |x_{ij} - x_{ik}|}{\sum_{i=1}^{S_{jk}} \max(x_{ij}, x_{ik})}$$

149 Worth to note that Bray-Curtis and Marczewski-Steinhaus indices calculated on
150 presence/absence data return the values of Sørensen index and Jaccard index in dissimilarity
151 form, respectively. Moreover, several abundance-based indices can be expressed if we
152 generalize a , b , and c quantities used during the definition of indices for presence/absence
153 data (Tamás et al. 2001).

154 Eq. 8.
$$a' = \sum_{i=1}^{S_{jk}} \min(x_{ij}, x_{ik})$$

155 Eq. 9.
$$b' = \sum_{i=1}^{S_{jk}} (\max(x_{ij}, x_{ik}) - x_{ij})$$

156 Eq. 10.
$$c' = \sum_{i=1}^{S_{jk}} (\max(x_{ij}, x_{ik}) - x_{ik})$$

157 Substituting a , b and c with a' , b' and c' into the formula of Sørensen index gives Bray-
158 Curtis, and doing so with Jaccard index results in the Marczewski-Steinhaus. Abundance
159 versions of all other presence/absence indices can be created in the same manner.

160

161 *A classification of FDissim indices*

162 FDissim indices incorporate trait information into the calculation of dissimilarity in different
163 ways. The simplest solution is when summary statistics or distributions are calculated for the
164 two communities and a measure of distance or segregation is calculated between them. We
165 call this the *summary-based class*, and in our review, we include two approaches within this,
166 the *typical value approach* and the *distribution-based approach*. In the second class we
167 include indices which utilize a symmetrical species by species (dis-)similarity matrix and link
168 it directly through matrix operations with the compositional matrix. We call this the
169 *dissimilarity-based class* which includes the *probabilistic*, the *ordinariness-based*, the
170 *diversity partitioning*, and the *nearest neighbour approaches*. The third class includes
171 methods which make use of between-species (dis-)similarities for classification of species;

172 therefore, we call it the *classification-based class*. The classification either transforms the
173 original structure of the dissimilarity matrix into discrete groups of species which can be used
174 as functional types, or expresses dissimilarities in a form of a tree-graph where between-
175 species dissimilarities are organized in an inclusive hierarchy. This is a widespread approach
176 for accounting for phylogenetic relatedness, since phylogenies are commonly summarized in
177 the form of cladograms. Such methods heavily rely on the algorithm chosen for the
178 classification, including the decisions about the number of clusters and the method for
179 breaking tied values. Examples are provided by Hérault & Honnay (2007), Nipperess et al.
180 (2010), and Cardoso et al. (2014), while a review is available by Pavoine (2016). As there is
181 no general recommendation for the classification method, we omit this class from the
182 framework detailed below and the comparative test. The classification of trait-based
183 dissimilarity indices and their main properties are summarized on Table 2.

184 *Typical value approach*

185 Indices following this approach represent each community with a typical trait value, and
186 calculate a distance metric between them. The most commonly applied typical trait value is
187 the community weighted mean (CWM; Garnier et al. 2004). The rationale behind the CWM
188 can be linked with the mass ratio hypothesis (Grime 1998) stating that the effect of species on
189 ecosystem functioning is proportional to their relative abundances. Although, several issues
190 emerged regarding its limited applicability in statistical inference (Hawkins et al. 2017, Peres-
191 Neto et al. 2017, Zeleny 2018) and its negligence of within-community variation (Muscarella
192 & Uriarte 2016), difference in CWM is still considered a reliable indicator of robust changes
193 in trait composition induced by selective forces like environmental matching or succession
194 (De Bello et al. 2007, 2013, Kleyer et al. 2012). Ricotta et al. (2015) investigated the
195 relatedness of the distance between CWMs with the probabilistic approach (see therein) and
196 showed its applicability on phylogenetic data. Due to its tolerable requirements for

197 computational capacity, Lengyel et al. (2020) used the Euclidean distance between trait
198 CWMs of phytosociological relevés for the trait-based numerical classification of grasslands
199 of Poland with a sample size of 6985 sites and 885 species. Another advantage of this method
200 is its Euclidean property. Besides the community-weighted mean, other typical values, e.g. the
201 median or the mode, might be considered depending on the scaling of the trait variable and on
202 specific research aims.

203

204 *Distribution-based approach*

205 Instead of typical values, the distribution of trait values is considered a more reliable
206 representative of the trait composition and variability of a community. Continuous
207 distributions can be defined by a density function, while discrete distributions by the
208 probabilities of the possible values, while both types can be characterized by a cumulative
209 distribution function (CDF). A useful analogue of the distance between typical values might
210 be distance between discrete distributions, density functions or CDFs.

211 If data is available on intraspecific trait variation, trait values forms a continuous distribution.
212 First, separate density functions have to be fitted within each species. Then, density function
213 of this community-level distribution can be calculated as weighted sum of species level
214 density functions (Carmona, de Bello, Mason, & Lepš, 2016). If such data is not available, we
215 can use relative abundances as estimates of probabilities of the corresponding trait values.
216 Pairs of trait values and their probability form a discrete distribution.

217 Similarity of density functions can be measured by their overlap (see Appendix S2 for
218 overview of overlap measures). Overlap functions between within-species trait distributions
219 has already been proved useful in the quantification of between-species niche segregation
220 (MacArthur & Levins 1967, Mouillot et al. 2005) or trait-based dissimilarity of species (Lepš

221 et al. 2006, De Bello et al. 2013). Nevertheless, they are perfectly applicable to the
222 community level as well.

223 Gregorius et al. (2003) proposed an index called *delta* for the quantification differences
224 between discrete trait distributions. Delta is the minimal sum of frequencies shifted from one
225 trait state to another trait state, weighted by the differences between the respective states.
226 Minimizing the sum of shifted frequencies is known in linear programming as the
227 transportation problem (Hitchcock 1941). Due to its relatively high computational demand, it
228 is unfeasible for large compositional and trait data matrices typically used in ecological
229 research, therefore, we exclude this index from our comparison.

230 Difference between two CDFs can be calculated at each possible trait values (i.e. not only the
231 observed ones), then the sum of them can be used as a trait-based dissimilarity measure. In
232 Appendix S3 we introduce the distance between CDFs in more detail.

233

234 *Maximally distinct communities*

235 Species-based dissimilarities, except Euclidean, Manhattan and (non-normalized) Canberra
236 distances, equal unity, which is their maximum, when the two compared communities do not
237 share any species. In this context, we could call such communities maximally distinct.

238 However, when traits are considered, two communities can be similar, even if they do not
239 share any species. For example, if all species of community *A* is replaced by a similar species
240 in community *B*, the two communities have no shared species, but from functional point of
241 view, they are similar. In this context, two communities are maximally distinct, when
242 similarity of any species from the first community is zero to any species in the other
243 community. It is a desirable property for a functional similarity index to take the value 0 if
244 and only if the two compared communities are maximally distinct.

