Mechanistic model: Analysis of diffusion dynamics of Lugol's chromoendoscopy in Basal layer-type squamous cell carcinoma in situ via Euler's method and Law of mass action

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Abstract

Basal layer-type squamous cell carcinoma in situ (BLSCC) is an aggressive malignancy tumor. In the past, it usually went ignored because its aggressive biological behavior is different from typical esophageal squamous cancer (SCC). For our mechanistic model, we analyzed diffusion dynamics of iodine stain in BLSCC with the help of Euler's method. We used the law of mass action description of the forming process of the iodine-glycogen Complex. Based on the above analysis, our mechanistic model reveals that the efficacy of Lugol's chromoendoscopy is determined by the thickness of the squamous epithelial cell layer, which contains glycogen granules, and the convection of the interpupillary capillary loop (IPCL). A further inference can be made: the unique histological structure of BLSCC suggests Lugol's chromoendoscopy does not detect some components of it because these components neither break enough squamous epithelial cells which contain glycogen granules nor contain enough number of IPCL in a specific time frame. Besides, if our mechanistic model starting point is BLSCC and typical SCC share the same evolution path, we found both their cytoplasm tends to solid phase from the iodine diffusion dynamics analysis in "pink color sign."

Introduction

With the evolution of endoscopic technique, there has been a change in the stage distribution of esophageal cancer. The incidence rate of superficial esophageal cancer is increasing over the last two decades([Kanamoto, Yamaguchi et al. 2000](#), [Wang, Jiao et al. 2004](#)). According to recent studies, The risk of nodal metastases of early esophageal cancers (invading no deeper than SM1) is slower than beyond the depth of invasion SM1([Manner, Pech et al. 2013](#), [Cho, Choi et al. 2014](#)). Early esophageal cancer has high cure rates because of low lymph node metastasis rate([Funakawa, Uto et al. 2015](#)), so early esophageal cancer screening becomes more significant.

The distinction of early esophageal neoplastic changes from normal esophageal mucosa can be a difficult task for conventional endoscopy([Hashimoto, Iriya et al. 2005](#)). Chromoendoscopy with iodine staining has a higher sensitivity than conventional endoscopy([Dawsey, Fleischer et al. 1998](#), [Freitag, Barros et al. 1999](#)), so it becomes a good choice for detecting early neoplastic changes. It is well known that Iodine's esophageal mucosa absorption mechanism is passive diffusion([Ishihara, Kanzaki et al. 2013](#)). Common squamous epithelium stains dark brown (Figure A) because glycogen with iodine union inside cells can produce this colour. These molecules are held together by electrostatic forces([Moulay 2013](#)), so it is a reversible process. Yellower color, even pink color, is usually associated with Neoplastic cells because

there is no glycogen in these tumor cells([Ishihara, Kanzaki et al. 2013](#)) (Figure B). However, the new definition of High-grade dysplasia from WHO([Board 2019](#)) suggests that Chromendoscopy with iodine staining may be less effective than the past understandings of superficial esophageal cancer. The newest version features slight modification to the definition: High grade involves more than half of the epithelium and severe cytological atypia regardless of the extent of epithelial involvement. The latter implies that high-grade dysplasia is not more than half of the epithelium(Figure D) and brings many difficulties in its diagnose and treatment([Sarbia, Wolfer et al. 2015](#)). Japanese pathologists called it Basal layer-type squamous cell carcinoma in situ([Zhuang, Chen et al. 2019](#)) (BLSCC).compare with the conventional carcinogenesis way of typical SCC, BLSCC infiltrates directly to lamina propria and do not involve in the upper half of the epithelium. Chromoendoscopy with iodine staining may be more reliable than narrow-band imaging in detecting BLSCC because the latter is harder to detect irregularly shaped multiform lesions and absence of homogenization([Ishihara, Takeuchi et al. 2010](#), [Goda, Dobashi et al. 2015](#), [Zhuang, Chen et al. 2019](#)). However, Xiaoduan Zhuang et al. showed. Basal layer-type squamous cell carcinoma in situ had a higher recurrence rate([Zhuang, Chen et al. 2019](#)), so BLSCC's recurrence rate implied some limitations of Lugol's Chromendoscopy for detecting a demarcation line

between normal mucosa and cancerous lesion. More interesting, For BLSCC, scattered stained spots in Iodine unstained areas(Zhuang, Chen et al. 2019) suggested there exist two color patterns of Lugol's Chromendoscopy: yellow and brown-dark. The latter color is usually considered a normal mucous membrane in the past(Ishihara, Kanzaki et al. 2013). In short, there are two problems with Lugol's Iodine: 1. Do Lugol's Chromendoscopy have the ability to detect a demarcation line between normal mucosa and BLSCC? 2. Why does exist such a difference in Lugol's Iodine staining patterns in BLSCC? difficult diagnosis(Zhuang, Chen et al. 2019) may lead to statistical models based on data from endoscopic technique and pathology, even next-generation sequencing, do not fully answer the first problem; further, the quantification of data's randomness(Agresti and Franklin 2018) is not enough to explain the second problem and the mechanism hidden behind. Understanding the mechanism hidden behind it can help develop more effective diagnostic and therapeutic strategies; thus, our problems need to be explained differently: a mechanistic model based on the histological structure.

