Symbiosis increases population size and buffers environmental fluctuations in a physiologically-structured model parameterized for thyasirid bivalves

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Abstract

Symbioses whereby one partner provisions a nutritional resource to the other may alter energy allocation towards reproduction and survival in the recipient partner, potentially impacting population dynamics. Asymbiotic thyasirid bivalves feed predominantly on free-living bacteria, which fluctuate in abundance due to seasonality-driven temperature variations. Symbiotic thyasirids are mixotrophs, gaining nutrients from free-living bacteria and symbiotic bacteria that they host on their enlarged gills. Symbiotic bacteria may function as an additional energy reserve for thyasirids, allowing the hosts to allocate more energy to reproduction. We hypothesize that, for symbiotic thyasirids, the symbionts are a nutritional source that mitigates resource limitation. Using Dynamic Energy Budget theory, we built a physiologically-structured population model assuming equal mortality rates in both species. We find that without seasonal fluctuations, symbiotic thyasirids have higher abundances than asymbiotic thyasirids since the symbionts increase reproduction. Both species have similar population sizes in fluctuating environments, suggesting different adaptations to seasonality: asymbiotic thyasirids have adapted their physiology, while symbiotic thyasirids have adapted through mixotrophy. Our results highlight the significance of linking individual energetics and life-history traits to population dynamics and are the first step towards understanding the role of symbioses in population and community dynamics.

11 *Keywords:* Energy reserves, dynamic energy budget theory, mixotrophy,
12 thysasirids, seasonality, structured population model, symbiosis

13 1. Introduction

14 Nutritional symbiosis is a prevalent interaction that can increase the
15 metabolic capabilities of the host (Dubilier et al., 2008; Moran, 2006). Hence,
16 symbiosis has the potential to affect host life-history traits, such as fecundity
17 and survival, which, in turn, determine population dynamics. However, how
18 symbiosis can influence host ecology and how this would be translated into
19 population and community dynamics is not known (Yule et al., 2013). Disen-
20 tangling the bottom-up effect of trophic symbiosis on ecological timescales, in
21 both constant and heterogeneous environments, is crucial to understanding
22 the conditions that lead to the persistence of populations and communities
23 (Miller and Rudgers, 2014).

24 Environmental heterogeneity and the pattern of environmental variation
25 are thought to be determinant factors in the evolution of the niche breadth,
26 particularly for traits such as foraging strategies (Lynch and Gabriel, 1987;
27 Kassen, 2002). Theory suggests that selection favours generalist strategies in
28 populations experiencing environmental heterogeneity (Lynch and Gabriel,
29 1987; Levins, 1968; Futuyma and Moreno, 1988). Experimental results have
30 confirmed such findings (Reboud and Bell, 1997; Bell and Reboud, 1997;
31 Kassen and Bell, 1998, but see Riddle et al. 1986 for conflicting results). For
32 example, selection experiments in *Chlamydomonas* in constant environments
33 have led to the evolution of specialists, either autotrophic or heterotrophic.
34 Conversely, in temporally varying environments, selection favours general-
35 ists capable of both autotrophic and heterotrophic nutrition. However, in
36 spatially varying environments, both specialists can be retained in the pop-
37 ulation (Reboud and Bell, 1997; Bell and Reboud, 1997; Kassen and Bell,
38 1998). Broadly, these results suggest that ecological specialists tend to be
39 selected in environments that are homogeneous in space or time, whereas
40 generalists tend to be favoured in temporally varying environments (Kassen,
41 2002; Lynch and Gabriel, 1987; Levins, 1968; Futuyma and Moreno, 1988;
42 Ackermann and Doebeli, 2004).

43 Nutritional symbioses in which the host has a mixotrophic nutrition (i.e.
44 the host can combine the nutritional input from the symbionts with het-
45 erotrophic or autotrophic feeding; Rossi et al., 2017) can be considered to

be generalist feeding strategies. For instance, mixotrophic symbioses are frequent in marine suspension feeders, which live in environments where light and plankton concentration are variable and often limiting (Muller-Parker and Davy, 2001; Grottoli et al., 2006). In octocorals, such trophic flexibility has been proposed to maximize nutrient uptake, allowing for increased energy acquisition, relative to asymbiotic species (Gori et al., 2012; Grottoli et al., 2006). Moreover, the loss of symbionts may not significantly affect the host's energetic input, making the host less affected by environmental variability (Rossi et al., 2017; Viladrich et al., 2017; Fabricius et al., 1995; Sorokin, 1991; Ferrier-Pagès et al., 2015). Thus, in seasonal environments, symbionts can provide energy to a mixotrophic host and stabilize the discontinuous energy inputs in resource availability (Rossi et al., 2017; Viladrich et al., 2017; Gori et al., 2012).

