Influence of the large-Z effect during contact between butterfly sister species

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Abstract

Comparisons of genomes from recently diverged butterfly populations along a suture zone in central Texas have revealed high levels of divergence on the Z chromosome relative to autosomes, as measured by fixation index, F_{st} . The pattern of divergence appears to result from accumulation of incompatible alleles, obstructing introgression on the Z chromosome in hybrids. However, it is unknown whether this mechanism is sufficient to explain the data. Here, we simulate the effects of hybrid incompatibility on interbreeding butterfly populations using a model in which populations accumulate cross-incompatible alleles in allopatry prior to contact. We compute statistics for introgression and population divergence during contact between model butterfly populations and compare them to statistics obtained for 15 pairs of butterfly species interbreeding along the Texas suture zone. For populations that have evolved sufficiently in allopatry, the model exhibits high levels of divergence on the Z chromosome relative to autosomes in populations interbreeding on time scales comparable to periods of interglacial contact between butterfly populations in central Texas. Levels of divergence on the Z chromosome increase when interacting groups of genes are closely linked, consistent with interacting clusters of functionally related genes in butterfly genomes. Results for various periods in allopatry are in qualitative agreement with the pattern of data for butterflies, supporting a picture of speciation in which populations are subjected to cycles of divergence in glacial isolation, and partial fusion during interglacial contact.

Introduction

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Recent studies comparing divergent populations of butterflies have revealed elevated levels of divergence on the Z chromosome relative to autosomes [1, 2]. To explain these observations, it was suggested that the observed patterns of divergence result from the accumulation of postzygotic incompatibilities, obstructing introgression on the Z chromosome in hybrids (see, for example, Fig. 5 of reference [2]). However, it is known that a number of other factors can contribute to this effect, such as changes in population size, differing rates of reproductive success for male and female butterflies, and a smaller effective population size for Z chromosomes relative to autosomes [3]. As a result, it is of interest to know the "bare" contribution of hybrid incompatibilities to the extent of divergence in autosomes and Z chromosomes, e.g. in a model where these effects are absent and mutations are individually neutral. In this work, we develop such a model and compare our results to those obtained by Cong et al. [2] for 15 closely related species of butterfly interbreeding along a suture zone in central Texas.

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The central Texas suture zone is formed by emigration of species from glacial refugia along coastal and inland regions of Mexico and the southern United States, including the Yucatan peninsula and the state of Florida (see Figs S1 and S2). The species sampled by Cong et al. diverged on the order of 1 million years ago [4], and have, as a result, experienced multiple periods of glacial cooling and interglacial warming. During glacial periods, central Texas was subjected to severe decreases in temperature [5], which would have caused drastic, if not total isolation of sister species in southeastern and southwestern refugia; During the most recent warming period, sister species migrated into Texas, while major portions of the populations remained in refugial regions, isolated from the suture zone by large distances. To determine the influence of hybrid incompatibilities with the Z chromosome during contact, we will at first neglect the effects of isolation by

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distance, and consider a generic model of secondary contact [6, 7] in which a population divides, the resulting sister populations evolve for a period in allopatry while accumulating hybrid incompatibilities, and later begin to interbreed. We then compare measures of introgression and population divergence for gene sequences in our model during periods of contact to results obtained for ~ 1 kb sequence windows by Cong et al. [2].

To represent the state space for pairs of sister populations, Cong et al. employed two basic statistics: The index of gene flow, I_{gf} , a simple extension of the indicator function G_{min} developed by Geneva et al. [6], defined as the fraction of sequence windows with $G_{min} \leq 0.25$, and the fixation index, or relative divergence, F_{st} . I_{gf} describes the fraction of sequence windows where introgression has occurred, while F_{st} describes the degree of genomic difference between populations (we note that I_{gf} is not directly related to gene flow as measured by the effective migration rate [8]). Multiple genomic samples were collected from each pair of populations, and separate indices were computed for autosomes and Z chromosomes. The results are shown in Fig. 1; The data points in this figure describe index values for sister organisms that have been classified as different species in the literature (green), more closely related organisms for which classification is uncertain (yellow), and samples of the same species (red). When populations are compared through their autosomes (Fig. 1A), the data exhibit a continuous pattern across the entire range of index values; However, for the Z chromosome (Fig. 1B), the data obtained from samples of the same species (red) are separated from those of closely related species by a gap of "missing" values, which could suggest a rapid transition [1,9]. For different species (green and yellow data points), F_{st} values for the Z chromosome are always larger than those for autosomes (Fig. 2). At the same time, the fraction of divergent nucleotide positions in the Z chromosomes of sister species is slightly smaller than that for autosomes [2], indicating similar rates of adaptation. In accord with these results, Cong et al. have argued that the

pattern of data in Fig. 1 reflects the influence of negative interactions between autosomes and Z chromosomes in hybrids during periods of interbreeding – i.e., the large-Z effect [3].