Model

Although the squamous epithelium is composed mainly of three cell layers(Mills 2012), each cell could be seen as a flat cell from morphological characteristics. We abstract the flat cell into a cube because the diffusion direction of Iodine is restricted in x,y, z-axis in 3D

dimensional space(Figure C). It is clear that the cube reduces the computational complexity of diffusion direction, so the nonkeratinizing, stratified squamous epithelium can be as simple as multilayer cubes(Figure C). We removed the cell nucleus and other organelles for the same principle because there is no relationship between them and iodine diffusion. As mentioned above, Basal layer-type squamous cell carcinoma in situ is High-grade dysplasia, restricted to the basal cell layer(Zhuang, Chen et al. 2019) (Figure D). In our model, we use a black cube for BLSCC(Figure E). Come back to our problems; we need to solve the demarcation line problem, so the key of our model is that tumor and normal tissues are joined in step base on the histology of BLSCC(Figure E). The molecule iodine diffuses to the glycogen interface forms an Iodine-glycogen complex(Ishihara, Kanzaki et al. 2013, Moulay 2013). To simplify our schematic diagram, we choose to ignore it and deduce the process by Law of mass action(Ferner and Aronson 2016)

Analysis and Result

Recent researches have shown that liquid-liquid phase separation does exist in the cytoplasm(Alberti, Gladfelter et al. 2019), and Macromolecular crowd is a common phenomenon inside the cell(Mourão, Hakim et al. 2014), it is evident that the viscous force exists in the natural fluid inside the cell. However, at the tissue level, the effect of it is almost imperceptible on Lugol's Chromendoscopy, more critical,

the inputs and outputs of Iodine are both passive diffusion, which suggests the free diffusion dynamic of Iodine has continuity characteristics, so we ignore the viscosity and make an approximation which describes “dry water”(Feynman, Leighton et al. 1963) rather than natural state inside the cell. According to Beer-Lambert law(Mayerhöfer, Pahlow et al. 2020) , we have

$$A_{\text{iodine}} = k_{\text{iodine}} \cdot l_{\text{esophagus}} \cdot C_{\text{complex}} \quad (1)$$

where A_{iodine} is the absorbance of normal esophageal mucosa after iodine staining; k_{iodine} is attenuation coefficient of normal esophageal mucosa after iodine staining; C_{complex} is the density of Iodine- glycogen complex; $l_{\text{esophagus}}$ is the length of esophageal epithelium which contain glycogen granules along the y-axis(note: let us first assume that C_{complex} is low concentration in our model).

A single cell’s model (cubic), suppose that the C_{complex} term mainly determine the color pattern. The Charge-transfer complex(Moulay 2013) means there is a chemical equilibrium between Iodine and glycogen:

where I is Iodine; G is glycogen; IG is Iodine- glycogen complex. (note: although Lugol iodine is a solution of iodine ions with Iodine, the organic reaction occurs only in the presence of a single iodine molecule. To simplify our complex reaction, we take Lugol iodine as a solution of Iodine in our model)

For a single cell (cubic), It is clear that G is constant and I is variable. Eq(1), k_{iodine} and $l_{\text{esophagus}}$ are fixed in a single cubic; logically, A_{iodine} is determined by the density of Iodine. The density of Iodine represents the state of every spatial point in iodine diffusion at some point, so Euler's method([Anderson and Wendt 1995](#)) is very suitable to use in our model.

It is well known that Iodine across the cell membrane by passive transport([Ishihara, Kanzaki et al. 2013](#)). the movement of Iodine usually across cytomembrane via facilitated diffusion mechanism([Nunez-Anita, Cajero-Juarez et al. 2011](#)) it is generally recognized that the thickness of the cell membrane is approximately 3nm([Van Meer, Voelker et al. 2008](#)), The volume of it takes fractional percentage point of the volume of the cell. Let us assume that number of iodine molecules is less than the transport protein on the cell membrane and Iodine continually diffuse into an infinitesimal fluid element. We can consider the transport cycle as an instantaneous state relative to the macro world to ignore the cytomembrane in the diffusion process of Iodine.

According to the oxygen diffusion mathematical model([Endeward 2012](#)), the rate of iodine concentration is appropriate for Fick's second law in the infinitesimal fluid element during the process of facilitated diffusion. Now we think of a single cell (cube) as an infinitesimal fluid element (iodines) (Figure C). For the x-axis, suppose that the

concentration gradient is $\frac{\partial C_{\text{iodine}}}{\partial X}$ at cubic's top edge; so we have:

$$J_{\text{top edge } -x} = -D \frac{\partial C_{\text{iodine}}}{\partial X} \quad (3)$$

where $J_{\text{top edge } -x}$ is the diffusion flux at the cubic top edge along the x-axis; D is diffusivity; C_{iodine} is the concentration of Iodine at cubic top edge; X is position, the dimension of x-axis; $-\frac{\partial C_{\text{iodine}}}{\partial X}$ is the concentration gradient of Iodine for one dimension diffusion at cubic top edge.

Then, let us assume that the concentration variation rate of our cubic is continuous, so we use the Taylor polynomial (Thomas, Weir et al. 2008) to approach the real function of the concentration gradient at the cubic bottom edge:

$$J_{\text{bottom edge } -x} = -D \left(\frac{\partial C_{\text{iodine}}}{\partial X} + \frac{\partial \left(\frac{\partial C_{\text{iodine}}}{\partial X} \right)}{\partial X} dx \dots \dots \dots \right) \quad (4)$$

where $J_{\text{bottom edge } -x}$ is the diffusion flux at cubic's bottom edge along the x-axis; $\frac{\partial \left(\frac{\partial C_{\text{iodine}}}{\partial X} \right)}{\partial X} dx$ is the second term of Taylor's expansion and equal to Fick's second law.

