- 1 GxEsum: a novel approach to estimate the phenotypic variance explained by
- 2 genome-wide GxE interaction based on GWAS summary statistics for biobank-
- 3 scale data

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### 1 Abstract

- 2 Genetic variation in response to the environment is fundamental in the biology of
- 3 complex traits and diseases, i.e. genotype-by-environment interaction (GxE).
- 4 However, existing methods are computationally demanding and infeasible to handle
- 5 biobank-scale data. Here we introduce GxEsum, a method for estimating the
- 6 phenotypic variance explained by genome-wide GxE based on GWAS summary
- 7 statistics. Through comprehensive simulations and analysis of UK Biobank with
- 8 288,837 individuals, we show that GxEsum can handle a large-scale biobank dataset
- 9 with controlled type I error rates and unbiased GxE estimates, and its computational
- 10 efficiency can be hundreds of times higher than existing GxE methods.

- 14 Keywords
- GxE interaction, whole-genome approach, Biobank-scale data, reaction norm model,
   LDSC

#### 1 Background

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The success of the human genome project has led to a paradigm-shift in the 3 complex trait analysis that focuses on the genome-wide association studies (GWAS) 4 5 [1]. GWAS have been incredibly successful at identifying genome-wide significant single nucleotide polymorphisms (SNPs) that are associated with causal variants 6 underlying complex traits [2, 3]. Moreover, whole-genome approaches, using all 7 8 common SNPs across the genome, have been useful to dissect the genetic 9 architecture of complex traits, e.g. SNP-based heritability and genetic correlation [4]. 10 However, the analytical modelling used in GWAS and whole-genome approaches usually assumes that there is no genotype-environment interaction (GxE), which can 11 12 be often violated against the true genetic architecture of complex traits. Indeed, 13 interaction is fundamental in biology and there has been increasing interest in estimating GxE, using genome-wide SNPs [5-7]. 14 Current state-of-the-art whole genome methods for estimating GxE include 15 16 genotype-covariate interaction genomic restricted maximum likelihood (GREML) and random regression GREML [8]. Recently, a multivariate reaction norm model (RNM) 17 has been introduced [9], which can disentangle GxE from genotype-environmental 18 correlation, providing more reliable GxE estimations. These methods typically 19 employ the GREML approach that requires individual level genotypes and is 20 computationally intensive. Especially when using biobank-scale data, the approach 21 becomes computationally intractable. 22 23 To reduce the computational limitation of GREML, linkage disequilibrium score 24 regression (LDSC) was introduced to estimate SNP-based heritability and genetic correlation [10]. LDSC is computationally efficient and requires no individual-level 25 genotypes. Instead, it uses GWAS summary statistics, regressing the association 26 27 test statistics of SNPs on their LD score. However, existing LDSC methods are

limited to additive models only [11-14].

In this study, we propose a novel approach to estimate the phenotypic variance 29 explained by genome-wide GxE based on GWAS summary statistics (GxEsum) for a 30 31 large-scale biobank dataset, correctly accounting for genotype-environment correlation and scale effects. In simulated and real data analyses, we show that the 32 computational efficiency of the proposed approach is substantially higher than RNM, 33 an existing GREML-based method, while the estimates are reasonably accurate and 34 35 precise. Because of this computational advantage, GxEsum may be an efficient tool 36 to estimate GxE that can be applied to large-scale data across multiple complex 37 traits.

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#### 1 **Results**

### 2 Method Overview

We propose a method to estimate the phenotypic variance explained by the wholegenome GxE, based on GWAS summary statistics, referred to as GxEsum. GxEsum can be a computationally efficient RNM using an extension of the LDSC approach. While the existing LDSC approach is designed to use estimated additive SNP effects in GWAS summary statistics (Supplementary Note 1), GxEsum requires summary statistics of SNP-by-environment interaction effects. For SNP effects modulated by an environment, the expected chi-square statistic ( $\chi_j^2$ ) is

$$\mathbf{E}[\chi_{j}^{2}|\ell_{j}] = \frac{N\sigma_{g_{1}}^{2}}{M} * \ell_{j} + 1 + 2(\sigma_{g_{1}}^{2} + \sigma_{\tau_{1}}^{2})$$

where N is the number of individuals, M is the number of SNPs,  $\sigma_{g_1}^2$  is the variance 10 due to GxE,  $\sigma_{\tau_1}^2$  is the variance due to residual heterogeneity or scale effects caused 11 by residual-environment interaction (RxE) and  $\ell_j$  is the LD score at the variant j that 12 can be estimated from a reference panel (please see Methods for a full derivation of 13 this equation). The  $\chi_i^2$  test statistics corresponds to the regression coefficient for the 14 interaction between the *i*th SNP and the environmental covariate (E). The outcome 15 trait is pre-adjusted for confounders and the main effects of E and then a regression 16 17 model with the main and interaction effects is run by SNP-by-SNP. If chi-square statistics from GWAS are regressed on LD scores, non-genetic interaction effects 18  $(\sigma_{\tau_1}^2)$  are captured by the intercept, from which GxE  $(\sigma_{g_1}^2)$  can be disentangled. 19 Consequently, GxE effects estimated by GxEsum are equivalent to that adjusted for 20 RxE when using RNM [9]. 21

To validate the proposed model, i.e. GxEsum, we used various simulations based on real genotype data (see Supplementary Note 2 for a full description of the simulation models). In simulations with and without GxE, we assessed the type I error rates and the accuracy of estimated GxE. We deliberately generated confounding effects such as genotype-environment (G-E) correlation, RxE and residual-environment (R-E) correlation to see if the type I error rate and the accuracy of GxEsum were affected by these confounding factors.

In the real data analysis, we used the UK Biobank data with 288,837 unrelated
individuals after stringent quality control. Subsets of the data with various sample
sizes were analysed to compare the precision (i.e. power) and the computational
efficiency of GxEsum and GREML-based GxE model (i.e. RNM).

Finally, we show how the genetic effects of a complex trait (e.g. BMI, hypertension or
 type 2 diabetes) are modulated by environment (e.g. neuroticism score, alcohol
 intake frequency, physical activity or age) by using the proposed method.

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# 1 Simulations

- 2 For a continuous trait, under the null (no GxE), whether or not there were
- 3 confounding effects (RxE and G-E and R-E correlations), the type I error rate of
- 4 GxEsum was not significantly inflated (Table 1). Note that the use of 500 replicates
- 5 for each simulation scenario can detect a type I error of greater than 0.07 or less
- 6 than 0.03 as significantly different from 0.05, using the binomial distribution theory
- 7 [15, 16]. Even with larger confounding effects (Supplementary Table 1), there was no
- 8 inflation for the type I error rate of GxEsum.