Our goal in this work is to determine whether this mechanism is sufficient to explain the data for butterflies – in particular, the large gaps, $\Delta F = F_Z - F_A$, between F_{st} values for autosomes and Z chromosomes shown in Fig. 2. To accomplish this, we simulate populations with different divergence times in allopatry, different migration rates, and different levels of hybrid incompatibility, leading either to fusion or continued divergence during secondary contact. Mutation rates, and rates of recombination within and between gene sequences are varied about values for *Drosophila* and *Heliconius* butterflies. As Bank et al. have pointed out [10], negative interactions between individually neutral mutations (i.e., neutral incompatibilities) are unstable in interbreeding populations, and ultimately break down due to recombination [11]. However, when crossovers between genes are infrequent, consistent with closely linked genes on butterfly chromosomes, there is an initial period during secondary contact where ΔF can increase dramatically, depending the migration rate and the strengths of interactions between incompatible alleles. In this case, which would perhaps correspond to interacting clusters of functionally related genes [12,13], large values of ΔF can develop in fusing populations on time scales comparable to interglacial warming periods; During these periods, the gap of missing F_{st} values obtained in Fig. 1B is statistically likely over a wide range of interaction strengths and migration rates for populations that have diverged sufficiently in allopatry. Mean values of I_{gf} during allopatry and secondary contact are in good agreement with Fig. 1 for autosomes, but slightly larger than expected for the Z chromosome. We return to these points later below.

Methods

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We simulate populations of diploid individuals evolving in allopatry and secondary contact, and we compute statistics for gene segments, consistent with the approach used in Fig. 1. Model genomes consist of several pairs of chromosomes, each containing a number of binary genes of length L loci. Populations evolve by plain Wright–Fisher dynamics with random mating between male and female individuals [14]. In each generation, mutations occur within genes at a rate μ per gene per generation. Pairs of male and female individuals are then selected at random according to fitness for mating. Male genomes undergo explicit meiosis, in which chromosomes are duplicated, and the resultant chromatids undergo random crossing over [15], with separate rates, r and r' , for crossing over within and between gene segments (meiosis is achiasmatic in model females, consistent with butterfly reproduction [16]). A single offspring is generated from each mating event by random union of male and female gametes, and the process is continued until the original population is replenished. Finally, an equal number of offspring (with mean $N\epsilon$, where N is the size of a population and ϵ is the migration rate) are randomly selected from each population to undergo migration, and the selected individuals are then exchanged between populations (in allopatry, $\epsilon = 0$).

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We consider two different scenarios for secondary contact: In scenario (i), a population of size N is first equilibrated for a period of Δt_E generations. Let $\mathbf{g}_l = (g_l, g'_l)$ denote the allelic state of a diploid locus l in a genome $\mathbf{g}$. Initially, all genomes in the population have $\mathbf{g}_l = 0$ uniformly, and mutation events act to assign the maternal (g_l) or paternal (g'_l) states of a locus to 1. All mutations are individually neutral. After equilibration, loci that have fixed in the population for the mutant allele type are returned to their initial states. The population is then duplicated, and the resultant "sister" populations evolve in allopatry for a period Δt_A . At the end of this period, loci that have fixed for

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the mutant allele across both populations are returned to their initial state. Several pairs
of loci are then selected to participate in hybrid fitness interactions (see below), and the
two populations evolve in contact for a period Δt_C subject to fitness costs incurred due
to interactions formed by various allele combinations at the selected loci. In scenario (ii),
the entire procedure is the same, except that the initial population has size $2N$ before
dividing into two populations of size N . In both scenarios, the W chromosome acts only
to determine the sex of an individual.