For tissue level, the width of the cube is infinitesimal, so we have

$$J_{\text{bottom edge } -x} \approx -D \left(\frac{\partial C_{\text{iodine}}}{\partial X} + \frac{\partial \left(\frac{\partial C_{\text{iodine}}}{\partial X} \right)}{\partial X} dx \right) \quad (5)$$

Then, according to mass conservation (Feynman, Leighton et al. 1963), the resultant diffusion flux at cube along the x-axis is

$$J_{\text{resultant } -x} = -D \frac{\partial C_{\text{iodine}}}{\partial X} dydz + D \left(\frac{\partial C_{\text{iodine}}}{\partial X} + \frac{\partial \left(\frac{\partial C_{\text{iodine}}}{\partial X} \right)}{\partial X} dx \right) dydz \quad (6)$$

$$= D \frac{\partial(\partial C_{\text{iodine}} / \partial X)}{\partial X} dx dy dz = D \frac{\partial^2 C_{\text{iodine}}}{\partial X^2} dx dy dz$$

where $J_{\text{resultant } -x}$ is the resultant diffusion flux at cubic along the x-axis.

Similarly, the resultant diffusion flux at cubic along y-axis and z-axis

are:

$$J_{\text{resultant } -y} = -D \frac{\partial C_{\text{iodine}}}{\partial Y} dx dz + D \left(\frac{\partial C_{\text{iodine}}}{\partial Y} + \frac{\partial(\partial C_{\text{iodine}} / \partial Y)}{\partial Y} dy \right) dx dz \quad (7)$$

$$= D \frac{\partial(\partial C_{\text{iodine}} / \partial Y)}{\partial Y} dx dy dz = D \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} dx dy dz$$

$$J_{\text{resultant } -z} = -D \frac{\partial C_{\text{iodine}}}{\partial Z} dy dz + D \left(\frac{\partial C_{\text{iodine}}}{\partial Z} + \frac{\partial(\partial C_{\text{iodine}} / \partial Z)}{\partial Z} dz \right) dx dy \quad (8)$$

$$= D \frac{\partial(\partial C_{\text{iodine}} / \partial Z)}{\partial Z} dx dy dz = D \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} dx dy dz$$

where $J_{\text{resultant } -y}$ and $J_{\text{resultant } -z}$ are the resultant diffusion flux at cubic along y-axis and z-axis, respectively.

Summing Eq(6),Eq(7) and Eq(8),we get

$$\begin{aligned} J_{\text{resultant}} &= J_{\text{resultant } -x} + J_{\text{resultant } -y} + J_{\text{resultant } -z} \\ &= D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz \end{aligned} \quad (9)$$

where $J_{\text{resultant}}$ is the resultant diffusion flux at cubic in the ideal state.

Eq(9) shows a total disregard for an organic reaction between Iodine and glycogen(Moulay 2013), so we write Eq(9) as:

$$\begin{aligned} J_{\text{resultant } -IG} &= J_{\text{resultant}} + \delta \\ &= D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz + \delta \end{aligned} \quad (10)$$

where δ impacts the organic reaction between Iodine and glycogen

resultant diffusion flux at cubic. $J_{\text{resultant IG}}$ is the resultant diffusion flux at cubic involves the organic reaction between Iodine and glycogen.

Now consider how the organic reaction takes effect on $J_{\text{resultant IG}}$. According to Eq(2), there are only two states of Iodine in our model: iodine molecule and Iodine- glycogen complex. For the total concentration of Iodine in our model:

$$C_T = C_{\text{iodine } -s} + C_{\text{complex } -s} \quad (11)$$

Where C_T is the total concentration of iodine molecule and Iodine- glycogen complex at single cube. $C_{\text{iodine } -s}$ is the concentration of iodine molecules at a single cube. $C_{\text{complex } -s}$ is the concentration of Iodine- glycogen complex at a single cube.

According to the Brownian movement theory([Feynman, Leighton et al. 1963](#)), the iodine-glycogen Complex comes from a random collision between Iodine and glycogen. Law of mass action([Ferner and Aronson 2016](#)) can be used to describe the process:

$$[IG] = k_{\text{on}} C_{\text{iodine } -s} \cdot C_{\text{gly}} \quad (12)$$

where $[IG]$ is the formation rate of Iodine- glycogen complex; C_{gly} is the concentration of unconjugated glycogen at a single cubic; k_{on} is the collision rate between Iodine and glycogen(note: it means how many collision events are happening per single Iodine molecular per second, when the total concentration of glycogen is constant).

Similarly, k_{off} represents the dissociate rate of Iodine- glycogen

complex. Normally, the formation heat of the Complex is -40kj/mol(Moulay 2013), so k_{off} is a positive constant. Base on the processes of dissociating and collision, we have:

$$\frac{dC_{\text{complex}-s}}{dt} = k_{\text{on}} C_{\text{iodine}-s} \cdot C_{\text{gly}} - k_{\text{off}} \cdot C_{\text{complex}-s} \quad (13)$$

Eq(13) is finally close to the static equilibrium. For chemical equilibrium, we have:

$$\frac{dC_{\text{complex}-s}}{dt} = 0 \quad (14)$$

Using Eq(13) with Eq(14), we get:

$$k_{\text{on}} C_{\text{iodine}-s} \cdot C_{\text{gly}} = k_{\text{off}} \cdot C_{\text{complex}-s} \quad (15)$$

The definition of k_{on} tells us k_{on} is not a constant because C_{gly} is variable during the diffusion process of Iodine. From the point of view of statistics, there is positive relativity between two variables base on collision probability.