### 9 Table 1. Type I error rates of GxEsum to detect GxE at a significance threshold of p-

### 10 value < 0.05.

Scenarios	Type   Error rate	
Var(GxE <sup>a</sup> ) = 0, var(RxE <sup>b</sup> ) = 0	0.066	
Var(GxE) = 0, var(RxE) = 0, G-E correlation <sup>c</sup> = 0.1	0.064	
Var(GxE) = 0, var(RxE) = 0, R-E correlation <sup>d</sup> = 0.1	0.044	
Var(GxE) = 0, var(RxE) = 0, G-E correlation=0.1, R-E 0.056 correlation=0.1		
$Var(GxE^{a}) = 0$ , $var(RxE^{b}) = 0.1$	0.044	
Var(GxE) = 0, var(RxE) = 0.1, G-E correlation <sup>c</sup> = 0.1	0.034	
Var(GxE) = 0, var(RxE) = 0.1, R-E correlation <sup>d</sup> = 0.1	0.028	
Var(GxE) = 0, var(RxE) = 0.1, G-E correlation=0.1, R-E correlation=0.1	0.054	
Average	0.049	

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<sup>a</sup>GxE: Genotype-Environment interaction, <sup>b</sup>RxE: Residual-Environment interaction, <sup>c</sup>G-E
 correlation: Genotype-Environment correlation, <sup>d</sup>R-E correlation: Residual-Environment
 correlation. We simulated phenotypic data based on a real genotypic dataset (ARIC GWAS)
 including 7,263 participants with 583,085 SNPs, using various scenarios. The phenotypes
 were standardised such that the phenotypic mean was 0 and the phenotypic variance was 1.
 Type I error rate (i.e. false-positive) was estimated from 500 replicates for each scenario.

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19 In simulation with non-zero interactions, estimated GxE (g1) was not remarkably

20 different from the true values whether there were significant G-E and R-E

21 correlations or not (see supplementary Figure 1). It was noted that RxE component

22 was correctly captured by the intercept and not confounded with GxE estimates even

when using non-normal environmental variables (Supplementary Note 3 and

Supplementary Tables 2 and 3). In the absence of RxE, estimated GxE was also

unbiased (Supplementary Figure 2). The estimated GxE seemed robust to different

values of G-E and R-E correlations ranging from 0.05 to 0.2, respectively

27 (Supplementary Figures 3 and 4).

28 On the other hand, estimated main genetic variance (g0) was slightly biased

especially when using a large G-E or R-E correlation (Supplementary Figure 4). This

30 is probably because of the fact that the main genetic effects are over-adjusted for the

- 1 environment due to the large correlations (between the trait and environment) in the
- 2 model.
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#### 4 Table 2. Type I error rates of GxEsum when using binary disease traits with various

5 population prevalence.

Scenarios	Population prevalence (k)	Type l error rate
	0.025	0.052
	0.05	0.042
Var(GxE) = 0, Var(RxE) = 0	0.1	0.076
	0.5	0.054
	0.025	0.044
Var(GxE) = 0, Var(RxE) = 0.1	0.05	0.036
(on the liability scale)	0.1	0.050
	0.5	0.052
Average		0.050

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We simulated quantitative phenotypic data based on a real genotypic dataset (ARIC GWAS)
including 7,263 individuals with 583,085 SNPs. The phenotypes were standardised such that
the mean was 0 and variance was 1, for which we applied the liability threshold model to
generate affected or unaffected disease status for each individual, using various values for
the population prevalence (k = 0.025, 0.05, 0.1 or 0.5). Type I error rate at a significance
threshold of p-value < 0.05 was estimated from 500 replicates for each scenario and</li>
population prevalence.

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15 We also validated that there was no inflation for the type I error rate when applying GxEsum to binary (disease) traits (Table 2 and Supplementary Table 4), showing 16 that GxEsum appears to be robust to false positives in the scenarios of various 17 confounders. In addition, we estimated the variance component of GxE on the 18 19 observed scale and transformed to that on the liability scale, using Robertson 20 transformation [17]. As shown in Supplementary Figure 5, the transformed estimates were close to the true simulated values on the liability scale, although the precision 21 22 of estimates (represented as 95% CI) was shown to be decreased when the population prevalence approached an extreme (e.g. k=0.025). GxE estimates were 23 biased when simulating a large effect size of GxE (e.g. 10% of phenotypic variance 24 25 explained by GxE) in the case of k=0.025 (Supplementary Figure 6) although they 26 were mostly unbiased in the case of k=0.1 (Supplementary Figure 7). The level of biasedness appeared to be increased when there were RxE effects (Supplementary 27 Figure 6). Finally, caution should be given in interpreting GxE estimates when there 28 are large confounding effects such as substantial G-E and R-E correlations 29 30 (Supplementary Figure 8). The inflated GxE estimates were probably due to the fact that the phenotypes were over-adjusted for the environment in the model because of 31 32 the correlation between the main trait and environment (G-E and R-E correlations). 33 This resulted in a reduced phenotypic variance (Supplementary Figure 9), hence an

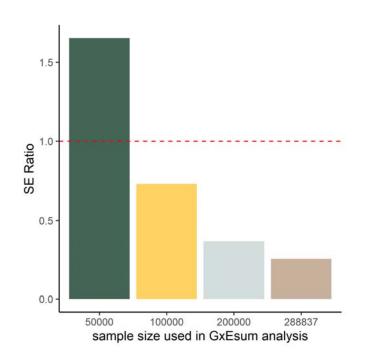
- 1 inflated GxE estimates that is the ratio of the estimated GxE variance to the
- 2 phenotypic variance.
- 3 Nevertheless, those confounders including RxE interaction and G-E/R-E correlations
- 4 would not produce false positives whether using continuous quantitative or binary
- 5 responses as shown above (also see Supplementary Tables 1 4). We additionally
- 6 tested if the type I error rate of GxEsum was controlled when there is collider bias,
- 7 which is a concern especially when using a self-report study (e.g. UK Biobank data)
- 8 [18]. In simulations with collider bias, although estimated SNP-heritability was
- 9 substantially (and unrealistically) underestimated (Supplementary Figures 10 and 11),
- the type I error rate of GxEsum was well controlled whether using continuous or
- binary responses (Supplementary Tables 5 and 6).
- 12 The estimated variance of the main genetic effects was mostly unbiased when using
- 13 binary disease traits without G-E/R-E correlations (Supplementary Figure 12). When
- there were significant G-E and /or R-E correlations, the estimated variance of the
- 15 main genetic effects appeared to be underestimated especially when there was RxE
- interaction (Supplementary Figure 13), which confirmed the fact that the main
- 17 genetic effects are over-adjusted for the environment due to correlations between
- the trait and environment (Supplementary Figure 9).
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# 20 Precision and Computational Efficiency

The precision was assessed by comparing the standard error (SE) of GxEsum and 21 RNM estimates. The SE of GxEsum was obtained from LDSC software (using a 22 jackknife method). The SE of RNM for GxE component can be obtained from the 23 information matrix [19] or from well-established theory [20] (see Supplementary 24 Table 7). Figure 1 shows that the SE of GxEsum was 1.65 times higher than that of 25 26 RNM when using the same sample size of 50,000. However, when sample size 27 increased for GxEsum up to 288,837, for which RNM estimation is infeasible, the ratio reduced to 0.2. GxEsum can use a larger sample size (e.g. > 1,000,000), for 28 which the ratio is expected to be further decreased, although the largest sample size 29 tested in this study was 288,837 (Supplementary Figure 14). 30 31 While the precision of GxEsum is competitive with that of RNM, the computational efficiency is dramatically different between two methods (Figure 2 and 32 33 supplementary Table 8). For example, when using a sample size of 50,000, the

- computing time for RNM was taken more than a thousand times than GxEsum. Even
- for GxEsum with a sample size of 288,837, its computational efficiency was still
- 36 substantially higher than RNM with a sample size of 50,000 (Supplementary Figure
- 14 and Supplementary Table 7). This justifies that GxEsum is a computationally
- <sup>38</sup> efficient tool that can be applied to biobank scale data for multiple complex traits and
- diseases. It is noted that we assumed that preliminary analyses for each method
- 40 were already done (e.g. GRM for RNM, and LD scores and GWAS for GxEsum)
- 41 (Supplementary Table 8).