245

246 *Probabilistic approach*

247 This approach can be traced back to the diversity framework proposed by Rao (1982), and
248 recently extended by Pavoine & Ricotta (2014). Rao's within community diversity is defined
249 as the expected dissimilarity between two randomly drawn individuals from a single
250 community:

251 Eq. 11.
$$Q(\mathbf{p}) = \sum_i \sum_j p_i p_j \delta_{ij}$$

252 where p_i is the relative abundance of the i th species in the community and δ_{ij} is the
253 dissimilarity between species i and j . This has become a widely used index of functional alpha
254 diversity (Botta-Dukát 2005). Likewise, a between-community component of diversity,
255 $Q(\mathbf{p}, \mathbf{q})$, can be defined as the dissimilarity between two random individuals, each selected
256 from different communities:

257 Eq. 12.
$$Q(\mathbf{p}, \mathbf{q}) = \sum_i \sum_j p_i q_j \delta_{ij}$$

258 Between community diversity can be expressed using within community diversity of the two
259 original communities ($Q(\mathbf{p})$ and $Q(\mathbf{q})$) and the community with mean relative abundances;
260 $Q\left(\frac{\mathbf{p}+\mathbf{q}}{2}\right)$.

261 Eq. 13.
$$2Q\left(\frac{\mathbf{p}+\mathbf{q}}{2}\right) = 2 \sum_i \sum_j \frac{p_i+q_i}{2} \frac{p_j+q_j}{2} \delta_{ij} = \frac{1}{2} \sum_i \sum_j [p_i p_j + q_i q_j +$$

262 $2p_i q_j] \delta_{ij} = \frac{Q(\mathbf{p})+Q(\mathbf{q})}{2} + Q(\mathbf{p}, \mathbf{q})$

263 Subtracting mean within community diversity from the between community diversity leads to
264 Rao's dissimilarity (also called *DISC*):

265 Eq. 14.
$$D_Q = \sum_i \sum_j p_i q_j \delta_{ij} - \frac{\sum_i \sum_j p_i p_j \delta_{ij} + \sum_i \sum_j q_i q_j \delta_{ij}}{2} = \sum_i \sum_j p_i q_j \delta_{ij} - \frac{Q(\mathbf{p}) + Q(\mathbf{q})}{2} =$$

266 $2Q\left(\frac{\mathbf{p}+\mathbf{q}}{2}\right) - Q(\mathbf{p}) - Q(\mathbf{q})$

267 where p_i and q_i are the relative abundances of species i in the two communities. Champely
268 and Chessel (2002) proved that if δ has squared Euclidean property, Rao quadratic entropy is
269 concave function, i.e. $Q\left(\frac{\mathbf{p}+\mathbf{q}}{2}\right)$ is higher than or equal to mean of $Q(\mathbf{p})$ and $Q(\mathbf{q})$. Thus under
270 this condition, $D_Q \geq 0$. If $0 \leq \delta_{ij} \leq 1$, $\sum_i \sum_j p_i q_j \delta_{ij}$, which is the weighted average of
271 between-species distances, also has to be within this range. Therefore, $0 \leq D_Q \leq 1$. However,
272 D_Q may be much less than 1, even if the two communities are completely distinct, when $Q(\mathbf{p})$
273 and $Q(\mathbf{q})$ are high. Therefore, Pavoine & Ricotta (2014) suggested dividing D_Q by its
274 theoretical maximum (see equations 3 and 4 in Pavoine & Ricotta 2014). They recognized
275 that the resulting indices are representatives of a broader family of indices, hereafter called
276 *dsimcom*, which are actually the implementations of Rao's between-community and within-
277 community components of diversity into the similarity formulae designed for
278 presence/absence data. For this index, it is necessary to introduce the similarity between
279 species, $\varepsilon_{ij}=1-\delta_{ij}$. The expected similarity between individuals of different communities,
280 $A = \sum_i \sum_j p_i q_j \varepsilon_{ij}$ is taken analogous with the shared diversity, a , according to the parameters
281 of the similarity indices for presence/absence data disregarding species properties, while the
282 expected similarities within communities ($A + B = \sum_i \sum_j p_i p_j \varepsilon_{ij}$ and $A + C = \sum_i \sum_j q_i q_j \varepsilon_{ij}$) are
283 analogous with the species numbers ($a+b$, $a+c$). In this way, Pavoine & Ricotta (2014)
284 presented formulae following the Sokal & Sneath, Jaccard, Sørensen, and Ochiai indices.
285 Additionally, a formula analogous with Whittaker's effective species turnover ($\beta=\gamma/\alpha-1$;
286 Whittaker 1972, Tuomisto 2010a) is suggested for two communities, which in similarity form
287 is shown to be identical with the overlap index of Chiu et al. (2014). In this formulation
288 $\gamma=A+B+C$ and $\alpha=(2A+B+ C)/2$. Pavoine & Ricotta (2014) showed that members of the

289 *dsimcom* family provide meaningful values also if absolute abundances, percentage values or
290 binary occurrences are used instead of relative abundances.

291 When ε_{ij} contains taxonomical similarities, its off-diagonal elements are 0, and $A=a$, $B=b$, and
292 $C=c$.

293 Worth to note the inherent link between D_Q and $CWMdis$ on the basis of the geometric
294 interpretation by Pavoine (2012) and Ricotta et al. (2015). Pavoine (2012) showed that if
295 between-species dissimilarities are in the form $\delta_{ij}=(d_{ij}^2)/2$ and d_{ij} is Euclidean embeddable, D_Q
296 is half the squared Euclidean distance between the centroids of two communities – a function
297 monotonically related with $CWMdis$, the simple Euclidean distance between centroids of
298 communities. As Ricotta et al. (2015) argue, if species relatedness is only described by a
299 dissimilarity matrix, which is the common case in phylogenetic analyses, species can be
300 mapped into a principal coordinate analysis ordination using d_{ij} . Given the Euclidean
301 embeddable property of d_{ij} , this ordination should produce $S-1$ or fewer ordination axes, all
302 with positive eigenvalues. Ordination scores for species can be used as traits, and therefore,
303 centroids of communities, and (squared) Euclidean distances between communities can be
304 calculated. In the special case when between-species dissimilarities are Euclidean distances,
305 D_Q must be equal with the Euclidean distance between the weighted averages of traits, that is,
306 $CWMdis$.

307 It is also notable that Swenson et al. (2011) and Swenson (2011) use the quantity $Q(\mathbf{p}, \mathbf{q})$ as a
308 standalone index of pairwise beta diversity and call it D_{pw} or “Rao’s D ”. The latter name is
309 misleading since Rao (1982) himself noted with D_{ij} the *DISC* (or D_Q) index. $Q(\mathbf{p}, \mathbf{q})$ measures
310 dissimilarity between two communities but the dissimilarity of a community from itself is not
311 zero. Swenson (2011) also presents a standardized version of $Q(\mathbf{p}, \mathbf{q})$ under the name Rao’s
312 H. With this formula the dissimilarity of a community to itself is scaled to 1, however, its

313 transformation to a meaningful scale where each community has dissimilarity value zero
314 towards itself is not elaborated. Due to this drawback, we do not consider these indices in our
315 review of functional dissimilarity measures.

316 Schmidt et al. (2017) proposed probabilistic indices with weighted and unweighted versions
317 for expressing community similarity on the basis of taxa interaction networks (called *TINA*,
318 taxa interaction-adjusted) and phylogenetic relatedness (*PINA*, phylogenetic interaction-
319 adjusted). *TINA* and *PINA* differ only in what type of data the interaction matrix contains.
320 Notably, the functional formula of weighted *TINA* is identical with the Ochiai version of
321 *dsimcom*. However, the unweighted *TINA*, abbreviated *TU*, is not a special case of *TINA*,
322 which we consider an inconsistency. Therefore, we did not include *TU* as a separate index.