If we combine Eq(15) with Eq(11), we get:

$$C_T = C_{\text{iodine}-s} + \frac{k_{\text{on}} C_{\text{iodine}-s} \cdot C_{\text{gly}}}{k_{\text{off}}} \quad (16)$$

So we can say that for C_{iodine} :

$$C_{\text{iodine}-s} = \frac{C_T}{1 + \frac{k_{\text{on}}}{k_{\text{off}}} C_{\text{gly}}} \quad (17)$$

Before we discuss the dynamics of Eq(18), we need to know: if C_T approach $+\infty$, does the organic reaction between Iodine and glycogen always keep chemical equilibrium?

We can explain the problem above with the help of proof of contraposition(Rosen 2011). If C_T approach $+\infty$, suppose that the

chemical equilibrium is broken($\frac{dC_{\text{complex}}}{dt} \neq 0$). The infinite value of C_{complex} suggest all glycogen react with Iodine, so we get:

$$C_{\text{gly}} = 0 \Rightarrow k_{\text{on}} C_{\text{iodine}} \cdot C_{\text{gly}} = 0 \quad (18)$$

So we write Eq(13) as:

$$\frac{dC_{\text{complex}}}{dt} = -k_{\text{off}} \cdot C_{\text{complex}} \quad (19)$$

By integrating both sides of Eq(19):

$$\int \frac{dC_{\text{complex}}}{dt} = - \int k_{\text{off}} \cdot C_{\text{complex}} \quad (20)$$

So we obtain:

$$C_{\text{complex}} = -\frac{k_{\text{off}}}{2} C_{\text{complex}}^2 + A \quad (21)$$

where A is Constant of integration.

Let all iodine molecules at the top edge of cubic in our model, we have:

$$C_{\text{complex}} = 0 \Rightarrow A = 0 \quad (22)$$

So that Eq(21) becomes:

$$C_{\text{complex}} = -\frac{k_{\text{off}}}{2} C_{\text{complex}}^2 \quad (23)$$

Substituting the equation in Eq(11), we find that:

$$C_T = C_{\text{iodine}} - \frac{k_{\text{off}}}{2} C_{\text{complex}}^2 \quad (24)$$

$\frac{k_{\text{off}}}{2} C_{\text{complex}}^2 > 0$, Eq(24) means:

$$C_T < C_{\text{iodine}} \quad (25)$$

However, according to Eq(11), we have:

$$C_T > C_{\text{iodine}} \quad (26)$$

These two equations are mutually incompatible. Indeed, the

hypothesis “if C_T approach $+\infty$, the organic reaction between iodine and glycogen do not keep chemical equilibrium” is false. So “the organic reaction always keeps chemical equilibrium” is automatically true.

Let us assume that the total concentration of glycogen is constant, so we get:

$$0 < C_{\text{gly}} < M \quad (27)$$

where M is the constant(the total concentration of glycogen before the chemical reaction occurs).

Eq(2) tell us:

$$\lim C_{\text{gly}} = 0 \Leftrightarrow \lim C_{\text{complex } -s} = M \quad (28)$$

Let us assume that $C_{\text{complex } -s}$ approach M after the color of the esophageal mucosa turns into brown-dark. Besides, According to the definition of k_{on} , k_{on} is determined by the value of C_{gly} , which means both of them to have the same monotonicity, so we get:

$$\lim C_{\text{complex } -s} = M \Rightarrow \lim k_{\text{on}} \cdot C_{\text{gly}} = 0 \quad (29)$$

Therefore, we can rewrite Eq(17) as:

$$C_{\text{iodine } -s} = \frac{C_T}{1 + \frac{k_{\text{on}}}{k_{\text{off}}} C_{\text{gly}}} \approx C_T \quad (30)$$

According to the definition of resultant diffusion flux, we get:

$$\frac{dC_{\text{iodine } -s}}{dt} dx dy dz = J_{\text{resultant}} \quad (31)$$

$$\frac{dC_T}{dt} dx dy dz = J_{\text{resultant } -IG} \quad (32)$$

Therefore, differentiate both side of Eq(30) and multiply by $dx dy dz$:

$$J_{\text{resultant -IG}} \approx J_{\text{resultant}} \\ \approx D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz \quad (33)$$

The equation says that for $C_{\text{complex -s}}$ approach M the term δ is equal to zero, so we neglect all effects of the organic reaction. Let us return our esophageal tissue. Gauss's theorem([Feynman, Leighton et al. 1963](#)) tell us that the total resultant diffusion flux from an iodine-stain area is equal to the sum of the fluxes out of each cell(cube) because each cubic is an infinitesimal fluid element(Figure E), so we form the sum:

$$J_{\text{resultant -IGS}} = \sum_n D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz \quad (34)$$

Where n is the number of cubes.

The diffusion is a continuous process, so:

$$J_{\text{resultant -IGS}} = \iiint D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz \quad (35)$$

For some researchers' view([Peng, Li et al. 2020](#)), High-frequency mutation genes encoding epigenetic modification suggest liquid-liquid phase separation may be present in the occurrence or progression of esophageal cancer. Liquid-liquid phase separation can convert into a solid-like state in the pathological state([Dogra, Joshi et al. 2019](#)).it is possible that Iodine cannot diffuse into these tumor cells because their cytoplasm tends to a solid phase. It is not easy to conclude without enough evidence, so we need to prove it with the help of some mathematical logic. Let us first assume that the tumor cell's cytoplasm

tends to the solid phase.