- 1 GxEsum uses the Wald test to get a p-value for the null hypothesis, i.e. absence of
- 2 GxE interaction, using an estimated GxE variance and its standard error. Therefore,
- 3 the power of the method is closely related to the precision.



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2 Figure 1. The ratio of standard error (SE) from GxEsum to that from RNM using

3 **UK Biobank data.** The SEs of GxE variance estimated from GxEsum with various

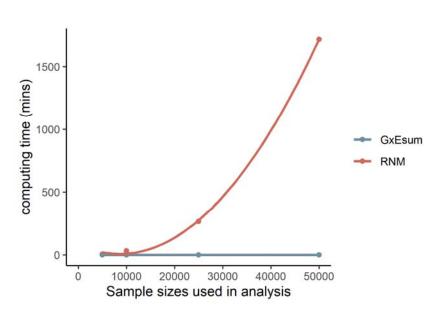
4 sample sizes ranging from 50,000 to 288,837 were obtained, and they were

5 compared to the SE of GxE variance estimated from RNM with a sample size of

- 50,000. The dashed horizontal line represents the ratio as 1.
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analyses. As the sample size increases, the computing time of RNM (red) increases

12 exponentially, while that of GxEsum (blue) is almost invariant (less than a minute).

#### 1 Real data analyses

2 We applied GxEsum to estimate genetic effects of body mass index (BMI) that were 3 modulated by an environment such as age, alcohol intake frequency, neuroticism 4 scores or physical activity. The significant GxE was observed from the analyses 5 using neuroticism scores. On the other hand, we did not find significant GxE when 6 using age, alcohol intake frequency and physical activity after Bonferroni correction (Bonferroni p-value = 0.05/10 = 0.005 since there were 10 significance tests in this 7 8 study) (Table 3). The GxEsum approach applied to a binary disease was conducted 9 using hypertension or type 2 diabetes as the main trait, and BMI, waist-hip ratio 10 (WHR). body fat percentage (BFP), or systolic/diastolic blood pressures (BP) as an environmental variable. Table 3 shows that the genetic effects of hypertension and 11 12 type 2 diabetes were significantly modulated by BMI, but not by other environmental variables. For a comparison, LDSC estimates (i.e. from the null model without GxE) 13 14 are also shown in Supplementary Table 9. 15 Because not all variables were without missing, we imputed missing phenotypes 16 using the mean value for each variable in the analyses, in order to maximise the sample size. In this real data analysis, there was no remarkable difference in the 17 18 results whether using phenotypic imputation or not although some variables improved their significance, e.g. NEU (Supplementary Tables 10 -12). It is noted that 19 20 our main phenotypes had a small proportion of missing values, i.e. 0.3%, 7.9% and 0.2% for BMI, hypertension and type 2 diabetes, respectively. If missing rate is 21 22 substantially high, we recommend to exclude missing values from the analysis, or a 23 better phenotypic imputation method [21] should be used. 24 25 26

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Main trait	Environmental variable	Main additive genetic variance ( $\sigma^2_{{\mathcal G}_0}$ )	GxE interaction variance ( $\sigma_{g_1}^2$ )	p-value for GxE
	Age	0.216 (0.007)	0.004 (0.002)	1.86E-02
BMI	NEU <sup>a</sup>	0.216 (0.007)	0.007 (0.002)	1.61E-05
DIVII	PA <sup>b</sup>	0.218 (0.007)	0.003 (0.001)	2.57E-02
	ALC <sup>c</sup>	0.216 (0.007)	0.003 (0.002)	5.98E-02
	BMI	0.152 (0.008)	0.006 (0.002)	2.09E-03
Hypertension	WHR <sup>d</sup>	0.154 (0.008)	0.005 (0.002)	3.21E-02
	BFP <sup>e</sup>	0.151 (0.008)	0.008 (0.003)	2.66E-02
	BMI	0.141 (0.014)	0.085 (0.022)	1.58E-04
Type 2 Diabetes	Diastolic BP <sup>f</sup>	0.198 (0.014)	-0.004 (0.006)	5.38E-01
	Systolic BP	0.204 (0.014)	-0.006 (0.006)	3.17E-01

#### 1 Table 3. Estimates obtained from GxEsum analysis using real data.

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3 We used a quantitative trait (BMI) and binary disease traits (hypertension and type 2 diabetes) because BMI is known to be

4 modulated by age/lifestyle such as NEU, ALC, PA [8, 22, 23], and hypertension and type 2 diabetes are known to be caused by

5 obese traits such as BMI and WHR [24, 25]. The p-value is from a Wald test for the estimated GxE variance not being different from

<sup>6</sup> zero. The estimates on the observed scale for the binary trait, hypertension, were transformed to those on the liability scale using

7 Robertson transformation[17, 26]. All estimates were from the GxEsum model.

- <sup>8</sup> <sup>a</sup>NEU: Neuroticism Score
- 9 <sup>b</sup>PA: Physical Activity
- 10 <sup>c</sup>ALC: Alcohol intake frequency
- <sup>11</sup> <sup>d</sup>WHR: Waist-Hip Ratio
- <sup>12</sup> <sup>e</sup>BFP: Body Fat Percentage
- <sup>13</sup> <sup>f</sup>BP: Blood pressure

### 1 **Discussion**

In this study, we propose GxEsum, a novel whole-genome GxE method, of which the 2 computational efficiency is a thousand times higher than existing methods. The 3 4 estimation of GxE using GWAS summary statistics has great flexibility in the 5 application of the method to multiple complex traits and diseases. The proposed 6 method and theory have been explicitly verified using comprehensive simulations that were carried out for both quantitative trait and binary disease. Moreover, we 7 8 showed that the type I error rate of the proposed method was not inflated by 9 moderate to severe collider bias [18] that caused a substantial underestimation of 10 heritability shown in our simulation (Supplementary Figures 10 and 11). In the real data analysis, we show that the genetic effects of BMI were significantly 11 12 modulated by NEU, which agrees with previous studies [9]. It is noted that the 13 significance of GxE was improved because we used a larger sample size, compared with the previous studies. Our result agrees with Robinson et al. (2017) who found 14 no significant GxE evidence for age when analysing BMI using the UK Biobank in 15 which the participants aged 40-69 at the recruitment. However, a dataset with a 16 wider range of ages is desirable, which would increase the power to detect GxE on 17 age. For example, a significant GxE was found in a BMI-age analysis using a dataset 18 including samples aged 18-80 at the recruitment [8]. For hypertension, its causal 19 20 relationship with BMI has been reported by a number of studies using Mendelian 21 randomization [24, 27]. However, it was not clear if the causal relationship is due to 22 GxE or something else, e.g. unknown non-genetic effects of the disease modulated by BMI status. We show that the causal relationship between hypertension and BMI. 23 and type 2 diabetes and BMI [28] reported in the previous studies [24, 27] may be 24 25 partly due to genome-wide GxE interaction effects. Interestingly, there is no significant evidence of genome-wide GxE for hypertension-WHR or hypertension-26 27 BFP causal relationship that was observed in Mendelian randomization studies [29, 30]. 28 The estimated intercept from GxEsum should be interpreted with caution. We show 29 that estimated intercepts were unbiased from the theoretically predicted values when 30 using the simulation of quantitative traits, as a proof of concept, i.e. the phenotypic 31 variance explained by RxE effects  $(h_{\tau_1}^2)$  can be obtained as  $h_{\tau_1}^2 = (intercept - 1 - 2h_{g_1}^2)$ 32 / 2 from eq. (4), or more generally,  $h_{\tau_1}^2 = (intercept - 1 - (k_{urtosis} - 1)h_{q_1}^2) / (k_{urtosis} - 1)$  from 33