323

324 *Ordinariness-based approach*

325 With respect to functional alpha diversity, Leinster & Cobbold (2012) introduced the concept
326 of species ordinariness defined as the weighted sum of relative abundances of species similar
327 to a focal species within the same community, or in other words, the expected similarity of an
328 individual of the focal species and an individual chosen randomly from the same community.

329 According to Ricotta & Pavoine (2015) it is straightforward to replace abundances with
330 ordinariness values in the species-based (dis-)similarity indices. Following this concept,
331 Ricotta & Pavoine (2015) introduced a new family of trait-based similarity measures called
332 *dissABC*. *dissABC* applies the schemes of Jaccard, Sørensen, Ochiai, Kulczynski, Sokal &
333 Sneath, and Simpson indices. Either relative or absolute abundances can be chosen as input
334 values. Species ordinariness values can be calculated either with respect to the pooled species
335 list of the two communities under comparison, or to the total species list of the data matrix.

336 For species-based analyses, Ricotta & Podani (2017) suggested a general formula of distance
337 measures in which community dissimilarity is calculated by the weighted averaging of
338 species-level differences in abundance. From this formula, a normalized Canberra distance,
339 Bray-Curtis distance, Marczewski-Steinhaus index, and an evenness-based dissimilarity index
340 (Ricotta 2018) can be derived. According to Pavoine & Ricotta (2019), replacing species
341 abundances with species ordinariness values, a meaningful dissimilarity index can be
342 designed, which is called *generalized_TradiDiss*. Additionally, this index contains a factor
343 which weights the contribution of each species to the overall dissimilarity between the two
344 communities. This weight can be set to give even weight to all species or to weigh them
345 proportionally to their relative abundance in the pooled communities.

346

347 *Diversity partitioning approach*

348 Following the work of Hill (1973), a community with *diversity of order q , qD* , is as diverse as
349 a theoretical community containing qD equally abundant species. The order of diversity, q ,
350 expresses the weight given to differences in species abundance, $q = 0$ representing the
351 presence/absence case, $q = \infty$ considering only the relative abundance of the most abundant
352 species in the community. Without accounting for interspecific similarities, there is emerging
353 consensus that using effective numbers (also called number of equivalents) is a
354 straightforward way for partitioning diversity into within-community (alpha), between-
355 community (beta) and across-community (gamma) components (Jost 2007). Of these three,
356 the between-community component, beta diversity, can be interpreted as a form of
357 dissimilarity when applied for two communities (Ricotta 2017). Beta diversity can be derived
358 from alpha and gamma diversity in a multiplicative (beta = gamma/alpha) or an additive way
359 (beta = gamma – alpha). Jost (2007) and Chao et al. (2012) argued that multiplicative beta
360 diversity is a useful way for quantifying community differentiation; however, due to its

361 scaling between 1 and N (N being the number of communities) it is not comparable across
362 samples containing different numbers of communities. To remove this dependence, they offer
363 three solutions with which the value of multiplicative beta can be normed. Although, for
364 pairwise comparisons, N is always 2, it seems straightforward to follow these
365 recommendations, since the scaling between 0 and 1 has several advantages, and most other
366 indices also share this property. The rescaling formulae of Chao et al. (2012) embody
367 different concepts of community (dis-)similarity, which together we call the family of
368 *multiplicative beta indices*. The first formula is the relative turnover rate per community,
369 which is a linear transformation of beta to the normed scale.

370 Eq. 15.
$$\beta_{turnover}\langle q \rangle = ({}^q\beta - 1)/(N - 1)$$

371 Here 0 means identical species composition, while 1 indicates totally distinct communities. In
372 the pairwise comparison ($N = 2$), $\beta_{turnover}\langle q \rangle = {}^q\beta - 1$.

373 The second index measures homogeneity, and is a linear transformation of the inverse of beta.
374 With respect to the fact that the complement term of homogeneity is heterogeneity, we call its
375 dissimilarity form $\beta_{heterogeneity}$:

376 Eq. 16.
$$\beta_{heterogeneity}\langle q \rangle = 1 - \left(\frac{1}{{}^q\beta} - \frac{1}{N} \right) / \left(1 - \frac{1}{N} \right)$$

377 When $N = 2$, $\beta_{het}\langle q \rangle = 2 - 2/{}^q\beta$. With $q = 0$ (presence/absence case) the index is identical with
378 Jaccard index, while with $q = \infty$ (abundance case) it is the Morisita & Horn index.

379 The third index measures overlap between communities, whose counterpart is segregation,
380 thus we call it β_{segr} :

381 Eq. 17.
$$\beta_{segregation}\langle q \rangle = 1 - \left[\left(\frac{1}{{}^q\beta} \right)^{q-1} - \left(\frac{1}{N} \right)^{q-1} \right] / \left[1 - \left(\frac{1}{N} \right)^{q-1} \right]$$

382 With $q = 0$, $\beta_{segregation}\langle q \rangle = \beta_{turnover}\langle q \rangle$, and both gives the Sørensen index.

383 According to Leinster & Cobbold (2012), it is possible to implement species similarities in the
384 calculation of effective numbers. This way, the meaning of ${}^qD^Z$, is the diversity of a
385 theoretical community with ${}^qD^Z$ *equally abundant* and *maximally different* species. Hence,
386 both unevenness in the abundance structure and the between-species similarities decrease the
387 value of effective species number. Due to measuring diversity in effective numbers, it is
388 possible to partition diversity into alpha, beta, and gamma fractions (Leinster & Cobbold
389 2012; Botta-Dukát 2018) in the multiplicative way. Then, this multiplicative beta can be
390 rescaled using the formulae proposed by Chao et al. (2012). These indices behave consistently
391 only if abundances are taken into account as relative abundances.

392

393 *Nearest neighbour approach*

394 The earliest representatives of this family were shown by Clarke & Warwick (1998) and Izsák
395 & Prince (2001), then Ricotta & Burrascano (2008), and Ricotta & Bacaro (2010; see D_{CW}
396 and D_{IP} indices). Later Ricotta et al. (2016) introduced a new, general family called *PADDis*.
397 All these indices were primarily defined for presence-absence data type. The approach is
398 based on a re-definition of the b and c quantities of the 2×2 contingency table. Looking at
399 species as maximally different, and taking X and Y the two communities under comparison, b
400 can be viewed as the total uniqueness of community X . The uniqueness of a single species in
401 X is 1 if it is absent in Y , otherwise it is 0. Therefore, b is the sum of species uniqueness
402 values. However, from a functional perspective, the uniqueness of a species present only in X
403 should be between 0 and 1 if it is absent in Y but a similar species present there. Therefore, it
404 is possible to define the analogue of b which accounts for similarities between species:

405 Eq. 18.
$$B = \sum_{i \in X} (1 - \max_{j \in Y} \varepsilon_{ij}) = S_x - \sum_{i \in X} \max_{j \in Y} \varepsilon_{ij}$$

406 The same logic applies for c , which is the uniqueness of community Y , where C expresses the
407 degree of uniqueness:

408 Eq. 19.
$$C = \sum_{i \in Y} (1 - \max_{j \in X} \varepsilon_{ij}) = S_Y - \sum_{i \in Y} \max_{j \in X} \varepsilon_{ij}$$

409 Ricotta et al. (2016) define the A quantify as follows:

410 Eq. 20.
$$A = a + (b - B) + (c - C)$$

411 Having A , B , and C defined as analogues of a , b , and c , it is now possible to design trait-based
412 similarity measures following the logics of Jaccard, Sørensen, Sokal & Sneath, Kulczynski,
413 Ochiai and Simpson indices. It is notable that Ricotta et al. (2016) define A as a quantity that
414 ensures the components B and C to add up to $a + b + c$ but with no explicit biological
415 interpretation. Notably, D_{IP} and D_{CW} are identical with the Sørensen and Kulczynski forms of
416 *PADDis*. The generalization of D_{IP} and D_{CW} to relative abundances, $D_{CW}(Q)$, was also derived
417 by Ricotta & Bacaro (2010). For these two versions, it is not necessary to explicitly define the
418 A component. Using the relationships between Jaccard, Sørensen, Kulczynski, Ochiai and
419 Sokal & Sneath indices, from $D_{CW}(Q)$ it is theoretically possible to derive the extension of
420 *PADDis* to relative abundances; however, the biological interpretation of A remains dubious
421 in this framework.