Another notable example of mixotrophy occurs in symbiotic thyasirid bivalves, a family that stands out for including symbiotic as well as asymbiotic members (Taylor et al., 2007; Southward, 1986). Symbiotic thyasirids are flexible mixotrophs that can digest their symbionts depending on environmental conditions, particularly the presence of sulfide and external particulate food (Dando and Spiro, 1993; Dufour and Felbeck, 2006). Evidence in other bivalves suggests that changes in the relative importance of different food sources are likely correlated to particulate food abundance (Pile and Young, 1999). A mixotrophic nutrition is considered a strategy that allows symbiotic thyasirids to thrive in fluctuating environments (Dufour and Felbeck, 2006; Duperron et al., 2013).

In the fjord of Bonne Bay (Newfoundland, Canada), two species of thyasirids are sympatric and have a patchy distribution. The first species resembles *Thyasira gouldi* (in shell characteristics and internal anatomy) and therefore is referred to as *T. cf. gouldi*; the second species, *Parathyasira* sp., is asymbiotic. Both symbiotic *T. cf. gouldi* and asymbiotic *Parathyasira* are particulate feeders that rely on chemoautotrophic bacteria as their primary resource (60% and 70%, respectively), with lesser contributions of suspended and particulate organic matter (Zanzerl et al., 2019). However, rather than collecting chemoautotrophic bacteria from sediments through pedal feeding, *T. cf. gouldi* harbours these bacteria extracellularly as symbionts on enlarged gills and digests them as an additional resource (Laurich et al., 2015; Zanzerl et al., 2019); hence, it is considered a mixotrophic species. For *T. sarsi*, another mixotrophic thyasirid, between 26 and 76% of their nutrition has been estimated to be obtained from the bacterial symbionts (Dando and Spiro,

1993). Given that the carbon isotope composition in *T. cf. gouldi* overlaps the lower range of the isotopic signature of *T. sarsi* (Dando and Spiro, 1993; Zannerl et al., 2019), it is likely that the reliance of *T. cf. gouldi* on symbionts may be similar to the lower limit of *T. sarsi*'s, comprising approximately 25% of their diet. For thysanurids inhabiting an environment with strong seasonality, temperature and resource fluctuations will affect the individual metabolic rates and the costs associated with maintaining the symbionts. Previous theoretical research showed that symbiotic *T. cf. gouldi* has a smaller energy reserve, which implies reduced energy assimilation and mobilization fluxes, lower somatic maintenance costs and growth rate, and more significant energy allocation to maturity and reproduction (Mariño et al., 2019). However, how the nutritional differences between symbiotic *T. cf. gouldi* and asymptotic *Parathysanura* are reflected at the population and community levels is not known.

Our previous results support the hypothesis that a mixotrophic (generalist) strategy results in higher energy allocation to reproduction (McKillup and Butler, 1979; Thompson, 1983; George, 1994; Viladrich et al., 2017). Thus, in a constant environment, a mixotrophic population should have larger abundances than the asymptotic (specialist) population. Here, we hypothesize that when there is seasonality, relying on symbionts will buffer the fluctuations in resource availability for the host population. We predict that if symbionts effectively mitigate resource variability, then the mixotrophic population will be less prone to extinction during winter when the abundance of free-living bacteria becomes limiting. Our prediction should hold while the abundance of symbionts is not zero and is at least equal to the lowest free-living bacterial abundance. However, the buffering effect of the symbionts should decrease as the host becomes more specialized and increases reliance on the symbionts. Hence, in highly seasonal environments, a low or intermediate level of dependence on symbionts (i.e. a generalist strategy) should be favoured over the specialist strategy.