According to Lennard-Jones potential (Israelachvili 2011), the attractive force is dominated in the solid phase, making it difficult to break these molecules' bonds. When Iodine tried to diffuse into the tumor cell, the concentration gradient will disappear in Y-axis, so we find:

$$\frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} \approx 0 \quad (36)$$

Suppose that we imagine for a moment that Iodine diffuse into the standard epithelial layer above BLSCC (Figure E). When these iodine molecules touch these tumor cells, we have its resultant diffusion flux :

$$J_1 = \iiint D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz \quad (37)$$

where J_1 is the resultant diffusion flux of Iodine which diffuses into the standard epithelial layer above BLSCC.

Meanwhile, some iodine molecules diffuse into the standard epithelial layer without BLSCC, so we have its resultant diffusion flux:

$$J_2 = \iiint D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz \quad (38)$$

where J_2 the resultant diffusion flux of Iodine which diffuses into the standard epithelial layer without BLSCC.

Eq(36) means:

$$\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} > \frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \quad (39)$$

According to the domination property of triple integrals(Thomas, Weir et al. 2008), we have:

$$J_2 > J_1 \quad (40)$$

Use Eq(32) and the definition of average value a function in space, we have:

$$\frac{dC_2}{dt} > \frac{dC_1}{dt}, [t_1, t_2] \quad (41)$$

where C_1 is the concentration of Iodine, which diffuses into the normal epithelial layer above BLSCC; C_2 is the Iodine concentration, which diffuses into the normal epithelial layer without BLSCC. $[t_1, t_2]$ is the diffusion of Iodine for a certain period.

Similar, definite integrals also have domination property, so:

$$C_2 = \int_{t_1}^{t_2} \frac{dC_2}{dt} > C_1 = \int_{t_1}^{t_2} \frac{dC_1}{dt} \quad (42)$$

Eq(15) tell us $C_{\text{iodine} -s}$ is positively associated with $C_{\text{complex} -s}$, so Eq(42) means:

$$C_{\text{complex} -s2} > C_{\text{complex} -s1} \quad (43)$$

where $C_{\text{complex} -s2}$ is the concentration of Iodine- glycogen complex without BLSCC; $C_{\text{complex} -s1}$ is the Iodine concentration-glycogen Complex above BLSCC.

Let $C_{\text{complex} -s}$ approach M, so $C_{\text{iodine} -s}$ tend to $+\infty$ base on Eq(15). Usually, Lugol's solution needs to spray enough Iodine through a spray catheter, compare with the large value of $C_{\text{iodine} -s}$. $C_{\text{complex} -s}$ is

in low concentration so that we can use Beer-Lambert law safely in our model.

According to Eq(1), it is logical that the efficacy of Lugol's staining is both determined by $I_{\text{esophagus}}$ and C_{complex} . However, the second law of thermodynamics tells us Iodine tends to the highest entropy(uncertainty is largest), so Iodine will have the same concentration at the end. In short, it seems $I_{\text{esophagus}}$ only dominates the efficacy of Lugol's staining. If $C_{\text{complex}} \rightarrow 0$ do not approach M , we also come to the same conclusion.

Can we answer our questions in the current steps? The answer is no. Squamous dysplasia is usually accompanied by dilation and elongation of the interpupillary capillary loop(IPCL)([Kumagai, Toi et al. 2010](#), [Oyama, Inoue et al. 2017](#)). That brings us to another variable we need to consider: the fluid dynamics characteristics of Iodine in IPCL. Compare with the iodine diffusion of cells, and we need to add convective fluxes for IPCL.

Letting $C_{\text{iodine}} \mu$ be the convective fluxes at an infinitesimal fluid element's top edge along the x-axis in IPCL and $C_{\text{iodine}} \mu + \frac{\partial C_{\text{iodine}}}{\partial x} \mu dx$ be the convective fluxes at an infinitesimal fluid element's bottom edge along x-axis base on Taylor polynomial, according to mass conservation, we write:

$$C_{\text{iodine}} \mu dydz - (C_{\text{iodine}} \mu + \frac{\partial C_{\text{iodine}}}{\partial x} \mu dx) dydz = - \frac{\partial C_{\text{iodine}}}{\partial x} \mu dx dydz \quad (44)$$

where $-\frac{\partial C_{\text{iodine}}}{\partial x} \mu dx dy dz$ is the net convective fluxes of Iodine at an infinitesimal fluid element along the x-axis for IPCL. Similarly, for the y-axis and z-axis, we write:

$$C_{\text{iodine}} v dx dz - (C_{\text{iodine}} v + \frac{\partial C_{\text{iodine}}}{\partial y} dy) dx dz = -\frac{\partial C_{\text{iodine}}}{\partial y} v dx dy dz \quad (45)$$

$$C_{\text{iodine}} \omega dx dy - (C_{\text{iodine}} \omega + \frac{\partial C_{\text{iodine}}}{\partial z} dz) dx dy = -\frac{\partial C_{\text{iodine}}}{\partial z} \omega dx dy dz \quad (46)$$

where $C_{\text{iodine}} v$ and $C_{\text{iodine}} \omega$ are both the convective fluxes at an infinitesimal fluid element's right and left edge along y-axis and z-axis in IPCL

For an infinitesimal fluid element of IPCL, the concentration variation rate of Iodine is equal to the sum of convection fluxes and diffusion fluxes, therefore:

$$\frac{\partial C_{\text{iodine}}}{\partial t} dx dy dz = \left(-\frac{\partial C_{\text{iodine}}}{\partial x} \mu - \frac{\partial C_{\text{iodine}}}{\partial y} v - \frac{\partial C_{\text{iodine}}}{\partial z} \omega + \frac{\partial^2 C_{\text{iodine}}}{\partial x^2} \right. \\ \left. \frac{\partial^2 C_{\text{iodine}}}{\partial y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial z^2} \right) dx dy dz \quad (47)$$

From Eq(33), we know at once:

$$J_{\text{resultant}} > J_{\text{IPCL}} \quad (48)$$

where J_{IPCL} is the concentration variation rate of Iodine at an infinitesimal fluid element of IPCL.