422

423 **Methods**

424 The performance of FDissim indices can be reliably tested on data sets with known
425 background processes driving community assembly which is hardly possible to satisfy with
426 real data. Therefore, we compared the performance of FDissim indices using simulated data
427 sets. The data sets were generated using the *comm.simul* function of the *comsimitv* R package
428 (Botta-Dukát & Czúcz 2016, Botta-Dukát 2020). This function follows an individual-based

429 model for a meta-community comprising N communities and a regional pool of S species.
430 Local communities include J individuals, and are distributed equidistantly along a continuous
431 environmental gradient (with gradient values between 0 and 1). Each individual possesses
432 three traits: an ‘environmental’, a ‘competitive’ trait, and a neutral trait, all ranging on [0; 1].
433 Intraspecific variation in trait values is neglected in the simulation, that is, individuals
434 belonging to the same species are identical. The environmental trait defines the optimum of
435 the species along the environmental gradient. The closer the position of a community along
436 the environmental gradient to the environmental trait value of a species, the more suitable it is
437 for that species:

438 Eq. 21.
$$\textit{suitability} = \frac{(\textit{environment} - \textit{environmental trait})^2}{\sigma}$$

439 where σ (sigma) is adjustable so as to change the niche width of the species, and hence, the
440 length of the gradient (see later). The competitive trait represents the resource acquisition
441 strategy of the individual. The more similar the latter value between two individuals, the
442 higher the competition is between them, which means that intraspecific competition is the
443 strongest. The neutral trait has no effect on community assembly, thus it is not considered in
444 our study. The simulation starts with the random assignment of all individuals of all
445 communities to species. The second step is a ‘disturbance’ event, when one individual ‘dies’
446 in each community. This individual is to be replaced by an offspring of other individuals
447 within the same community or those of other communities. Each individual produces one
448 offspring or does not reproduce. Probability of reproduction depends on the strength of
449 competition. The offspring remains in the same community or randomly disperses into any of
450 the other communities. Finally, the dead individual is replaced by one new individual from
451 the seeds produced and dispersed. The probability that an individual of a certain species
452 replaces the dead individual is defined by the number of seeds of that species and the

453 suitability of the habitat. Steps between the disturbance event and the establishment of a new
454 individual constitute a single 'generation'. Community composition is evaluated after lot of
455 generations. The strength of the environmental filtering can be adjusted by the sigma
456 parameter, respectively. When sigma is 0, all species are maximally specialist, which means
457 that they can occur only at the optimum point of the gradient (that is, at the exact value for the
458 environmental trait). If sigma is infinity, species are maximally generalist and all points along
459 the environmental gradient are equally suitable for them. Therefore, sigma is the parameter
460 which defines the suitability of each point of the gradient for each species based on its
461 distance from the respective optima. We generated data sets with sigma values 0.01, 0.1, 0.25,
462 0.5, 1 and 5 in order to simulate situations with different strength of environmental filtering.
463 The number of communities was 30, each community comprised 200 individuals, the number
464 of species in the species pool was 300, the simulation iterated for 100 generations, and we
465 allowed no intraspecific trait variation. For all the other parameters, we used the default
466 options.

467 However, it needed further explanation what real situations the six simulated levels of
468 environmental filtering represent. To provide a reference and assist interpretation, we
469 calculated two species-based beta-diversity measures, the multiplicative beta (Whittaker
470 1960) and the gradient length of the first axis of a detrended correspondence analysis (DCA)
471 ordination (Hill & Gauch 1980; Appendix S5, Fig. S5.1). The former gives the number of
472 distinct communities present in the total species pool of the gradient, while the latter is
473 minimal number of average niche breadths (also called turnover units) necessary for covering
474 the total gradient length. Moreover, we plotted the abundance of species in the sample units
475 along the gradient as a visual tool for assessing gradient length (Appendix S5, Fig. S5.2). All
476 these methods indicated that with sigma = 0.01 the gradient is extremely long: there are more
477 than 10 distinct communities and near 20 turnover units along the gradient. Samples with such

478 high beta diversity are very rare and special in real ecological research; therefore, findings
479 from simulations with $\sigma = 0.01$ are mostly of theoretical importance. Beta diversity
480 values from $\sigma = 0.1$ to $\sigma = 1$ are more similar to real study situations, hence they
481 should be more relevant for practice. At $\sigma = 5$, environmental filtering is practically not
482 operating, between-community variation is driven by interspecific relations and chance.

483 We calculated between-species dissimilarities as the Gower distance between their
484 environmental trait values which in this case equals the Euclidean distance scaled to [0; 1].
485 These distances had to be transformed to similarities according to the requirements of the
486 FDissim indices. Several formulae are available with which it is possible; however, they may
487 assume different functional relationships between similarity and distance. One of such
488 formulae we used is the linear transformation according to *Similarity = 1 - Distance*. Besides
489 this, we also used *Similarity = $e^{-u \times Distance}$* which supposes a curvilinear function between
490 similarity and distance (Leinster & Cobbold 2012). With this exponential formula, it is
491 possible to weight the importance of small Gower distances between species relative to large
492 distances. With changing the parameter u it is possible to adjust how steeply similarity
493 decreases with increasing distance. We set $u = 10$ which leads to a relatively steep decline.
494 Although, after this transformation the minimal value for similarity is higher than zero, we
495 considered it negligibly low ($e^{-10} \approx 0.000045$) so we did not apply the transformation proposed
496 by Botta-Dukát (2018). For all FDissim indices where it was necessary we used the similarity
497 matrix or a dissimilarity matrix calculated as *Dissimilarity = 1 - Similarity* as input. The
498 dissimilarity matrix is identical with the Gower distance matrix if the similarities were
499 calculated in a linear way, but in the other case, it keeps the exponential relationship between
500 distance and (dis-)similarity.

501 Dissimilarity matrices were calculated for the four community data sets with different sigma
502 values, with the two functions transforming Gower distances, and across a broad range of

503 available FDissim indices. For indices where absolute or relative abundances could have been
504 taken into account, we opted for relative abundance for the sake of better comparability. With
505 *generalized_Traddiss*, we calculated the ‘even’ and the ‘uneven’ weighting versions. The
506 entire analysis was run with abundance and presence/absence data. Some FDissim indices are
507 only suitable for binary data, thus the number of indices applied for relative abundance and
508 binary data were 25 and 31, respectively. In cases of indices handling both data types, we
509 used exactly the same version of the index as with abundance data, hence communities with
510 different numbers of species were given equal weight due to division by community totals.
511 Additionally, dissimilarity matrices were also calculated using the Bray-Curtis index (for
512 binary data: Sørensen index in dissimilarity form) to provide a contrast against the case
513 disregarding between-species dissimilarities.