Since the physiological responses of individuals can be considered the underlying basis of their ecological dynamics, models that consider the organismal bioenergetics are powerful tools to understand how energetic constraints determine changes in the niche of a species as a consequence of environment fluctuations (Nisbet et al., 2012). Energy budget models describe the rates at which an individual assimilates and uses energy for maintenance, growth, and reproduction (van der Meer, 2006; Kooijman, 2010). To understand how the differences due to feeding and symbiosis translate to the population level

and shape host population dynamics, we combine the individual-level energy budget dynamics with a physiologically-structured population model (Kooijman, 2010; De Roos et al., 2009). We built a population model that accounts for the species' physiology according to the individual DEB model and takes into account the seasonal pattern of temperature and resource abundance. Using this model, we simulated the dynamics of the symbiotic *T. cf. gouldi* and the asymbiotic *Parathyasira*.

Previously, we suggested that the energy allocation patterns in symbiotic thyasirids may represent an evolutionary strategy where the symbionts function as a partial energy reserve, allowing the individuals to invest more energy in reproduction (Mariño et al., 2019). Here, we focus on the differences in populations inhabiting a constant versus seasonal environment, and evaluate different scenarios of symbiont dependence and abundance. We show how the symbiotic strategy is likely to mitigate the effects of environmental variability in a population of symbiotic thyasirids. We discuss the buffering effect of the symbionts in terms of the evolution and ecological adaptation of thyasirids and mixotrophic bivalves.

2. Methods

2.1. The model

We formulated a continuous population model that focuses on the representation of individual physiology and life history. To describe individuals, we used the DEB-abj model (Kooijman, 2014), which is structured by energy, volume, maturity and reproduction (Fig. 1). We used published data from *T. cf. gouldi* and *Parathyasira* sp. to parameterize the model (Mariño et al., 2019). We assumed that individuals in the population could exploit one or two resources, depending on whether they are asymbiotic or symbiotic. To explicitly include the dependency of the resource on the environmental temperature, we modelled the resource according to relationships derived from the Metabolic Theory of Ecology (Savage et al., 2004). To test our predictions of how symbiosis affects populations of thyasirid bivalves, we conducted numerical simulations for *T. cf. gouldi* and *Parathyasira* in different environmental conditions that consider various temperature and resource availability scenarios. To further analyze the possible effects of symbiosis on populations of *T. cf. gouldi*, we carried out simulations representing different relative symbiont abundances and different contribution of symbionts to the host's diet.

Figure 1. Representation of the three main components of the model for *Thyasira cf. gouldi* in time: 1) the environment (A, B, C), 2) the individual (D, E, F, G) and 3) the population (H). The environmental variables of temperature (A, equation 1) and free-living bacterial resource (C, equation 2) determine each individual's dynamics. The carrying capacity of the free-living bacterial resource ($K_R(T)$) and its growth rate ($r_R(T)$) are functions of the environmental temperature (B, equations 3 and 4). For both parameters, we follow relationships derived from the Metabolic Theory of Ecology (Savage et al., 2004). We characterize the individuals by four variables: energy in reserve (D), structural volume (E), maturity (F) and reproduction energy (G), according to the DEB model (equation 7). We obtain the population dynamics (H) by numerically integrating over all the individuals (equation 10). The simulations' parameters are given in Tables 2 and 3. We assumed an initial condition of 5 embryos for the simulation of the population.

158 2.2. Environment

159 2.2.1. Temperature

160 We modelled an annual cycle that corresponds to the seafloor tempera-
161 tures at Bonne Bay, which range from 0.7 to 14 °C, approximately (Laurich
162 et al., 2015, see Fig. 1A). More specifically, the temperature at time t os-
163 cillates around the average temperature ($\bar{T}$) with amplitude T_a and period
164 equal to the length of the year:

$$T(t) = \bar{T} + T_a \sin\left(2\pi \frac{t}{365}\right). \quad (1)$$

165 For comparative purposes, we also modelled a constant environment as-
166 suming that the temperature is equal to the mean annual temperature, $\bar{T}$.

167 2.2.2. Resource

168 The primary resource for *T. cf. gouldi* and *Parathyasira* is free-living,
169 chemoautotrophic bacteria (Zanzerl et al., 2019). In cold, marine sediments,
170 such as Bonne Bay, bacterial production is typically seasonal, with specific
171 growth rates increasing with temperature; further, bacterial production is
172 directly proportional to bacterial biomass (Sander and Kalff, 1993). Thus,
173 we assumed that the free-living bacterial resource R is a function of the
174 environmental temperature T , and follows logistic growth:

$$R(T) = r_R(T)R \left(\frac{K_R(T) - R}{K_R(T)} \right), \quad (2)$$

175 where r_R is the resource growth rate and K_R is the maximum resource density.
176 For notational simplicity, we let $T = T(t)$; however, it should be understood
177 that temperature may be a function of time as described in equation 1.