For the same volume, we use the domination property of triple integrals again; we have:

$$\iiint J_{\text{resultant}} > \iiint J_{\text{IPCL}} \quad (49)$$

According to the definition of average value a function in space(Thomas, Weir et al. 2008), we get:

$$\frac{1}{D} \iiint J_{\text{resultant}} > \frac{1}{D} \iiint J_{\text{IPCL}} \quad (50)$$

where D is the same volume of iodine diffusion area in both cells (cubic) and IPCL.

Therefore:

$$\frac{dC_{\text{resultant}}}{dt} > \frac{dC_{\text{IPCL}}}{dt}, [t_1, t_2] \quad (51)$$

where $C_{\text{resultant}}$ is the concentration of iodine in cells; C_{IPCL} is the concentration of iodine in ICPL.

According to the domination property of definite integrals:

$$C_{\text{resultant}} > C_{\text{IPCL}}, [t_1, t_2] \quad (52)$$

Owing to convective fluxes always exist in a blood vessel, it is clear that " $C_{\text{resultant}} > C_{\text{IPCL}}$ " does not disappear until all iodine molecules are absorbed into the bloodstream. Unlike the iodine diffusion among cells, the diffusion from cells to IPCL always exists during the operational process of Lugol's Chromoendoscopy. In short, our two questions can be answered by two factors: the thickness of the squamous epithelial cell layer, which contains glycogen granules, and the number of IPCL. In other words, if BLSCC has enough glycogen granules and fewer IPCL, Lugol's Chromendoscopy does not work. The two factors are consistent with endoscopic characteristics ([Zhuang, Chen et al. 2019](#)) and histology structure in BLSCC.

Suppose that the tumor cell's cytoplasm always keeps liquid phase. According to the clinical observation data show that BLSCC is a common

accompaniment to typical squamous cell carcinoma (SCC)([Zhuang, Chen et al. 2019](#)), so, logically, both of them have the same physical characteristics in the hypothesis, and Iodine can diffuse into these cells' cytoplasm.

Now let us consider the "pink color sign" in squamous cell dysplasia. According to Ishihara et al.'s theory([Ishihara, Kanzaki et al. 2013](#)), "pink color sign" is iodine leak into the esophageal lumen first because of lack of the keratin layer. However, under such assumption, a concentration gradient between the area that is the pink color sign(high-grade dysplasia involves the whole epithelium layer)and its peripheral area(dysplasia do not involve the whole epithelium layer) base on the second law of thermodynamics. When the iodine molecules from the area that are a pink color sign leak into the esophageal lumen first, the iodine molecules of the peripheral area continue to spread the area that is a pink color sign because of the driving force from the concentration iodine gradient. That can lead to two situations: 1. The "pink color sign" is a looping structure; its middle always keeps yellow color. 2. It is impossible to keep a static demarcation line between the area that is a pink color sign and its peripheral area during the whole diffusion process. It is a dynamic changing process. The deduction versus its actual endoscopic characteristics provides a conflicting result. Consequently, the assumption is false. If iodine leaks into IPCL first, we come to the

same conclusion.

Let us come back to our first hypothesis: the tumor cell's cytoplasm tends to a solid phase. Suppose that the number of iodine molecules maintains constant in iodine unstained and stained lesions. For infinitesimal fluid element on the surface of mucosa with the pink color sign, we have:

$$J_{\text{pink}} = \iiint D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz \quad (53)$$

where J_{pink} is the resultant diffusion flux of iodine on the surface of mucosa with the pink color sign.

For infinitesimal fluid element on the surface of mucosa without the pink color sign, the assumption above tell us the diffusion flux has not existed at the infinitesimal fluid element top edge along the y-axis, so we have

$$J_n = \iiint D \left(\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} - \frac{\partial C_{\text{iodine}}}{\partial Y} - \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \right) dx dy dz \quad (54)$$

where J_n the resultant diffusion flux of iodine on the surface of mucosa without the pink color sign.

Obviously

$$\frac{\partial^2 C_{\text{iodine}}}{\partial X^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} > \frac{\partial^2 C_{\text{iodine}}}{\partial X^2} - \frac{\partial C_{\text{iodine}}}{\partial Y} - \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2} + \frac{\partial^2 C_{\text{iodine}}}{\partial Z^2} \quad (55)$$

Therefore:

$$J_{\text{pink}} > J_n \quad (56)$$

We use the definition of average value a function in space and the domination property of definite integrals again, we have:

$$C_{\text{pink}} > C_n, [t_1, t_2] \quad (57)$$

where C_{pink} is the concentration of Iodine on the surface of mucosa with the pink color sign; C_n is the concentration of Iodine on the surface of mucosa without the pink color sign.

According to the second law of thermodynamics, it is clear that Iodine moves from the surface of mucosa with a "pink color sign" to the surface of mucosa without the pink color sign. Further, the " $-\frac{\partial C_{\text{iodine}}}{\partial Y} - \frac{\partial^2 C_{\text{iodine}}}{\partial Y^2}$ " term of Eq(54) tells us iodine molecules continue to leak into the epithelial layer. High-grade intraepithelial neoplasia is usually accompanied by expansion, distortion pipe diameter of IPCL ([Kumagai, Toi et al. 2010](#)), so the convection fluxes can accelerate the process base on Eq(52). From the point of view of histology, IPCL does not interfere with the diffusion of Iodine on the mucosal surface because it cannot extend to the top mucosal surface. In conclusion, the normal esophagus epithelium layer continues to absorb iodine molecules on the mucosal surface, leading to a shallow concentration of Iodine on the mucosal surface. When the upper half of epithelium is replaced by neoplastic cells in a certain area, a "pink color sign" can happen because only a few iodine molecules remained in its area. Our model hypothesizes that "the tumor cell's cytoplasm tends to solid phase" is true.