eq. (5). However, in real data analyses, there may be additional confounding effects
 such as scale effects, residual heteroscedasticity or/and sample heterogeneity that
 are often attributed to unknown factors. Moreover, when using binary traits,

substantial scale effects can be generated (statistical RxE effects) because only
 affected and unaffected status are observed and individual differences within
 affected or unaffected group are ignored. These additional confounding effects and
 statistical scale effects are captured and estimated as an intercept in GxEsum [10],
 resulting in unreliable RxE estimates. It is noted that RxE estimation is not the main

interest of GxEsum and can be more reliably estimated in RNM that is designed to

43 model both GxE and RxE.

1 The existing GxE methods require individual-level genotype data which often has a restriction to share, and their computational burden is typically high. Moreover, it is 2 not clear how they perform when the representativeness of the samples is limited, 3 e.g. selection bias due to a collider in the UK Biobank samples. On the contrary, the 4 5 proposed approach, GxEsum, is computationally efficient and can detect GxE 6 interaction correctly for both quantitative and binary disease traits even when there is 7 moderate to server collider bias. If GWAS summary statistics of estimated main 8 additive and interaction effects can be made publicly available, a meta-analysis 9 across multiple cohorts can be possible for an ever-large GxE study (like the context 10 of LDSC SNP-heritability meta-analysis). There are some issues that the measure of environmental variable may not be standardised across study cohorts, and the 11 environmental variable may be even unavailable in some cohorts. However, these 12 issues can be remedied when the information of exposome that is the standardised 13 measure of all exposures for individuals, complemented to the genome, is available. 14 There is a GxE method that can use GWAS summary statistics, i.e. VarExp, which is 15 16 recently published. While VarExp benefits computationally from using GWAS summary statistics, it needs to invert the correlation matrix between SNPs, which 17 prevents from using a large number of SNPs [31]. Furthermore, the theoretical 18 frameworks of GxEsum and VarExp are fundamentally different in that the latter 19 20 does not account for confounding effects such as scale effects, residual heterogeneity or RxE that can be captured by the estimated intercept of GxEsum. 21 22 Finally, the performance of VarExp has been verified with a limited magnitude of 23 interaction effects up to 1.5% and 0.25% of the phenotypic variance for quantitative 24 and binary traits, respectively [31]. 25 Like RNM, GxEsum can fit environmental exposures such that the genetic effects of a trait can be modelled as a nonlinear function of a continuous environmental 26 27 gradient. The potential modifier of the genetic effects is not limited to environmental exposures but can be extended to novel variables from multi-omics data such as 28 gene-expression, protein expression and methylation data [32, 33]. Polygenic risk 29 scores [34, 35] can also be considered as an environmental variable in the model. 30 31 This novel approach may allow dissecting a latent biological architecture of a 32 complex trait in a future application of GxEsum.

In the analysis of binary disease traits, estimates on the liability scale, transformed 33 from those on the observed scale using Robertson transformation, should be 34 35 interpreted with caution. Biased estimates on the liability scale are likely due to the 36 violation of the normality assumption that is essentially required for the Robertson transformation, i.e. large interaction effects can cause a non-normal phenotypic 37 38 distribution. It is also known that if the transformation involves substantial non-39 additive effects, it can give biased estimates on the liability scale [17, 26, 36]. However, when non-additive effects are small, the transformation can give 40 reasonably accurate estimates on the liability scale, which is also evidenced by our 41 42 simulations with small interaction effects. As shown in the real data analysis, the magnitude of genome-wide GxE is not large (< 10% of the phenotypic variance), 43 showing that the bias of transformation due to the assumption violation may not be 44 45 substantial in general. Nevertheless, it is required to develop a better transformation 1 method for large interaction effects in a further study, e.g. when using multiple

- 2 environmental variables simultaneously, the interaction effects are aggregated and
- 3 can be substantially large.

There are a number of limitations in our study. First, like RNM, GxEsum does not 4 5 determine the causal direction between variables, which can be provided from 6 previous studies or other epidemiologic methods, e.g. Mendelian randomisation, as prior information. Second, we only modelled the first order of random regression 7 8 coefficients with a single environmental variable, and there may be significant 9 additional effects when modelling a higher-order interaction or multiple 10 environmental variables. It is possible to extend GxEsum model to fit additional quadratic and polynomial terms or multiple environmental variables simultaneously. 11 12 However, assessing the performance of these advanced models is a formidable task, requiring a further study. Third, the estimation for the main genetic effects can be 13 biased when there are large G-E and/or R-E correlations. Because of such 14 correlations, the main genetic effects are over-adjusted when the phenotypes of the 15 16 main trait are adjusted for the environmental variable in the model. Therefore, a careful interpretation of the estimated main genetic effects is required when using 17 GxEsum. Fourth, we did not investigate the performance of GxEsum for ascertained 18 case-control studies in which cases are over-sampled. A further study is required to 19 extend the method to non-random case-control samples so that it can be applied to 20 consortium data with multiple case-control studies. Lastly, when using the same 21 sample size, the precision of GxEsum is not better than GREML-based GxE 22 23 methods, implying that the former is only useful when using a large sample size that the latter cannot handle. 24

### 25 Conclusions

Despite these caveats, GxEsum can be a useful tool to estimate whole-genome GxE as it can achieve a higher precision (i.e. power) from a larger sample size, compared

to existing GxE methods. Especially when the scale of available resources increases,

29 GxEsum may be a unique method that can be applied to large-scale data across

30 multiple complex traits and diseases in the context of GxE.