178 To include the dependence of the resource on the environmental tempera-
179 ture, we described both resource parameters using relationships derived from
180 the Metabolic Theory of Ecology (Savage et al., 2004). We assumed that the
181 growth rate and carrying capacity increase exponentially with temperature.
182 Further, around the limits of the bacteria's thermal niche, both param-
183 eters drop steeply to zero, according to a Sharpe-Schoolfield term (Schoolfield

et al., 1981, see Fig. 1B). Hence, the resource growth rate is given by:

$$r_R(T) = r_0 e^{(-\mathcal{E}/k_B)(1/T-1/T_0)} \left(1 + e^{(-\mathcal{E}_L/k_B)(1/T-1/T_L)} + e^{(-\mathcal{E}_H/k_B)(-1/T+1/T_H)} \right)^{-1}, \quad (3)$$

where r_0 is the resource growth rate at a reference temperature T_0 , k_B is the Boltzmann constant, $\mathcal{E}$ is the average activation energy driving resource growth at intermediate temperatures, $\mathcal{E}_L$ and $\mathcal{E}_H$ are the inactivation energies that determine the slope of the resource growth rate as it drops to zero at the lower and upper thermal tolerance limits, T_L and T_H , respectively.

The maximum resource density follows a similar formulation:

$$K_R(T) = K_0 e^{(-\mathcal{E}/k_B)(1/T-1/T_0)} \left(1 + e^{(-\mathcal{E}_L/k_B)(1/T-1/T_L)} + e^{(-\mathcal{E}_H/k_B)(-1/T+1/T_H)} \right)^{-1}, \quad (4)$$

where K_0 is the maximum resource density at a reference temperature T_0 . As with the resource growth rate, the parameters $\mathcal{E}$, $\mathcal{E}_L$ and $\mathcal{E}_H$ represent the temperature sensitivity of the maximum resource density within and outside of the lower and upper temperature thresholds, T_L and T_H .

2.3. Individual dynamics

We described the individual life history and physiology (i.e. feeding, growth, and reproduction) as a function of the individual state variables and the state of the environment.

2.3.1. Feeding

All individuals forage on the resource (free-living bacteria) following a functional response $f(t, T, R)$, which is a function of the time of the year, the temperature and the resource abundance. Asymbiotic individuals feed only on one resource according to the scaled functional response:

$$f_A(R) = \frac{R(T)}{R_{\max}}, \quad (5)$$

where $R_{\max}$ is the maximum resource density.

205 Symbiotic individuals can forage on the symbionts as an additional re-
 206 source, which we modelled as a constant, scaled abundance S . Thus, the
 207 functional response for symbiotic individuals $f_S(t, T, R)$ includes their re-
 208 liance on symbionts α , and is given by:

$$f_S(R) = (1 - \alpha) \left(\frac{R(T)}{R_{\max}} \right) + \alpha \left(\frac{S}{R_{\max}} \right). \quad (6)$$

209 2.3.2. Growth and reproduction: DEB-abj model

210 The individual dynamics are according to the Dynamic Energy Budget
 211 theory (Kooijman, 2010). This approach distinguishes between the biomass
 212 of the organism that functions as an energy reserve and as structure. Specif-
 213 ically, we use the DEB-abj model, which is a one parameter extension of
 214 the standard DEB model that accounts for a growth pattern recognized in
 215 bivalves termed metabolic acceleration (Kooijman, 2014).