During allopatry, mutant alleles are lost, or rise toward fixation in each population via
genetic drift. Loci that are nearly fixed for the mutant allele type in one population are
usually far from fixation in the other. Let $p_{l,\gamma}$ denote the frequency of the mutant allele
type at locus l in population γ , with $\gamma = 1, 2$. To describe the cost of hybridization,
we select loci in autosomes for which $p_{i,1} \sim 1$ and $p_{i,2} \sim 0$ to interact negatively with loci
in the Z chromosome(s) for which $p_{j,1} \sim 0$ and $p_{j,2} \sim 1$ (see Fig. 3). We then repeat
this process with the population subscripts interchanged, selecting an equal number of
loci in autosomes with $p_{i,2} \sim 1$ and $p_{i,1} \sim 0$ to interact negatively with loci in the Z
chromosome(s) for which $p_{j,2} \sim 0$ and $p_{j,1} \sim 1$.

Let $f(\mathbf{g}_i, \mathbf{g}_j)$ denote the log fitness cost for a pair of selected loci, (i, j) . We define
 f as follows: If both loci are homozygous for the mutant allele, $f = 4s$; if one locus is
homozygous for the mutant allele and one locus is heterozygous, $f = 2s$; and if both
loci are heterozygous, $f = s/4$. For all other combinations, $f = 0$. The fitness of a
genome $\mathbf{g}$ is then defined as, $w = \exp - \sum_{(i,j)} f(\mathbf{g}_i, \mathbf{g}_j)$. Here, mutant loci on the single Z
chromosome of a female genome are dominant, and act as homozygous loci on the two Z
chromosomes of a male genome. This condition, and the fact that f is less than s when
both loci are heterozygous, ensures that hybrid females are typically less fit than hybrid
males, consistent with Haldane's rule. As result, gene flow on the Z chromosome is limited

by the fitness of female genomes, in accord with the analysis of Cong et al. [2]. For male 144
genomes, the fitness model is basically the same as the "pathway" model used by Lindtke 145
and Buerkle to describe hybrid interactions among autosomal loci [11]. 146

Below, we simulate populations of genomes with three pairs of chromosomes in which 147
autosomes carry three genes, and Z chromosome carry six genes. To define w , we select 148
six pairs of loci for which the differences between $p_{l,1}$ and $p_{l,2}$ above are largest. In 149
most of the simulations, we select loci that connect the first pair of autosomes to the Z 150
chromosome(s). The parameters of the simulations are selected so that their scaled values 151
($N\mu$, Nr , and Nr') agree in order of magnitude with values obtained for *Heliconius* and 152
Drosophila, an organism commonly used to infer the biochemical functions of butterfly 153
genes [2]. The scaled mutation rate for a gene (of typical length 1770 bp) in *Drosophila* is 154
about $N\mu \sim 1$ [17]; Here, we will assume a similar rate for butterflies. The typical length 155
of a chromosome in *Heliconius* is about 20 Mbp, and the crossover rate per chromosome is 156
about $r \sim 1$ per generation [16]; If we assume that genes in *Heliconius* are comparable in 157
length to those in *Drosophila*, we obtain a crossover rate per gene in *Heliconius* of about 158
 $r \sim 10^{-4}$ per generation. The effective population size for *Heliconius* is about 10^6 , which 159
leads to a scaled rate of about $Nr \sim 100$ per gene per generation [3]. 160

In practice, we describe genes using strings of characters in our C++ code. The 161
number of mutant alleles participating in a gene segment is typically less than a few 162
percent for the timescales considered here, so that most of the loci in a gene do not 163
carry divergent mutations (see [2] for comparison with butterfly populations). For this 164
reason, we use smaller gene strings of length $L = 100$ loci in our code to reduce the cost 165
of the simulations. We simulate populations of $N = 10^4$ individuals, while varying the 166
parameters s , ϵ and r' . Since the morphologies (i.e., sex organs, wing color patterns, etc.) 167
of butterfly sister specimens are very similar, prezygotic barriers to introgression may be 168

small. For this reason, we sample moderate to large migration rates, $0.1 \leq N\epsilon \leq 10$. To counterbalance the effects of migration, we sample a broad range of interaction strengths, $0.01 \leq s \leq 0.1$, including the "null model", $s = 0$, for comparison. Our main findings are summarized in the figures below. Supporting figures are contained in the supplementary material file. Data and C++ code used to conduct the simulations can be obtained from: <https://cloud.biohpc.swmed.edu/index.php/s/D766rG6fWZWrsfG>.