514 Then for each dissimilarity matrices, we conducted two types of analyses. Firstly, we
515 compared how strongly the dissimilarity indices correlate with the environmental distance
516 using Kendall tau rank correlation. This gives an estimate of how well a dissimilarity index
517 reveals the monotonic relationship between trait composition of local communities and the
518 environmental gradient. We visually assessed the shape of relationship between dissimilarity
519 and environmental distance in the case of lowest sigma (i.e., longest gradient) when the
520 distortion of linear relationship between the two is supposed to be the strongest. Then, to
521 disentangle the effects of different methodological decisions and the sigma parameter on the
522 correlation between FDissim indices and environmental distance we calculated a random
523 forest model. In this model the dependent variable was the Kendall tau correlation coefficient,
524 while the independent variables were the sigma, the data type (abundance vs.
525 presence/absence), the transformation method for Gower distances (linear vs. exponential),
526 and the FDissim method. Within approaches FDissim methods often strongly correlated that
527 resulted in very similar Kendall’s tau values. Therefore, only the Sørensen/Bray-Curtis

528 versions of *dsimcom*, *dissABC*, *PADDis/D_{CW}*, *generalized_Tradiidiss* with uneven weights, as
529 well as $\beta_{turnover}$, *CWMdis*, and the *CDFdis* were included into this analysis. Variable
530 importance scores (VIS) in the random forest were estimated by the permutation approach
531 based on mean decrease in log-likelihood using the *varimp* function of the *partykit* package.
532 The effects of the model terms were also illustrated by heat-maps.

533 All statistical analyses were done in R (R Core Team 2019) using the *FD* (Laliberté &
534 Legendre 2010, Laliberté et al. 2014), *adiv* (Pavoine 2020a,b), *comsimitv* (Botta-Dukát 2020),
535 *vegan* (Oksanen et al. 2019), *DescTools* (Signorell et al. 2020), *partykit* (Hothorn et al. 2006,
536 Strobl et al. 2007, Strobl et al. 2008, Hothorn & Zeileis 2015) packages.

537 **Results**

538 Kendall tau correlation coefficients decreased as the strength of environmental filtering
539 decreased (that is, with increasing sigma) in all examined cases. For *FDissim* indices which
540 handled both data types, presence/absence data resulted in lower correlations than abundance
541 data for all indices. For most indices, this difference was highest at intermediate values for
542 sigma. These trends were consistent between the linear and the exponential transformations.
543 Correlations for all indices at all sigma values with linear transformation are shown in Table 3
544 for abundances data and in Table 4 for presence/absence data.

545 In most simulation scenarios, the *FDissim* indices correlated more strongly with the
546 environmental gradient than the species-based Bray-Curtis index. However, in several
547 occasions, indices belonging to the nearest neighbour family performed poorer than the
548 species-based dissimilarity. Notably, at the highest sigma and with presence/absence data, all
549 indices showed correlation near to zero but among them the Bray-Curtis index had the highest
550 correlation with environmental distance.

551 As expected, we found perfect rank correlations among Jaccard, Sørensen, Sokal-Sneath and
552 Whittaker's beta versions of *dsimcom*, among Jaccard, Sørensen and Sokal-Sneath forms of
553 *dissABC*, between D_{IP} and Sørensen form of *PADDis* (only for presence-absence data),
554 between D_{CW} and Kulczynski form of *PADDis* (only for presence-absence data), and between
555 D_{IP} and D_{CW} (for abundance data type).

556 Dissimilarity indices showed various shapes of relationship with environmental distance
557 (Appendix S4). At strongest environmental filtering, all FDissim indices had dissimilarity
558 values near zero at minimal environmental distance, only the species-based Bray-Curtis which
559 had dissimilarity was near 0.4 at the smallest environmental distances. In case of linear
560 transformation of Gower distances and presence/absence data, approximately linear
561 relationship was found for *CWMdis*, *CDFdis*, D_Q , Sørensen and Ochiai forms of *dsimcom*,
562 Jaccard form of *dissABC*, Marczewski-Steinhaus form of *generalized_Tradiidiss* with both
563 weighting versions, $\beta_{heterogeneity}$ and $\beta_{segregation}$; although, most other indices showed only a
564 small degree of distortion of linear function (Figure S4.1). Exponential relationship was found
565 for the evenness-based (PE) form of *generalized_Tradiidiss*. Notably, the taxon-based Bray-
566 Curtis index had the steepest asymptotic function among all. In case of exponential
567 transformation all other indices relying on between-species dissimilarities showed an
568 asymptotic curve (Figure S4.2).

569 In the random forest, niche width (that is, sigma) acquired by far the highest variable
570 importance score (VIS=0.114). The less important variables were the data type (VIS=0.0176),
571 the dissimilarity method (VIS=0.0037) and the transformation (VIS=-0.00001). The heat map
572 (Figure 1) also revealed a strong decrease in correlation along increasing sigma. It is also
573 clearly shown that in most cases abundance data resulted in significantly higher correlation
574 than presence/absence. The difference between linear and exponential transformation methods
575 was not always visible. Regarding variation between dissimilarity indices, the most striking

576 patterns were the relatively poor performance of the *PADDis/D_{CW}* indices. All but the latter
577 index combined with abundance data and linear transformation of dissimilarities lead to the
578 highest correlation with environmental distance.

579

580 **Discussion**

581 *General patterns in the correlation with environmental distance*

582 We ran different simulation scenarios with varying strength of environmental filtering. We
583 expected that the correlation between FDissim indices and environmental distance to be the
584 highest when the environmental filtering is the strongest, and the correlation to become
585 neutral when environmental filtering is not effective. When environmental filtering was
586 strongest (that is, minimal overlap of species niches along the environmental gradient), all
587 FDissim indices correlated highly with the environmental gradient. As expected, correlation
588 between trait dissimilarity and environmental distance decreased as filtering weakened,
589 moreover, differences between families of indices became more apparent. This result suggests
590 that all tested methods are able to reveal the strong environmental filtering processes.

591 As the contribution of competitive exclusion and stochastic processes approach or override
592 environmental filtering, the correlation between FDissim indices and the background gradient
593 becomes weaker. This decrease itself is not a drawback of the FDissim methods, rather it is a
594 consequence of our study design, since we applied a series of scenarios where the effect of
595 niche filtering was decaying. However, we think that the degree of the decrease reflects the
596 sensitivity of the FDissim indices to the underlying trait-environmental relationship. Indices,
597 which showed high correlation with environmental distance, could be capable of revealing the
598 environmental signal even when it is weak. Actually, in our tests, most indices reached
599 similarly high correlation, and there were only a few combinations of simulation parameters

600 which resulted in a decreased correlation with environmental distance for some dissimilarity
601 indices.

602 *Determinants of the correlation based on the random forest model*

603 The random forest model revealed that the effect of gradient length is the most important
604 determinant of the correlation between dissimilarity and environmental distance, while
605 methodological decisions had much lower variable importance. These observations suggest
606 that the absolute value of the correlation between dissimilarity and environmental distance is
607 primarily dependent on the sample in hand, and can be influenced by methodological
608 decisions to a limited extent.