Suppose that number of iodine molecules is not less than the transport protein on the cell membrane. It is clear that $J_{\text{top edge} -x}$ is

invariable, and the concentration of iodine molecules is saturation on the top edge of the cell membrane; however, Eq(3) and Eq(4) tell us:

$$J_{\text{top edge} -x} > J_{\text{bottom edge} -x} \quad (58)$$

It suggests the number of iodine molecules is less than the transport protein on the bottom edge of the cell membrane. Hence, the derivation process is the same as the previously assumed condition after Iodine diffuses into the mucosal layer.

Discussion

From the fractal dimension point of view([Grizzi, Russo et al. 2005](#)), the tumor is an actual three-dimensional structure, and tumor-associated angiogenesis is on the non-integer dimensions (it is between 2D and 3D). Non-integer dimensions mean the rate of tumor angiogenesis is less than the tumor growth rate. As the tumor overgrows, the energy available per cell will be less and less. Although the Warburg effect ([Basan, Hui et al. 2015](#)) may be a solution from the angle of cost-benefit analysis, reprogramming energy metabolism is not enough to solve the conflict between the overgrowth of cancer cells and energy requirement. This conflict inevitably leads to a substantial morphological change of blood vasculature: tortuous, irregular branched and circumferential enlarged et al([Farnsworth, Lackmann et al. 2014](#)), so It is not strange that the degree of micro-vascular irregularity is associated with the invasion depth of superficial squamous cell

carcinoma(Oyama, Inoue et al. 2017). the nutrients and oxygen first move into the extra-vascular tissue by the flow of blood(convection) and then diffuse into the tumor tissue with the help of a concentration gradient(Baish, Gazit et al. 1996). For- dimensional diffusion in a plane, the maximum distance of oxygen diffusion is 100um(Secomb, Hsu et al. 1993, Baish, Gazit et al. 1996)(note: the actual thickness of epithelium is at least greater than 200um)(Vieth, Mastracci et al. 2016). Warburg effect means glucose is the principal metabolic fuel of cancer cells, so the maximum distance of glucose diffusion is significant for the energy requirement of cancer cells.

Compare with oxygen's simple diffusion, Eq(58) tells us the maximum distance of glucose's facilitated diffusion is minor than 100um because the number of membrane proteins limits its concentration gradient. Come back to the histological structure of Basal layer-type squamous cell carcinoma in situ; the lamina propria usually contains many vessels (Mills 2012). The basement membrane has many pore(Lv, Chen et al. 2014), so these histological characteristics mean glucose can diffuse into the epithelium through the basement membrane without the help of the intercapillary capillary loop(note: the maximum distance of glucose is facilitated diffusion may be further lessened by porous medium). When the distance from the basement membrane to the cancer cell is less than the maximum distance of glucose diffusion, it is logical that

tumor-associated angiogenesis is unnecessary at that distance. For BLSCC, the histological characteristics suggest that many parts of it are located within the maximum distance of glucose diffusion. These components contain a fewer number of interpupillary capillary loops. However, it is essential to note that tumor-associated angiogenesis depends on the maximum distance of glucose diffusion and the glycolysis rate of tumor cell(Chen, Yi et al. 2021). A histological perspective means tumor-associated angiogenesis also depends on the degree of cytological atypia(Figure D). In brief, the essential prerequisite for tumor-associated angiogenesis is:

$$V_{\text{gly}} > V_{\text{diffusion}} \quad (59)$$

where V_{gly} is the glycolysis rate of tumor cells, $V_{\text{diffusion}}$ is the glucose rate that diffuses into the tumor cell from lamina propria.

According to Eq(1) and Eq(2), the distance of glucose diffusion and the concentration of glucose present negative relativity, so Eq(59) tells us tumor-associated angiogenesis is the integration effect between the distance of glucose diffusion and the glycolysis rate of tumor cell. When the glycolysis rate is faster, the degree of cytological atypia is more prominent, and tumor cell without IPCL is closer to the basement membrane. Metabolomics study(Chen, Yi et al. 2021) suggests the increased glycolysis rate of tumor cells is a gradual process, so it means the growth of tumor cells without IPCL exists in the specific time frame.

Compared with the evolution of typical SCC, BLSCC has fewer IPCL in the specific time frame.

Moreover, These BLSCC components usually locate more close to the basement membrane to replace enough cells containing glycogen. To detect BLSCC, the sensitivity of Lugol's staining may be finally determined by the maximum distance of glucose diffusion and the degree of cytological atypia. When IPCLs are few on this condition, some components of BLSCC also may be able to escape the detection of Narrow-band imaging with magnifying endoscopy.

Similarly, low-grade squamous intraepithelial neoplasia/dysplasia (LGIN) (Board 2019) maybe not also be detected by Lugol's chromoendoscopy and Narrow-band imaging with magnifying endoscopy on the same condition. Compare with BLSCC on the condition, LGIN may not have a vast impact on the prognosis of squamous cell carcinoma over some time because most of it lacks early infiltration (Chen, Xu et al. 2017) from epithelium to submucosa. This difference may stem from the difference in reprogramming energy metabolism. Metabolomics study (Chen, Yi et al. 2021) also showed glycolysis rate of high grade squamous intraepithelial neoplasia might be higher than low grade in cervical squamous intraepithelial lesion whose structure is similar to the esophagus. It suggests microenvironment of BLSCC may be more acidic than LOGIN in the esophagus (diffusion of hydrogen ion).