Results

To begin our investigation, we first explore the time dependence of the statistics G_{min} and F_{st} for populations evolving in allopatry for comparison with the results of Geneva et al. [6]. To define the statistics, let $d_l^{\mu\nu} = |g_l^\mu - g_l^\nu|$ denote the difference (Hamming distance) between genomes $\mathbf{g}^\mu$ and $\mathbf{g}^\nu$ at (haploid) locus l , and let

$$d_{\lambda, \lambda+\Delta}^{\mu\nu} = \sum_{l=\lambda}^{\lambda+\Delta} d_l^{\mu\nu} \quad (1)$$

denote the distance between $\mathbf{g}^\mu$ and $\mathbf{g}^\nu$ for a window of loci, $[\lambda, \lambda + \Delta]$. Assume that we have sampled a small number of genomes from each population. For a given window of loci, G_{min} is then defined as the ratio [6],

$$G_{min} = \min d_{\lambda, \lambda+\Delta}^{\mu\nu} / \overline{d_{\lambda, \lambda+\Delta}^{\mu\nu}}^{1,2} \quad (2)$$

where $\min d_{\lambda, \lambda+\Delta}^{\mu\nu}$ and $\overline{d_{\lambda, \lambda+\Delta}^{\mu\nu}}^{1,2}$ are the minimum and average distances between sequences sampled from different populations; The fixation index, or relative divergence is defined as [6],

$$F_{st} = 1 - \frac{\overline{d_{\lambda, \lambda+\Delta}^{\mu\nu}}^1 + \overline{d_{\lambda, \lambda+\Delta}^{\mu\nu}}^2}{2 \overline{d_{\lambda, \lambda+\Delta}^{\mu\nu}}^{1,2}} \quad (3)$$

where, for example, $\overline{d_{\lambda, \lambda+\Delta}^{\mu\nu}}^1$ is the average distance between sequences sampled from population 1 with $\mu \neq \nu$. Below, we compute G_{min} for individual gene sequences, and we compute F_{st} by averaging the numerator and denominator of the fraction in Eq. (3) over gene sequences [18]. Unless otherwise noted, we compute G_{min} by sampling four genomes from each population, and we compute F_{st} by sampling ten genomes from each population (this is intended as a means to reduce noise in plots like Fig. 1). The introgression measure, I_{gf} , is defined as the fraction of gene segments with $G_{min} \leq 0.25$ (see Fig. 4A of Geneva et al. [6] for comparison). Except for the number of samples used to compute F_{st} , our approach is the same as that used by Cong et al. [2].

In Fig. 4, we plot F_{st} and G_{min} for autosomal genes as a function time since diverging in allopatry under scenarios (i) and (ii). The results can be compared with those in Fig. 2 of Geneva et al. [6]. Although a direct comparison is not possible (Geneva et al. average simulations of a single sequence window over a range of μ and r values), our results behave as one would expect for the lower values of μ and r used in our simulations (note that the transition to allopatry in Geneva et al. is analogous to our scenario (i)). Interestingly, there is a noticeable difference in the plots of G_{min} for duplication and division of populations in allopatry, and we find that scenario (ii) leads to closer agreement with butterfly data for I_{gf} (Fig. 5). Plots of F_{st} computed from four and ten samples per population are essentially identical (this is not surprising since F_{st} already reflects an average over several gene windows).

In the remaining figures, we describe results for secondary contact between populations under scenario (ii). To plan our simulations, we assume that periods of contact are comparable to those of real populations during interglacial warming periods. The time scale for interglacial periods in North America over the last million years is roughly between 10^4 and 10^5 years. To calibrate the model to real time scales, we assume, consistent with

our choice of parameters, that N generations in the model correspond to N_e generations 211
for butterfly populations, where N_e is the effective population size for butterflies. Then, 212
solving for α in the expression $\alpha N_e \tau = \Delta \tau$, where τ is the generation time and $\Delta \tau$ is the 213
length of an interglacial period, the corresponding period of contact in the model is αN . 214
Although data for N_e is unavailable for the species in Fig. 1, we can obtain a rough idea 215
of how N_e varies over time and among species from the study of *Heliconius* populations 216
by van Belleghem et al. [3] (for *Drosophila*, see [19]). Below, we focus our attention on 217
values of $N_e \tau$ on the order of 10^5 years, consistent with the lower range of N_e values in 218
van Belleghem et al. [3], in which case, N generations in the model corresponds to the 219
length of a glacial or interglacial period for butterflies. We then simulate different values 220
of ϵ and s for different periods in allopatry. 221