609 Correlations were stronger with abundance than with presence/absence data. This finding is at
610 least partly attributable to our simulation design where community composition was driven by
611 individual-based processes: birth, fitness difference, reproduction, and death. As a result,
612 species relative abundances had to be proportional with their environmental suitability in the
613 local community. Transforming such data to binary scale loses meaningful information and
614 weakens the correlation between dissimilarity in trait composition and environmental
615 background. In cases when presences and absences of species respond more robustly to the
616 main environmental gradient, while relative abundances change stochastically, or abundance
617 estimations are inaccurate, the binary data type might be more straightforward.

618 Transforming between-species dissimilarities has a potential to conform distributional
619 requirements, to approximate expert intuitions about relatedness of species or to customize
620 sensitivity to functional difference with respect to specific research aims. For most indices
621 across the tested range of gradient length and data type, the exponential transformation
622 resulted a somewhat lower correlation than with linear transformation. More insight is
623 provided by examining the shape of the relationships besides the pure correlation value. After

624 linear transformation of Gower distances, most dissimilarity indices showed a linear or
625 slightly curved function along environmental distance; although the scatter of the evenness-
626 based *generalized_TradiDiss* differed considerably from the straight line towards an
627 exponentially increasing one. After exponential transformation of between-species trait
628 dissimilarities, all indices in the direct dissimilarity-based class showed a rather steeply
629 increasing asymptotic function. This result suggests that with the exponential transformation
630 of between-species dissimilarities, it is possible to make FDissim indices more sensitive to
631 smaller differences in functional composition. Certainly, summary-based indices (*CWMDis*,
632 *CDFdis*) are not affected by this transformation, since they are not based on between-species
633 dissimilarities.

634 *Comparison of taxon-based vs. trait-based dissimilarity*

635 The basic assumption of functional ecology is that the traits of individuals should be in closer
636 relationship with ecological properties than their taxonomical status. Following this argument,
637 we expected that trait-based dissimilarity measures correlate more strongly with the
638 environmental background than species-based indices. In contrast, higher correlation of
639 species-based dissimilarity than trait-based dissimilarity indicates loss of information with the
640 introduction of between-species similarity – which is non-sensual since our data was
641 simulated in a way to possess a strong pattern in trait-environment relationship. We used the
642 Sørensen/Bray-Curtis index in a dissimilarity form as a reference method representing
643 species-based dissimilarity calculations disregarding traits. Our expectation was fulfilled by
644 all indices with the exception of the members of the nearest neighbour family (*D_{IP}*, *D_{CW}* and
645 *PADDis*). We suspect two potential reasons behind the low performance of these latter groups
646 of indices. The first one is the improper scaling factor used for standardizing the ‘operational
647 part’ of the indices (see the description in of the *PADDis* family and the discussion about it
648 under the paragraph “Within-family variation of indices”). Second, these indices rely on the

649 quantities of minimally different species in the two communities under comparison. However,
650 the minimum is a less robust descriptor of any sample distribution because of its dependency
651 on sampling error; therefore, it might provide a poor representation of total community
652 dissimilarity.

653 Although, we did not include dissimilarity values at exactly zero distance, the y-intercept (also
654 called ‘nugget’) of the dissimilarity vs. environmental distance functions can be extrapolated
655 with negligible error (Fortin & Dale 2005). Brownstein et al. (2012) argued that the nugget of
656 the distance decay relationship is a direct estimate of the amount of chance in the variation
657 between local communities. In this respect worth noting is that the nugget with species-based
658 Bray-Curtis index was near 0.4, while with all trait-based indices the nugget was near zero.
659 This suggests that without accounting for species similarities, environmental distance between
660 communities can be overestimated due to similar species replacing each other.

661 *Within-family variation of indices*

662 The perfect correlation between Jaccard, Sørensen and Sokal-Sneath forms of *dsimcom* and
663 *dissABC* families was expected, since the original, taxon-based Jaccard, Sørensen and Sokal-
664 Sneath indices are algebraically related, too (Janson & Vegelius 1981). However, for *PADDis*
665 Jaccard, Sørensen and Sokal-Sneath forms showed correlation below 1. At this family, the *B*
666 and *C* components of the 2×2 contingency table are defined as measurable quantities with
667 clear interpretation: the sum of species uniqueness values within each community. The total
668 diversity ($A+B+C$) is defined to be equal with the species richness of the pooled pair of
669 communities ($a+b+c$), and the quantity *A* is derived by subtracting ($B+C$) from it. With this
670 definition, *A* remains a virtual quantity with no biological interpretation. In *PADDis* indices,
671 trait-based quantities *B* and *C* appear in the numerator (the ‘operational part’ sensu Ricotta et
672 al. 2016) of the indices, while in the denominators (i.e., in the ‘scaling factor’) the taxon-
673 based quantities, *a*, *b* and *c* are used. We argue that the inconsistent behaviour of *PADDis* is

674 due to the application of taxon-based quantities for scaling factors of trait-based operational
675 parts. At the same time, we acknowledge that we either see no obvious solution to define total
676 diversity or shared diversity according to the uniqueness-based idea behind *PADDis* in a more
677 realistic way. In the *generalized_TradiDiss* family, the trait-based analogue of Bray-Curtis
678 index can be achieved by calculating generalized Canberra distance with uneven weighting of
679 species. We expected this to be perfectly correlated with Marczewski-Steinhaus form of
680 *generalized_TradiDiss* index with uneven weighting, since Bray-Curtis and Marczewski-
681 Steinhaus indices are the abundance forms of Sørensen and Jaccard indices, respectively.
682 However, the correlation between them was lower. In the *generalized_TradiDiss* family,
683 between-community dissimilarity is calculated as weighted sum a standardized differences in
684 species ordinariness values. Species ordinariness is calculated on the basis of species
685 abundance and trait values; however, weights used for adjusting species-level contributions
686 are derived solely from abundances. Therefore, *generalized_TradiDiss* also follows a ‘hybrid’
687 approach in accounting for taxon-based vs. trait-based information. We argue that this is the
688 reason why the algebraic relationships between the original Sørensen and Jaccard indices does
689 not apply to its Sørensen/Bray-Curtis-type and Jaccard/Marczewski-Steinhaus-type forms. To
690 sum up, we point to our observation that Jaccard, Sørensen and Sokal-Sneath forms of certain
691 families of indices do not satisfy the algebraic relationships they supposed to, opening space
692 for potential confusion. These algebraic relations hold only if *A*, *B* and *C* quantities are
693 explicitly and consistently defined.

694 Families of *FDissim* indices combine abundance difference of species between plots and
695 interspecific trait differences in a unique way, while indices belonging to the same family
696 differ in how they relate this amount of ‘unshared’ variation (summarized as the *b* and *c*
697 portions of the contingency table) to the shared (*a*) variation. Some indices are able to handle
698 abundances either as absolute or relative abundance (e.g. *dsimcom*, *generalized_TradiDiss*,

699 *dissABC*), while others divide absolute abundances by their sum over the respective
700 community, thus they work only with relative abundances. When indices in the former group
701 are set to consider absolute abundances, they become sensitive to variation in the summed
702 abundances of the communities under comparison. To place our tests on a common ground,
703 we simulated communities with equal total number of individuals, and set all indices, where
704 relevant, to work with relative abundances. Hence, we removed the effect of differences in
705 total abundance. The constant number of individuals might have increased the similarity
706 between FDissim indices belonging to the same family and the correlation with the
707 environmental gradient. The sum of abundances, let them be measured on any quantitative
708 scale, may vary considerably in real study situations due to aggregated distribution of
709 individuals or uneven sampling effort. Therefore, our findings are more likely valid for
710 settings when the sum of abundances are relatively stable, e.g. when sampling effort is
711 controlled and individuals are dispersed evenly, or when abundances are recorded on
712 percentage scale.