Low PH condition is usually associated with high expression of matrix metalloproteases and invasive tumor front(Rohani, Hao et al. 2019). Owing to BLSCC close to basement membrane on the condition, it is logical that BLSCC tends to infiltration at an earlier stage with completely missing basement membrane(Chen, Xu et al. 2017). besides, when BLSCC and LGIN above the maximum distance of nutrients, the degree of irregularity in the BLSCC's micro-vascular morphology is more severe than LOGIN from the energy requirement point of view.

According to the classification of intermolecular forces' different physical or chemical origin(Israelachvili 2011), it is clear that reprogramming energy metabolism can affect intermolecular forces inside the cell are purely electrostatic origin. Research(Alshareedah, Kaur et al. 2019) shows that the electrostatic force plays a crucial role in driving the formation of Liquid-liquid phase separation. It is possible that reprogramming energy metabolism can break phase separation of enzymes' homeostasis with the help of low PH condition(Prouteau and Loewith 2018, Dignon, Best et al. 2020), so the Warburg effect suggests BLSCC's cytoplasm may be closer to solid-phase than LGIN. Come back to our model, it suggests iodine molecules may permeate cells of LGIN more easily than BLSCC because of their different degree of Warburg effect. The inference will cause a decline of the term " $C_{\text{iodine}-s}$ " so that " $C_{\text{complex}-s}$ " is reduced base on Eq(15). According to Eq(1), LGIN is easier

to undergo color fading than BLSCC in the same condition of Lugol's staining. From a data science perspective for detecting early cancer of the esophagus, LOGIN may have a higher positive rate than BLSCC for Lugol's Chromoendoscopy. Clinical data also hints at this trend([Dawsey, Fleischer et al. 1998](#)). on the other side of the spectrum, Lennard-Jones potential suggests cytoplasm's solid phase could prevent oxygen's simple diffusion, so it means cancer cells have to choose anaerobic metabolism. It is more than likely that reprogramming energy metabolism and LLPS are mutually reinforcing relationships.

Although BLSCC is regarded as a kind of high-grade squamous dysplasia([Board 2019](#)), a question remains: do BLSCC have an independent evolution process relative to typical superficial esophageal carcinoma? The cytological resemblance between them is remarkable. Most cases of BLSCC usually coexist with typical SCC components or LOGIN components([Zhuang, Chen et al. 2019](#)). These histological characteristics suggest BLSCC and typical superficial esophageal carcinoma might share the same evolution way even though the lamina propria mucosae is easier to be infiltrated by BLSCC than LOGIN. Still, in the absence of any further experimental evidence, we cannot answer this question fully. From a data science point of view, it is a potential choice to construct a phylogeny tree([Schwartz 2008](#)) base on data from next-generation sequencing(NGS) and an algorithm for answering the question.

Phylogeny tree is involved in depicting the evolutionary relationship among species and exploring various tumor lineage([Coorens, Farndon et al. 2020](#)). Logically, we can construct a phylogeny tree among BLSCC, LGIN, typical superficial esophageal carcinoma, and regular esophageal tissue base on specific algorithms and data from NGS. However, inter-observer variation in the pathological diagnosis of BLSCC and LGIN ([Zhuang, Chen et al. 2019](#)) may bring difficulty to phylogeny analysis, so how to raise pathological diagnostic accurate is the key to construct the phylogeny tree.

Conclusion

In conclusion, through an analysis of diffusion dynamics of Lugol's chromoendoscopy in Basal layer-type squamous cell carcinoma in situ, our model reveals that the efficacy of Lugol's chromoendoscopy is determined by the thickness of the squamous epithelial cell layer, which contains glycogen granules and the number of IPCL. When some components of BLSCC near the basement membrane, Lugol's chromoendoscopy's effect should weaken because their energy requirement does not only rely on tumor angiogenesis, and their unique histological structure does not allow them to break squamous epithelial cell layer which contains glycogen granules. By extrapolating iodine diffusion from the "pink color sign," it is possible that the cytoplasm of BLSCC and typical superficial esophageal carcinoma tend to solid-phase if

they both share the same evolution path.

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Figure

Figure A

Lugol's chromoendoscopy: 1. Brown dark pattern is normal squamous epithelium; 2. Yellow pattern is usually associated with dysplasia or early malignancy.

Figure B

“pink color sign” means high grade dysplasia involves the whole epithelium layer, Yellow pattern dysplasia don’t involve the whole epithelium layer.

Figure C

For our model, the nonkeratinizing ,stratified squamous epithelium can be as simple as multilayer cubes and infinitesimal fluid elements; it is clear that the calculation of diffusion direction of Iodine is simplified.

Figure D

FigureD(a) and (b) shows BLSCC's unique histological structure. It is similar to the definition of high-grade dysplasia from WHO(2019): severe cytological atypia regardless of the extent of epithelial involvement. Please note the difference between (a) and (b). Due to tumor-associated angiogenesis of BLSCC, the integrated effects of the maximum distance of nutrient diffusion and the degree of cytological atypia may be determined. (Note: The picture does not show the actual thickness of epithelium because the specimen of endoscopic submucosal dissection

tends to shrink by dehydrated)

Figure E

Tumor and normal tissues are joined in step base on the histology of BLSCC. BLSCC are black cubes; we analyze the iodine diffusion between BLSCC and normal epithelium via the Euler method through the geometry structure.