The results of this survey are summarized in Figs 6–9. In Figs 6 and 7 we plot the 222
mean value of F_Z versus F_A during contact for populations that have evolved in allopatry 223
for $\Delta t_A = N$ and $\Delta t_A = 2N$ generations; The mean values of F_A just prior to contact 224
are $F_A \simeq 0.3$ and $F_A \simeq 0.5$, respectively. Populations remain in contact for $\Delta t_C = N$ 225
generations. Each set of averages (circles, squares, etc.) is the result of 128 replicate 226
simulations (i.e., with the same values of s and ϵ) sampled every 100 generations. Lower 227
panels in the figures describe the fraction of simulations contributing to each data point 228
The numbers of samples per data point are shown in Figs S3 and S4. Of particular 229
interest is the index value $F_A \simeq 0.15$, the smallest value of F_A for different species (yellow 230
and green data points) in Fig. 2. As is evident by inspection of the data for $F_A \simeq 0.15$ in 231
Fig. 6B, large values of ΔF , consistent with the data for butterflies (Fig. 2), can occur at 232
low frequency if hybrid interactions are sufficiently strong. For weaker interactions (Fig. 233
7), such that small values of F_A are frequent, the mean value of F_Z still usually remains 234
above the point $F_Z \simeq 0.3$ corresponding to the lower edge of the data for different species 235

in Fig. 1. As a result, samples taken from a simulation during contact are unlikely to occur in the region of missing F_Z values. A similar pattern emerges for shorter times in allopatry, with more weakly diverged populations (Fig. 6A); Because fewer loci reach fixation when Δt_A is small, stronger interactions are required to maintain a significant level of divergence for the Z chromosome. In all of the simulations, mean values for I_A versus F_A , and I_Z versus F_Z during contact are similar to those during allopatry in Fig. 5. However, I_Z values are typically larger than those for butterflies (Fig. 1) at intermediate values of F_Z ; Results for $s = 0.1$ and $\Delta t_A = 2N$ are shown in Fig. 8 (note that data is recorded in the gap region, $F_Z \leq 0.3$, consistent with Fig. 6). As expected [11], larger rates of crossing over between genes, consistent with larger distances between genes on butterfly chromosomes, lead to smaller differences, ΔF , between F_Z and F_A (Fig. 9). Interestingly, the "null model" leads to smaller values of ΔF during contact (Fig. 9) than allopatry (Fig. 5). Lower rates of migration, for which populations tend toward continued speciation, are briefly explored in Figs S6–S7. In this case, populations do not exhibit "fat tail" statistics for low values of F_A , and large values of ΔF are less frequent.

In planning our simulations, we have implicitly assumed that real populations are subjected to repeated periods of isolation and contact on the order of glacial and interglacial periods. Given that real populations may be in various stages of divergence, we studied a single cycle of isolation and contact as a means to determine the influence of large-Z hybrid interactions during periods of contact. Because the morphologies of butterfly sister species (i.e., sex organs, wing color patterns, etc.) are similar, species boundaries are presumed to be somewhat porous, consistent with higher rates of migration in the model. For sufficiently strong interactions, the model leads to large differences between F_Z and F_A under fusion conditions, comparable, on average, to those in Fig. 2. In addition, the gap region, $F_Z \leq 0.3$ in Fig. 1 is statistically unlikely in the model over a wide range

of interaction strengths and migration rates. However, while mean values of I_A during
 contact are consistent with the data for I_A in Fig. 1A, the results for I_Z are clearly differ-
 ent from Fig. 1B for intermediate values of F_Z , and appear to reflect a missing feature,
 or features, in the model dynamics. For example, if male butterflies are more abundant
 than females, effective population sizes and levels of introgression on autosomes and Z
 chromosomes will tend to be similar, which should lead to smaller values of I_Z . Increasing
 the numbers of genes segments considered in the model may also lead to better results.
 In any case, the model is clearly a very simplistic representation of butterfly dynamics.