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- 34 Methods
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# 36 GxEsum

37 Following Ni et al. (2019), RNM can be written as

### $y=b+g+\tau=b+g_0+g_1\times E+\tau_0+\tau_1\times E$

38 where y is N vector of phenotypic observations, **b** is a vector of fixed effects, **g** is N

individual genetic effects, which can be decomposed into the first and second order

- 1 of genetic random regression coefficients,  $g_0$  and  $g_1$ ,  $\tau$  is residual effects,
- 2 decomposed into the first and second order of residual random regression
- 3 coefficients,  $\tau_0$  and  $\tau_1$ , and E is an N vector of environmental variable. Note that E
- 4 can be also any covariate variable (e.g. smoking, alcohol intake frequency).
- 5 Assuming that the phenotypes (y) are pre-adjusted for the main genetic effects ( $g_0$ ),
- 6 environmental or covariate variable (E) and other fixed effects (b), the model can be
- 7 rewritten as

$$y = g_1 \times E + \tau_0 + \tau_1 \times E = X\beta_1 \times E + \tau_0 + \tau_1 \times E$$

- 8 where X is an  $N \times M$  standardised genotype matrix for M SNPs,  $\beta_1$  is an M vector of
- 9 SNP interaction effects modulated by the environment (i.e. GxE SNP effects). It is
- noted that  $\tau_0$  is residual effects that are consistent across environment whereas  $\tau_1$
- 11 captures heterogeneous residual effects across environment (i.e. RxE).
- Following Bulik-Sullivan et al. (2015), assuming  $\mathbb{E}[g_1] = \mathbb{E}[\beta_1] = 0$ , the expected chi-
- 13 square statistics of variant *j* for the GxE is

$$\mathbb{E}[\chi_i^2] = N \cdot \operatorname{Var}(\widehat{\beta_{1i}}) \qquad \qquad \text{eq. (1)}$$

14 Using the law of total variance,  $Var[\widehat{\beta_{1}}]$  can be obtained as

$$\operatorname{Var}(\widehat{\beta_{1_{j}}}) = \mathbb{E}\left[\operatorname{Var}(\widehat{\beta_{1_{j}}}|\mathbf{EX})\right] + \operatorname{Var}\left[\mathbb{E}(\widehat{\beta_{1_{j}}}|\mathbf{EX})\right]$$
$$= \mathbb{E}\left[\operatorname{Var}(\widehat{\beta_{1_{j}}}|\mathbf{EX})\right]$$

15

- where **EX** is an  $N \times M$  matrix with each column having the Hadamard product
- between **E** and  $X_j$  (standardised genotypes at the *j* th SNP) and the conditional
- 18 expectation of  $\widehat{\beta_{1j}}$  is  $\mathbb{E}(\widehat{\beta_{1j}}|\mathbf{EX}) = 0$ .
- 19 Noting that the least-square estimate of  $\widehat{\beta_{1j}}$  can be obtained as  $\widehat{\beta_{1j}} = (\mathbf{E}\mathbf{X}_j)'\mathbf{y}/N$ ,
- 20  $Var(\widehat{\beta_{1l}}|EX)$  can be rearranged as

21

$$Var(\widehat{\beta_{1j}}|\mathbf{EX}) = Var[(\mathbf{EX}_j)'\mathbf{y}/N|\mathbf{EX}]$$

$$= \frac{1}{N^2} Var[(\mathbf{EX}_j)'\mathbf{y}|\mathbf{EX}]$$

$$= \frac{1}{N^2} (\mathbf{EX}_j)' Var(\mathbf{y}|\mathbf{EX}) (\mathbf{EX}_j)$$

$$= \frac{1}{N^2} (\mathbf{EX}_j)' Var[(\mathbf{EX})\beta_1 + \tau_0 + \mathbf{E}\tau_1 |\mathbf{EX}] (\mathbf{EX}_j)$$

$$= \frac{1}{N^2} (\mathbf{EX}_j)' Var[(\mathbf{EX})\beta_1 |\mathbf{EX}] (\mathbf{EX}_j)$$

$$+ \frac{1}{N^2} (\mathbf{EX}_j)' (\mathbf{EX}_j) Var(\tau_0) + \frac{1}{N^2} (\mathbf{EX}_j)' (\mathbf{E}) (\mathbf{E})' (\mathbf{EX}_j) Var(\tau_1)$$

$$= \frac{1}{N^2} (\mathbf{E}\mathbf{X}_j)'(\mathbf{E}\mathbf{X}) (\mathbf{E}\mathbf{X})'(\mathbf{E}\mathbf{X}_j) \operatorname{Var}(\boldsymbol{\beta}_1 | \mathbf{E}\mathbf{X})$$
$$+ \frac{1}{N^2} [N \operatorname{Var}(\boldsymbol{\tau}_0) + (\mathbf{E}\mathbf{X}_j)'(\mathbf{E})(\mathbf{E})'(\mathbf{E}\mathbf{X}_j) \operatorname{Var}(\boldsymbol{\tau}_1)]$$
$$= \frac{1}{N^2} \frac{h_{g_1}^2}{M} (\mathbf{E}\mathbf{X}_j)'(\mathbf{E}\mathbf{X}) (\mathbf{E}\mathbf{X})'(\mathbf{E}\mathbf{X}_j)$$
$$+ \frac{1}{N^2} [N (1 - h_{g_1}^2 - h_{\tau_1}^2) + h_{\tau_1}^2 (\mathbf{E}\mathbf{X}_j)'(\mathbf{E})(\mathbf{E})'(\mathbf{E}\mathbf{X}_j)]$$

- 1 where  $h_{g_1}^2$  and  $h_{\tau_1}^2$  is the proportion of phenotypic variance explained by GxE and
- 2 RxE, respectively.

4

Therefore,  $\mathbb{E}[\chi_i^2]$  in eq. (1) can be written as

$$\mathbb{E}\left[\chi_{j}^{2}\right] = N \cdot \operatorname{Var}\left(\widehat{\beta_{1j}}|\mathbf{EX}\right)$$
$$= \frac{1}{N} \left[\frac{h_{g_{1}}^{2}}{M} \left(\mathbf{EX}_{j}\right)' \left(\mathbf{EX}\right)(\mathbf{EX})' \left(\mathbf{EX}_{j}\right) + N \left(1 - h_{g_{1}}^{2} - h_{\tau_{1}}^{2}\right) + h_{\tau_{1}}^{2} \left(\mathbf{EX}_{j}\right)' \left(\mathbf{EX}_{j}\right)\right] \quad \text{eq. (2)}$$

5 According to Bulik-Sullivan et al. (2015), the products of the standardised genotypes

6 at variant *j* and other variants can be expressed as a function of LD scores, i.e.

$$\frac{1}{N^2} (\mathbf{X}_j)'(\mathbf{X}) (\mathbf{X})'(\mathbf{X}_j) = \frac{1}{N^2} \left( N^2 + \left[ N * \left( 1 - \tilde{r}_j^2 \right) + \tilde{r}_j^2 * N^2 \right] * (M - 1) \right)$$
$$= \mathbf{1} + \left[ \frac{1 - \tilde{r}_j^2}{N} + \tilde{r}_j^2 \right] * (M - 1)$$
$$= \ell_j + \left[ \frac{(M - 1)(1 - \tilde{r}_j^2)}{N} \right]$$
$$\approx \ell_j + \frac{M - \ell_j}{N}$$

7 where  $\tilde{r}_i^2$  defined as the expected sample correlation between genotypes at the *j*th

variant and the other (*M*-1) variants, and  $\ell_j = 1 + \tilde{r}_j^2(M-1)$  is the LD scores of the *j*th SNP.