713 *Limitations of our study*

714 In our study, we simulated a research situation in a simplistic way. We applied only one
715 environmental gradient which operated as an environmental filter driving convergence on a
716 single trait. Besides this, we applied another trait which was constantly affected by a low level
717 of competitive exclusion. These two traits were uncorrelated. Nevertheless, there was some
718 effect of random drift on community composition due to the probabilistic components of the
719 simulation algorithm. We varied the strength of environmental filtering thus it had different
720 relative contribution compared with competitive exclusion and stochasticity. In real research
721 situations local trait composition is influenced by a wide range of processes, including several
722 abiotic and biotic filters acting simultaneously. Unless they are manipulated as parts of an
723 experimental system, the full set of such filters are usually unknown for the researchers. The

724 multiplicity of filters may reduce the ability of FDissim indices in recovering trait-
725 environment relationships. Further research should clarify how increasing complexity of the
726 sample affects the behaviour of FDissim indices.

727

728 **Conclusions**

729 Considering the diversity of concepts they are built upon, FDissim indices showed
730 unexpectedly low variation in performance. CWMdis, dsimcom, generalized_TradiDiss
731 acquired the highest correlation with environmental distance in all simulation scenarios,
732 therefore they seem to be equally suitable for quantifying pairwise beta diversity based on
733 traits. Nevertheless, the most important determinant of the matching between trait-based
734 dissimilarity and environmental distance is the length of the trait gradient. Besides this, the
735 data type (presence/absence vs. abundance) also affected the correlation more strongly than
736 the choice of FDissim method. Extending the comparative tests of FDissim measure to more
737 complex gradients and real data sets could offer further insight into their behaviour.

738

739 **Data availability**

740 Simulated data was generated using the comsimtv R package. Own functions for functional
741 dissimilarity indices are made available through the Zenodo public repository:
742 [10.5281/zenodo.4323590](https://doi.org/10.5281/zenodo.4323590).

743

744 **Author contributions**

745 A.L. designed and carried out the analysis, lead writing, Z.B.D. discussed the concept and the
746 results, wrote parts of and commented on the manuscript.

747

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969 **Tables and Figures**

970

971 Table 1. Similarity and dissimilarity forms of resemblance indices for presence-absence data

972

Name of the index	Similarity version	Dissimilarity version
Sørensen	$s_S = \frac{2a}{2a + b + c} = \frac{a}{(S_j + S_k)/2}$	$d_S = \frac{b + c}{2a + b + c} = \frac{b + c}{S_j + S_k}$
Ochiai	$s_O = \frac{a}{\sqrt{(a + b)(a + c)}} = \frac{a}{\sqrt{S_j S_k}}$	$d_O = \frac{b + c}{\sqrt{S_j S_k}}$
Kulczynski	$s_K = \frac{1}{2} \left(\frac{a}{a + b} + \frac{a}{a + c} \right) = \frac{a}{2/(1/S_j + 1/S_k)}$	$d_K = \frac{1}{2} \left(\frac{b}{a + b} + \frac{c}{a + c} \right) = \frac{1}{2} \left(\frac{b}{S_j} + \frac{c}{S_k} \right)$
Simpson	$s_{Si} = \frac{a}{a + \min(b, c)} = \frac{a}{\min(S_j, S_k)}$	$d_{Si} = \frac{b + c}{\min(S_j, S_k)}$
Jaccard	$s_J = \frac{a}{a + b + c} = \frac{a}{S_{jk}}$	$d_J = \frac{b + c}{a + b + c} = \frac{b + c}{S_{jk}}$
Sokal & Sneath	$s_{SS} = \frac{a}{a + 2(b + c)}$	$d_{SS} = \frac{2(b + c)}{a + 2(b + c)}$

973

974

975 Table 2. Classification of trait-based dissimilarity indices. In columns of input data type X-es indicate, if abundance (A), relative abundance (R),
 976 and presence-absence data can be used as input.

Class	Approach	Family	References	Input Data			R function
				A	R	P/A	
<i>Summary-based</i>	<i>Typical value</i>	<i>CWM-based</i>	Ricotta et al. (2015)	X	X	X	FD:::functcomp
	<i>Distribution-based</i>	<i>CDF-based</i>	Appendix S3	X	X	X	our new functions, see Data availability
<i>Direct dissimilarity</i>	<i>Probabilistic</i>	<i>DISC/D_Q</i>	Rao 1982, Pavoine & Ricotta (2014)	X	X	X	adiv:::SQ
		<i>dsimcom</i>	Pavoine & Ricotta (2014)	X	X	X	adiv:::dsimcom
	<i>Ordinariness-based</i>	<i>dissABC</i>	Pavoine & Ricotta (2015)	X	X	X	adiv:::dissABC
		<i>generalized_Tradiidiss</i>	Pavoine & Ricotta (2019)	X	X		adiv:::generalized_Tradiidiss
	<i>Diversity</i>	<i>multiplicative beta</i>	Chao et al. (2012)		X		our new functions, see Data

	<i>partitioning</i>						availability
	<i>Nearest neighbour</i>	$D_{CW}, D_{CW}(Q)$	Clarke & Warwick (1998), Ricotta & Bacaro (2010)		X	X	our new functions, see Data availability
		D_{IP}	Izsák & Prince (2001), Ricotta & Bacaro (2010)		X	X	our new functions, see Data availability
		<i>PADDis</i>	Ricotta et al. (2016)			X	adiv:::PADDis
<i>Classification-based</i>	not discussed	not discussed	Hérault & Honnay (2007), Nipperess et al. (2010), Cardoso et al. (2014), Pavoine (2016)				

978 Table 3. Kendall tau correlations between environmental distance and the functional
 979 dissimilarity measures at different values of sigma and with abundance data type

	Sigma=0.01	Sigma=0.1	Sigma=0.25	Sigma=0.5	Sigma=1	Sigma=5
<i>CWMdis</i>	0.974	0.905	0.846	0.828	0.649	0.251
<i>CDFdis</i>	0.974	0.904	0.845	0.83	0.646	0.255
<i>D(Q)</i>	0.974	0.912	0.832	0.828	0.637	0.243
<i>dsimcom.SS</i>	0.974	0.911	0.832	0.829	0.638	0.243
<i>dsimcom.Jac</i>	0.974	0.911	0.832	0.829	0.638	0.243
<i>dsimcom.Sor</i>	0.974	0.911	0.832	0.829	0.638	0.243
<i>dsimcom.Och</i>	0.974	0.911	0.832	0.829	0.639	0.243
<i>dsimcom.Beta</i>	0.974	0.911	0.832	0.829	0.638	0.243
<i>dissABC.Jac</i>	0.967	0.899	0.82	0.813	0.617	0.243
<i>dissABC.Sor</i>	0.967	0.899	0.82	0.813	0.617	0.243
<i>dissABC.SS</i>	0.967	0.899	0.82	0.813	0.617	0.243
<i>dissABC.Och</i>	0.968	0.899	0.819	0.814	0.618	0.243
<i>dissABC.Kul</i>	0.968	0.898	0.819	0.814	0.619	0.243
<i>dissABC.Si</i>	0.954	0.867	0.789	0.791	0.616	0.243
<i>Tradidiss.GC.even</i>	0.974	0.908	0.816	0.829	0.626	0.245
<i>Tradidiss.MS.even</i>	0.974	0.908	0.814	0.828	0.623	0.243
<i>Tradidiss.PE.even</i>	0.974	0.907	0.828	0.831	0.639	0.25
<i>Tradidiss.GC.uneven</i>	0.967	0.901	0.827	0.815	0.622	0.244
<i>Tradidiss.MS.uneven</i>	0.966	0.899	0.823	0.813	0.618	0.243
<i>Tradidiss.PE.uneven</i>	0.969	0.905	0.837	0.821	0.637	0.249
$\beta_{turnover}$	0.974	0.911	0.837	0.829	0.641	0.251
$\beta_{heterogeneity}$	0.974	0.911	0.837	0.829	0.641	0.251
$\beta_{segregation}$	0.974	0.911	0.837	0.829	0.641	0.251