In real populations [2] butterflies forage and interbreed on large structured landscapes,
 often consisting of connected islands on which butterfly numbers can vary dramatically
 (see, for example [20–22]). During periods of isolation, sister populations may evolve
 discordant mating cycles [13] and mate preferences [1], which limit interbreeding during
 periods of contact. Organisms can also evolve preferences for local resource types [23],
 which can limit migration across contact zones, or cause asymmetry in migration rates.
 Although some of these effects have been explored using island, or stepping stone mod-
 els [10, 11, 24, 25], it would be interesting to know how interbreeding populations evolve
 on continuous landscapes, including basic behavioral aspects of butterflies (e.g. flight
 patterns [21], mating cycles, etc.), and the topographies of their resource distributions.
 The present work is a first step toward this goal.

Acknowledgments

It is a pleasure to thank Jing Zhang and two anonymous reviewers for helpful comments
 during the completion of this work. This study is supported in part by a grant (to NVG)
 from the National Institutes of Health (GM127390).

Fig. 1. Index of gene flow versus index of fixation for autosomes (A) and Z chromosomes (B) of sister species sampled by Cong et al. Data for I_A and I_Z is multiplied by a factor of 4 to remove a scaling factor used in their work. Data points describe pairs of organisms that have been classified as different species in the literature (green), closely related organisms for which classification is uncertain (yellow), and organisms of the same species (red). The dotted lines in panel (B) are included simply to guide the eye.

Fig. 2. Correlation between F_Z and F_A from Fig. 1. The dotted line $F_Z = F_A$ is included to guide the eye.

Fig. 3. Part of a hybrid genome formed at the time of contact. The illustration describes a pair of hybrid interactions (dotted lines) connecting selected alleles (solid lines) in the Z chromosome (left) to selected alleles in an autosome (right) in a male hybrid genome. Gene segments are denoted by shaded squares.

Fig. 4. Mean value of G_{min} and F_{st} for autosomal genes as a function time since diverging in allopatry under scenarios (i) (green) and (ii) (maroon). Averages are computed from 128 replicate simulations with $N = 10^4$, $\mu = 10^{-4}$, and $r, r' = 10^{-2}$. The plots are precise polynomial fits to the averages.

Fig. 5. Mean value of I_A and F_Z versus F_A (squares) corresponding to the simulations in Fig. 4. Error bars denote the widths of the distributions. Broken lines are precise polynomial fits to the paths defined by $\langle I_A \rangle(t)$ and $\langle F_Z \rangle(t)$ versus $\langle F_A \rangle(t)$ as a function of time, where braces denote averaging over simulations (a plot of $\langle I_Z \rangle(t)$ versus $\langle F_Z \rangle(t)$ for scenario (ii) (orange) is also included for comparison with Fig. 1). The widths of the distributions for I_{gf} reflect the small number of gene sequences considered in the model.

Fig. 6. Mean value of F_Z versus F_A for several values of the migration rate, $N\epsilon = 1.5$ (circles), 2.5 (squares), 4 (triangles), and 6 (crosses), and different times in allopatry. Each set of averages is computed from 128 replicate simulations with $N = 10^4$, $\mu = 10^{-4}$, $r, r' = 10^{-2}$ and $\Delta t_C = N$. Error bars describe the widths of the distributions for $N\epsilon = 4$. Lower panels describe the fraction of simulation paths contributing to each bin for F_A .

Fig. 7. Mean value of F_Z versus F_A for decreasing interaction strengths. The parameters of the simulations are the same as those listed in Fig. 6 except where indicated in the figure.

Fig. 8. Mean values of I_A versus F_A and I_Z versus F_Z for the simulations in Fig. 6B. Error bars indicate the widths of the distributions for $N_\epsilon = 4$. The widths reflect the relatively small numbers of gene sequences used to determine I_A and I_Z .

Fig. 9. Mean value of F_Z versus F_A as the rate of crossing over between gene sequences is increased from $r' = 0.01$ (circles) to $r' = 0.1$ (squares). Averages are computed from 128 replicate simulations with $s = 0.01$, $N = 10^4$, $\mu = 10^{-4}$, $r = 10^{-2}$, and $\Delta t_C = N$. Results for the "null model" ($s = 0$) for $r' = 0.01$ (triangles) are included for comparison. Additional statistics are provided in Fig. S5.

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