10 According to the central moment theory of standard normal distribution of three

- independent random variables ( $X_1$ ,  $X_2$  and E), each with an N vector, useful
- 12 equations are

$$\mathbb{E}[(\mathbf{X}_{1})'(\mathbf{X}_{1})] = N$$
$$\mathbb{E}[(\mathbf{X}_{1})'(\mathbf{X}_{2})(\mathbf{X}_{2})'(\mathbf{X}_{1})] = N$$
$$\mathbb{E}[(\mathbf{X}_{1})'(\mathbf{X}_{1})(\mathbf{X}_{1})'(\mathbf{X}_{1})] = N^{2}$$
$$\mathbb{E}[(\mathbf{E}\mathbf{X}_{1})'(\mathbf{E})(\mathbf{E})'(\mathbf{E}\mathbf{X}_{1})] = \mathbb{E}[(\mathbf{E}\mathbf{X}_{1})'(\mathbf{E}\mathbf{X}_{2})(\mathbf{E}\mathbf{X}_{2})'(\mathbf{E}\mathbf{X}_{1})] = 3N$$

1 and

$$\mathbb{E}[(\mathbf{E}\mathbf{X}_1)'(\mathbf{E}\mathbf{X}_1)(\mathbf{E}\mathbf{X}_1)'(\mathbf{E}\mathbf{X}_1)] = N^2.$$

2

- 3 Therefore, assuming that **E** and  $X_i$  have negligible correlation for a polygenic trait (i.e.
- 4 a tiny proportion of the phenotypic variance of E can be explained by a single SNP,
- 5  $X_i$ , the term  $(EX_i)'(EX)(EX)'(EX_i)$  can be expressed as a function of LD scores as

$$\frac{1}{N^2} (\mathbf{E} \mathbf{X}_j)' (\mathbf{E} \mathbf{X}) (\mathbf{E} \mathbf{X}_j) = \frac{1}{N^2} \left( N^2 + \left[ 3N \left( 1 - \tilde{r}_j^2 \right) + \tilde{r}_j^2 * N^2 \right] * (M - 1) \right)$$
$$= 1 + \left[ \frac{3(1 - \tilde{r}_j^2)}{N} + \tilde{r}_j^2 \right] * (M - 1)$$
$$= \ell_j + \frac{3(M - \ell_j)}{N}$$

6 Thus, a part in eq. (2) can be rearranged as

$$\frac{1}{N} \left[ \frac{h_{g_1}^2}{M} (\mathbf{E} \mathbf{X}_j)' (\mathbf{E} \mathbf{X}) (\mathbf{E} \mathbf{X})' (\mathbf{E} \mathbf{X}_j) + N(1 - h_{g_1}^2) \right] \\
= \frac{1}{N} \left[ \frac{N^2 h_{g_1}^2}{M} \left( \ell_j + \frac{3(M - \ell_j)}{N} \right) + N(1 - h_{g_1}^2) \right] \\
= \frac{N h_{g_1}^2}{M} \left( \ell_j + \frac{3(M - \ell_j)}{N} \right) + 1 - h_{g_1}^2 \\
= \frac{(N - 3) h_{g_1}^2}{M} \ell_j + 1 + 2 h_{g_1}^2 \\
= \frac{N(1 - 3/N) h_{g_1}^2}{M} \ell_j + 1 + 2 h_{g_1}^2 \\
= \frac{N h_{g_1}^2}{M} \ell_j + 1 + 2 h_{g_1}^2 \\
= \frac{N h_{g_1}^2}{M} \ell_j + 1 + 2 h_{g_1}^2 \\
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= \frac{N h_{g_1}^2}{M} \ell_j + 1 + 2 h_{g_1}^2 \\
= \frac{N h_{g_1}^2}{M} \ell_j + 1 + 2 h_{g_1}^2 \\
= \frac{N h_{g_1}^2}{M} \ell_j + 1 + 2 h_{g_1}^2 \\
= \frac{N h_{g$$

7

- 8 The term, 1 3/N, in eq. (3) can be approximated as 1 in the analysis using biobank
- 9 scale data, which contains over  $10^5$  samples.
- 10 The remaining part in eq. (2) can be rearranged as

$$\frac{1}{N} \left[ N \left( -h_{\tau_1}^2 \right) + h_{\tau_1}^2 (\mathbf{E} \mathbf{X}_j)' (\mathbf{E}) (\mathbf{E})' (\mathbf{E} \mathbf{X}_j) \right] = 2h_{\tau_1}^2$$

- where  $\mathbb{E}[(\mathbf{EX}_1)'(\mathbf{E})(\mathbf{E})'(\mathbf{EX}_1)] = 3N$  according to the central moment theory of
- 12 standard normal distribution (see above), assuming that E and each column of X
- have a negligible correlation, which satisfies if **E** is an environmental variable or a
- 14 polygenic trait.

1 Therefore,

2 
$$\mathbb{E}[\chi_j^2] = N \cdot \operatorname{Var}(\widehat{\beta_{1j}} | \mathbf{EX}) = \frac{N h_{g_1}^2}{M} \ell_j + 1 + 2h_{g_1}^2 + 2h_{\tau_1}^2$$
 eq. (4)

where  $1 + 2h_{g_1}^2 + 2h_{\tau_1}^2$  can be obtained as the intercept of the outcome by fitting to the proposed model (GxEsum). It is noted Eq. (4) is valid when  $X_j$  is not strictly normally distributed, i.e. the centred and standardised genotypes of jth SNP, which is already shown in Bulik-Sullivan et al. [10]. When the environmental variable (**E**) is non-normal, the general form of the fourth central moment term can be expressed as  $\mathbb{E}[(\mathbf{E}X_1)'(\mathbf{E})(\mathbf{E})'(\mathbf{E}X_1)] = k_{urtosis} N$  where  $k_{urtosis}$  is the kurtosis of **E.** And, only the intercept part of the Eq. (4) is slightly modified as

10 
$$\mathbb{E}[\chi_j^2] = N \cdot \operatorname{Var}(\widehat{\beta_{1j}} | \mathbf{EX}) = \frac{N h_{g_1}^2}{M} \ell_j + 1 + (k_{urtosis} - 1) h_{g_1}^2 + (k_{urtosis} - 1) h_{\tau_1}^2$$
 eq. (5)

11 Eq. (4) and (5) are verified using simulations (see Supplementary Note 3 and

12 Supplementary Table 2).

13 To validate the proposed model in general, we used comprehensive phenotypic

simulations that were based on real genotype data (see Supplementary Note 4).

# 15 Real data

UK Biobank data were used, which contains 0.5 million individuals aged between 40-16 17 69 years. The data consists of health-related information for each participant who was recruited in 2006-2010, and their imputed genomic data (~92 million SNPs) has 18 been distributed through European Genome-phenome Archive. A stringent quality 19 20 control process for individuals was set as followings: 1) who were reported as non-21 white British, 2) who were having mismatched gender between the reported and the inferred by the genotypic data, 3) who were having missing rate over 0.05, 4) who 22 were having putative sex chromosome aneuploidy. In addition, only HapMap3 SNPs 23 24 were used which were passed from the stringent quality controls for SNPs. The filter 25 for SNPs is set as followings: 1) which were having INFO score less than 0.6, 2) which were having a MAF less than 1%, 3) which were having Hardy-Weinberg 26 Equilibrium (HWE) P-value less than 1E-4, 4) one of which from the duplicated SNPs. 27 28 From those passing the tough procedures, we additionally excluded one of pair of 29 samples who were having the genomic relationship higher than 0.05. After quality 30 control, 288,837 individuals and 1,133,273 SNPs were remained. We estimated LD 31 scores using the genotypic data of UK Biobank after these quality control processes. 32 Among trait phenotypes available in the UK biobank, we arbitrarily selected BMI (a quantitative trait), hypertension and type 2 diabetes (binary disease traits) and tested 33 34 if the genetic effects of the complex traits were significantly modulated by an environmental variable, i.e. NEU, ALC, PA or age (for testing BMI), BMI, WHR or 35 36 BFP (for hypertension), and BMI, diastolic BP or systolic BP (for type 2 diabetes). The number cases for hypertension and type 2 diabetes was 134,499 (population 37 prevalence is 0.51) and 11,694 (population prevalence is 0.04), respectively. The 38 phenotypes of the main trait were adjusted for potential confounders such as age, 39 40 gender, year of birth, assessment centre, Townsend Deprivation Index, genetic batch,