D_{IP}	0.923	0.778	0.68	0.565	0.338	0.034
D_{CW}	0.923	0.778	0.68	0.565	0.338	0.034
<i>Bray-Curtis (species-based)</i>	0.711	0.832	0.778	0.678	0.455	0.086

980

981

982 Table 4. Kendall tau correlations between environmental distance and the functional
 983 dissimilarity measures at different values of sigma and with presence/absence data type

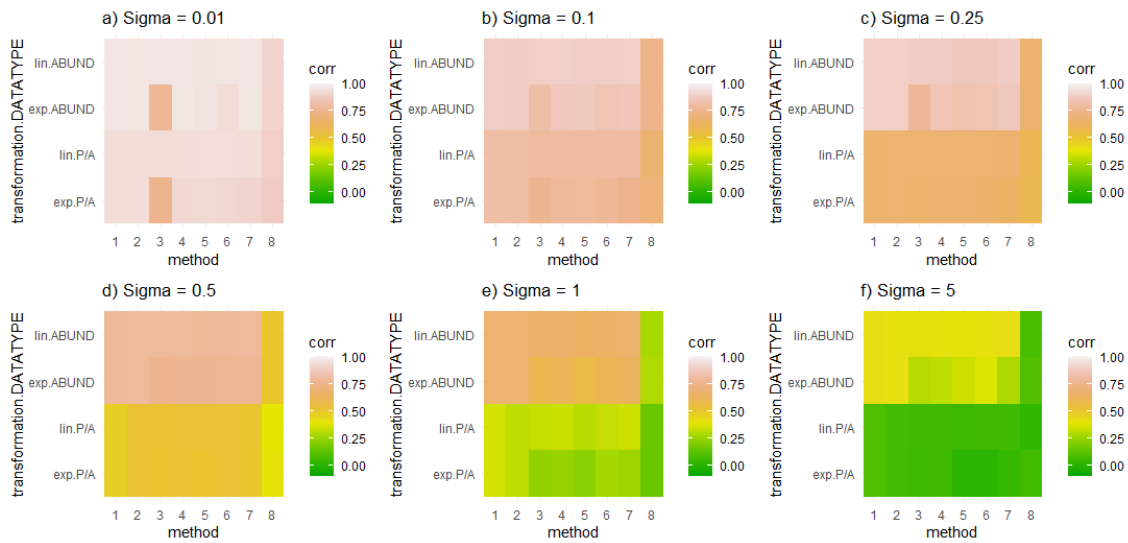
	Sigma=0.01	Sigma=0.1	Sigma=0.25	Sigma=0.5	Sigma=1	Sigma=5
<i>CWMdis</i>	0.944	0.818	0.691	0.568	0.353	0.014
<i>CDFdis</i>	0.943	0.820	0.700	0.594	0.306	-0.001
<i>D(Q)</i>	0.941	0.818	0.701	0.59	0.313	-0.003
<i>dsimcom.SS</i>	0.944	0.821	0.705	0.593	0.316	-0.003
<i>dsimcom.Jac</i>	0.944	0.821	0.705	0.593	0.316	-0.003
<i>dsimcom.Sor</i>	0.944	0.821	0.705	0.593	0.316	-0.003
<i>dsimcom.Och</i>	0.944	0.822	0.707	0.592	0.323	0.000
<i>dsimcom.Beta</i>	0.944	0.821	0.705	0.593	0.316	-0.003
<i>dissABC.Jac</i>	0.946	0.819	0.704	0.592	0.292	-0.006
<i>dissABC.Sor</i>	0.946	0.819	0.704	0.592	0.292	-0.006
<i>dissABC.SS</i>	0.946	0.819	0.704	0.592	0.292	-0.006
<i>dissABC.Och</i>	0.946	0.819	0.704	0.591	0.293	-0.006
<i>dissABC.Kul</i>	0.946	0.819	0.704	0.591	0.294	-0.006
<i>dissABC.Si</i>	0.939	0.835	0.701	0.556	0.324	0.019
<i>Tradidiss.GC.even</i>	0.945	0.820	0.707	0.593	0.305	-0.005
<i>Tradidiss.MS.even</i>	0.945	0.819	0.707	0.592	0.304	-0.005
<i>Tradidiss.PE.even</i>	0.947	0.821	0.704	0.595	0.323	-0.002
<i>Tradidiss.GC.uneven</i>	0.946	0.819	0.702	0.592	0.308	-0.006
<i>Tradidiss.MS.uneven</i>	0.946	0.819	0.703	0.592	0.307	-0.006
<i>Tradidiss.PE.uneven</i>	0.947	0.820	0.698	0.593	0.326	-0.003
$\beta_{turnover}$	0.943	0.817	0.699	0.585	0.331	-0.003
$\beta_{heterogeneity}$	0.943	0.817	0.699	0.585	0.331	-0.003
$\beta_{segregation}$	0.943	0.817	0.699	0.585	0.331	-0.003

<i>D_{IP}</i>	0.905	0.696	0.597	0.435	0.158	-0.017
<i>D_{CW}</i>	0.904	0.694	0.593	0.431	0.160	-0.017
<i>PADDis.Jac</i>	0.904	0.679	0.575	0.418	0.154	-0.025
<i>PADDis.Sor</i>	0.905	0.696	0.597	0.435	0.158	-0.017
<i>PADDis.SS</i>	0.902	0.662	0.546	0.396	0.144	-0.034
<i>PADDis.Och</i>	0.904	0.697	0.596	0.436	0.159	-0.017
<i>PADDis.Simp</i>	0.881	0.620	0.474	0.343	0.158	0.030
<i>PADDis.Kul</i>	0.904	0.694	0.593	0.431	0.160	-0.017
<i>Sørensen (species-based)</i>	0.698	0.724	0.606	0.415	0.127	0.048

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985

986 Figure 1. Heat maps showing the interactive effects of niche width (sigma), transformation of
987 between-species dissimilarities (lin = linear, exp = exponential), data type (ABUND =
988 abundance, P/A = presence/absence), and dissimilarity index (1 – *CWMDis*, 2 – *CDFdis*, 3 –
989 D_Q , 4 – *dsimcom*/Sørensen, 5 – *dissABC*/Sørensen, 6 – *generalized_Tradiidiss*/generalized
990 Canberra, uneven weighting, 7 – $\beta_{turnovers}$, 8 – D_{CW}) on the correlation with environmental
991 distance



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