- 1 household income, educational qualification, the first 10 principal components, and
- 2 the environmental variable. For any phenotypic missing value for each variable, we
- 3 used the mean of the phenotypes of the variable, i.e. phenotypic imputation with the
- 4 mean. A better phenotypic imputation method [21] can be used, which is likely to
- 5 improve the significance of GxE. Further details of the variables used on this study
- 6 are in Supplementary Note 4.
- 7 In GWAS, we used a linear model for quantitative traits as well as for binary
- 8 responses. The use of a linear model applied to binary responses is because it has
- 9 been reported that a logistic regression may generate biased estimates in some
- 10 instances [37] and our simulations (Supplementary Note 2) were based on a probit
- model (i.e. a linear transformation of the inverse standard normal distribution) that
- 12 can be well approximated by a linear model [38].
- 13

# 14 Abbreviations

- 15 GxE: genotype-by-environment interaction
- 16 RNM: reaction norm model
- 17 GWAS: genome-wide association studies
- 18 SNPs: single nucleotide polymorphisms
- 19 GREML: genomic restricted maximum likelihood
- 20 LDSC: linkage disequilibrium score regression
- 21 RxE: residual-environment interaction
- 22 G-E correlation: genotype-environment correlation
- 23 R-E correlation: residual-environment correlation
- 24 SE: standard error
- 25 BMI: body mass index
- 26 WHR: waist-hip ratio
- 27 BFP: body fat percentage
- 28 NEU: neuroticism score
- 29 PA: physical activity
- 30 ALC: alcohol intake frequency
- 31

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1

### 2 Authors' contribution

- 3 S.H.L. conceived the idea and directed the study. S.H.L. and J.S. derived and
- 4 verified the theory. J.S performed the analyses. J.S. and S.H.L. drafted the
- 5 manuscript.
- 6
- 7 Funding
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  9 160100229).
- 10 Availability of Data and Materials
- 11 Data:
- 12 The UK Biobank data are accessed via https://www.ukbiobank.ac.uk/
- 13 The ARIC study data are accessed via dbGaP (<u>https://dbgap.ncbi.nlm.nih.gov</u>) and
- 14 its accession code is phs000280.v7.p1.

### 15 Software:

- 16 GxEsum model is implemented in the script that are publicly available <u>at</u>
- 17 <u>https://github.com/honglee0707/GxEsum</u>, and the demonstration of GxEsum
- 18 software is described in Supplementary Note 5. The version of source code used in
- the manuscript is deposited with DOI: 10.5281/zenodo.4659681 at
- 20 https://zenodo.org/record/4659681#.YGkZXc9xeUk.
- 21 LDSC can be download from https://github.com/bulik/ldsc
- 22 PLINK version 1.9 can be download from <a href="https://www.cog-genomics.org/plink/1.9/">https://www.cog-genomics.org/plink/1.9/</a>
- 23 MTG2 version 2.15 can be download from
- 24 https://sites.google.com/site/honglee0707/mtg2
- 25 Ethics approval and consent to participant
- 26 The current study was approved by the University of South Australia Human
- 27 Research Ethics Committee. The ARIC Study was approved by the institutional
- review boards of all participating institutions, including the University of Minnesota,
- Johns Hopkins University, University of North Carolina, University of Mississippi
- 30 Medical Centre, and Wake Forest University. The UK Biobank was approved by the
- North West Multi-centre Research Ethics Committee (11/NW/0382). the reference
- number approved by the UK Biobank is 14575. All UK Biobank and ARIC Study
- 33 participants gave written informed consent.
- 34 Competing interests
- 35 The authors declare that they have no competing interests.

1					
2	References				
3	1.	Visscher PM, Brown MA, McCarthy MI, Yang J: Five years of GWAS discovery. Am J Hum			
4		Genet 2012, <b>90:</b> 7-24.			
5 6	2.	Sud A, Kinnersley B, Houlston RS: Genome-wide association studies of cancer: current insights and future perspectives. Nature Reviews Cancer 2017, 17:692-704.			
7	3.	Pasaniuc B, Price AL: Dissecting the genetics of complex traits using summary association			
8		statistics. Nature Reviews Genetics 2017, 18:117-127.			
9	4.	Yang J, Lee SH, Goddard ME, Visscher PM: GCTA: a tool for genome-wide complex trait			
10		<b>analysis.</b> Am J Hum Genet 2011, <b>88</b> :76-82.			
11	5.	Arnau-Soler A, Macdonald-Dunlop E, Adams MJ, Clarke T-K, MacIntyre DJ, Milburn K,			
12		Navrady L, Hayward C, McIntosh AM, Thomson PA, et al: Genome-wide by environment			
13		interaction studies of depressive symptoms and psychosocial stress in UK Biobank and			
14		Generation Scotland. Translational Psychiatry 2019, 9:14.			
15	6.	Gong J, Hutter CM, Newcomb PA, Ulrich CM, Bien SA, Campbell PT, Baron JA, Berndt SI,			
16		Bezieau S, Brenner H, et al: Genome-Wide Interaction Analyses between Genetic Variants			
17		and Alcohol Consumption and Smoking for Risk of Colorectal Cancer. PLoS Genet 2016,			
18	_	<b>12</b> :e1006296.			
19	7.	Manning AK, Hivert M-F, Scott RA, Grimsby JL, Bouatia-Naji N, Chen H, Rybin D, Liu C-T,			
20		Bielak LF, Prokopenko I, et al: A genome-wide approach accounting for body mass index			
21		identifies genetic variants influencing fasting glycemic traits and insulin resistance. <i>Nature</i>			
22	0	Genetics 2012, <b>44</b> :659-669.			
23	8.	Robinson MR, English G, Moser G, Lloyd-Jones LR, Triplett MA, Zhu Z, Nolte IM, van Vliet-			
24 25		Ostaptchouk JV, Snieder H, LifeLines Cohort S, et al: <b>Genotype-covariate interaction effects</b> and the heritability of adult body mass index. <i>Nat Genet</i> 2017, <b>49:</b> 1174-1181.			
25 26	9.	Ni G, van der Werf J, Zhou X, Hypponen E, Wray NR, Lee SH: Genotype-covariate correlation			
20	9.	and interaction disentangled by a whole-genome multivariate reaction norm model. Nat			
27		Commun 2019, <b>10:</b> 2239.			
28 29	10.	Bulik-Sullivan BK, Loh PR, Finucane HK, Ripke S, Yang J, Schizophrenia Working Group of the			
30	10.	Psychiatric Genomics C, Patterson N, Daly MJ, Price AL, Neale BM: LD Score regression			
31		distinguishes confounding from polygenicity in genome-wide association studies. <i>Nat</i>			
32		Genet 2015, <b>47</b> :291-295.			
33	11.	Finucane HK, Bulik-Sullivan B, Gusev A, Trynka G, Reshef Y, Loh PR, Anttila V, Xu H, Zang C,			
34		Farh K, et al. Partitioning heritability by functional annotation using genome-wide			
35		association summary statistics. Nat Genet 2015, 47:1228-1235.			
36	12.	Gazal S, Marquez-Luna C, Finucane HK, Price AL: Reconciling S-LDSC and LDAK functional			
37		enrichment estimates. Nat Genet 2019, 51:1202-1204			
38	13.	Hou K, Burch KS, Majumdar A, Shi H, Mancuso N, Wu Y, Sankararaman S, Pasaniuc B:			
39		Accurate estimation of SNP-heritability from biobank-scale data irrespective of genetic			
40		architecture. Nat Genet 2019, <b>51</b> :1244-1251.			
41	14.	Ni G, Moser G, Schizophrenia Working Group of the Psychiatric Genomics C, Wray NR, Lee			
42		SH: Estimation of Genetic Correlation via Linkage Disequilibrium Score Regression and			
43		Genomic Restricted Maximum Likelihood. Am J Hum Genet 2018, 102:1185-1194.			
44	15.	Rosner B: Fundamentals of biostatistics. Nelson Education; 2015.			
45	16.	Austin PC: Type I error rates, coverage of confidence intervals, and variance estimation in			
46		propensity-score matched analyses. Int J Biostat 2009, 5: Article 13.			
47	17.	Lee SH, Wray NR, Goddard ME, Visscher PM: Estimating missing heritability for disease			
48		from genome-wide association studies. American journal of human genetics 2011, 88:294-			
49		305.			

1	18.	Munafò MR, Tilling K, Taylor AE, Evans DM, Davey Smith G: Collider scope: when selection
2		bias can substantially influence observed associations. International Journal of
3		Epidemiology 2017, <b>47:</b> 226-235.
4	19.	Lynch M, Walsh B: Genetics and analysis of quantitative traits. Sinauer Sunderland, MA;
5		1998.
6	20.	Visscher PM, Hemani G, Vinkhuyzen AA, Chen GB, Lee SH, Wray NR, Goddard ME, Yang J:
7		Statistical power to detect genetic (co)variance of complex traits using SNP data in
8		unrelated samples. PLoS Genet 2014, 10:e1004269.
9	21.	Hormozdiari F, Kang Eun Y, Bilow M, Ben-David E, Vulpe C, McLachlan S, Lusis Aldons J, Han
10		B, Eskin E: Imputing Phenotypes for Genome-wide Association Studies. The American
11		Journal of Human Genetics 2016, <b>99</b> :89-103.
12	22.	Sutin AR, Ferrucci L, Zonderman AB, Terracciano A: Personality and obesity across the adult
13		life span. Journal of personality and social psychology 2011, 101:579-592.
14	23.	Rask-Andersen M, Karlsson T, Ek WE, Johansson Å: Gene-environment interaction study for
15		BMI reveals interactions between genetic factors and physical activity, alcohol
16		consumption and socioeconomic status. <i>PLoS genetics</i> 2017, <b>13</b> :e1006977-e1006977.
17	24.	Hyppönen E, Mulugeta A, Zhou A, Santhanakrishnan VK: A data-driven approach for
18		studying the role of body mass in multiple diseases: a phenome-wide registry-based case-
19		control study in the UK Biobank. The Lancet Digital Health 2019, 1:e116-e126.
20	25.	Lee M-R, Lim Y-H, Hong Y-C: Causal association of body mass index with hypertension using
21	201	a Mendelian randomization design. <i>Medicine</i> 2018, <b>97</b> :e11252-e11252.
22	26.	Dempster ER, Lerner IM: Heritability of Threshold Characters. Genetics 1950, <b>35</b> :212-236.
23	27.	Larsson SC, Bäck M, Rees JMB, Mason AM, Burgess S: <b>Body mass index and body</b>
24	27.	composition in relation to 14 cardiovascular conditions in UK Biobank: a Mendelian
25		randomization study. European heart journal 2020, 41:221-226.
26	28.	Morrison J, Knoblauch N, Marcus JH, Stephens M, He X: Mendelian randomization
27	20.	accounting for correlated and uncorrelated pleiotropic effects using genome-wide
28		summary statistics. Nature Genetics 2020, <b>52</b> :740-747.
29	29.	Si S, Tewara MA, Li Y, Li W, Chen X, Yuan T, Liu C, Li J, Wang B, Li H, et al: <b>Causal Pathways</b>
30	23.	from Body Components and Regional Fat to Extensive Metabolic Phenotypes: A Mendelian
31		Randomization Study. Obesity 2020, 28:1536-1549.
32	30.	Zanetti D, Tikkanen E, Gustafsson S, Priest James R, Burgess S, Ingelsson E: Birthweight, Type
33	50.	2 Diabetes Mellitus, and Cardiovascular Disease. Circulation: Genomic and Precision
34		Medicine 2018, 11:e002054.
35	31.	Laville V, Bentley AR, Privé F, Zhu X, Gauderman J, Winkler TW, Province M, Rao DC, Aschard
36	JT.	H: VarExp: estimating variance explained by genome-wide GxE summary statistics.
30 37		Bioinformatics 2018, <b>34:</b> 3412-3414.
38	32.	Zhou X, Im HK, Lee SH: CORE GREML for estimating covariance between random effects in
39	52.	linear mixed models for complex trait analyses. Nature Communications 2020, 11:4208.
39 40	33.	Zhou X, Lee SH: An integrative analysis of genomic and exposomic data for complex traits
40 41	55.	and phenotypic prediction. <i>bioRxiv</i> 2020:2020.2011.2009.373704.
41	34.	Khera AV, Chaffin M, Aragam KG, Haas ME, Roselli C, Choi SH, Natarajan P, Lander ES, Lubitz
42 43	54.	
		SA, Ellinor PT, Kathiresan S: Genome-wide polygenic scores for common diseases identify individuals with risk equivalent to monogenic mutations. Nature Genetics 2018, 50:1219-
44 45		1224.
45 4C	25	
46	35.	Truong B, Zhou X, Shin J, Li J, van der Werf JHJ, Le TD, Lee SH: Efficient polygenic risk scores
47 49		for biobank scale data by exploiting phenotypes from inferred relatives. <i>Nature</i>
48 40	26	Communications 2020, 11:3074.
49 50	36.	Van Vleck LD: Estimation of Heritability of Threshold Characters. Journal of Dairy Science
50		1972, <b>55</b> :218-225.

- Sun R, Carroll RJ, Christiani DC, Lin X: Testing for gene-environment interaction under
   exposure misspecification. *Biometrics* 2018, 74:653-662.
- 3 38. Lee SH, Goddard ME, Wray NR, Visscher PM: A Better Coefficient of Determination for
- 4 **Genetic Profile Analysis.** *Genetic Epidemiology* 2012, **36**:214-224.

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