216 Each individual is characterized by four state variables: energy in reserve
 217 (E), structural volume (L^3), cumulative energy invested into maturation
 218 (E_H), and cumulative energy invested into reproduction (E_R). The dynamic
 219 of the individual in time is given by:

$$\begin{aligned} \frac{dE}{dt} &= \dot{p}_A - \dot{p}_C, \\ \frac{dL^3}{dt} &= \kappa(\dot{p}_C - \dot{p}_S)/[E_G], \end{aligned} \quad (7)$$

$$\begin{cases} \frac{dE_H}{dt} = (1 - \kappa)\dot{p}_C - \dot{p}_J \text{ and } \frac{dE_R}{dt} = 0, & \text{if } (E_H < E_H^p), \\ \frac{dE_H}{dt} = 0 \text{ and } \frac{dE_R}{dt} = (1 - \kappa)\dot{p}_C - \dot{p}_J, & \text{otherwise,} \end{cases}$$

220 where the energy fluxes are denoted by $\dot{p}$ (see Table 1), κ is the fraction of
 221 mobilized reserve allocated to somatic metabolism, $[E_G]$ is the specific cost
 222 to grow one unit of structure, and E_H^p is the puberty threshold.

Table 1. Energy fluxes ($\dot{p}$, J/d) and shape correction function ($\mathcal{M}$) at each developmental stage. Each stage is defined according to the cumulative maturity thresholds E_H^b , E_H^j and E_H^p , which represent birth, metamorphosis, and puberty, respectively. The scaled functional response is f ($0 \leq f \leq 1$, where 1 is the highest amount of food), $\{\dot{p}_{Xm}\}$ is the maximum surface-area specific ingestion rate ($\{\dot{p}_{Xm}\} = \{\dot{p}_{Am}\} / \kappa_X$, J/day $\cdot$ cm², for a maximum surface-area specific assimilation rate $\{\dot{p}_{Am}\}$), κ_X is the assimilation efficiency from food to reserve, $\dot{v}$ is the energy conductance rate from the energy reserve (cm/day), $\dot{r}$ is the individual growth rate (1/day, equation 8), $[\dot{p}_M]$ is the volume-specific somatic maintenance cost (J/day $\cdot$ cm³), k_J is the maturity maintenance rate coefficient. The structural lengths at the beginning and at the end of the acceleration are L_b and L_j , which correspond to the structural lengths at birth and at metamorphosis. Notation: square brackets ($[\]$) indicate quantities related to structural volume, curly brackets ($\{ \}$) denote quantities related to structural surface-area, dots ($\dot{\ }$) indicate rates.

Flux	Embryo ($E_H \leq E_H^b$)	Early juvenile ($E_H^b < E_H \leq E_H^j$)	Late juvenile ($E_H^j < E_H < E_H^p$)	Adult ($E_H \geq E_H^p$)
Feeding, $\dot{p}_X$	0	$f\{\dot{p}_{Xm}\}\mathcal{M}$	$f\{\dot{p}_{Xm}\}\mathcal{M}$	$f\{\dot{p}_{Xm}\}\mathcal{M}$
Assimilation, $\dot{p}_A$	$\kappa_X \dot{p}_X$	$\kappa_X \dot{p}_X$	$\kappa_X \dot{p}_X$	$\kappa_X \dot{p}_X$
Mobilization, $\dot{p}_C$	$E\dot{v}(\mathcal{M}/L - \dot{r})$	$E\dot{v}(\mathcal{M}/L - \dot{r})$	$E\dot{v}(\mathcal{M}/L - \dot{r})$	$E\dot{v}(\mathcal{M}/L - \dot{r})$
Soma maint., $\dot{p}_S$	$[\dot{p}_M]L^3$	$[\dot{p}_M]L^3$	$[\dot{p}_M]L^3$	$[\dot{p}_M]L^3$
Maturity maint., $\dot{p}_J$	$k_J E_H$	$k_J E_H$	$k_J E_H$	$k_J E_H^p$
Shape function, $\mathcal{M}$	$L_b/L_b = 1$	L/L_b	L_j/L_b	L_j/L_b

223 The growth rate for each individual is given by:

$$\dot{r} = \frac{\kappa \frac{E}{L^4} \dot{v} \mathcal{M} - [\dot{p}_M]}{\kappa \frac{E}{L^3} + [E_G]}, \quad (8)$$

224 where $\mathcal{M}$ is a shape correction function that varies according to the stage of
225 the individual (see Table 1), $\dot{v}$ is the energy conductance rate, and $[\dot{p}_M]$ is
226 the somatic maintenance cost.

227 The energy fluxes for all the metabolic rates are temperature-dependent
228 (see Section 1.3 in Kooijman, 2010), therefore the parameters of the model
229 are standardized to a reference temperature of 20°C. The correction between
230 the reference temperature and the empirical temperature T is done through
231 the Arrhenius relationship:

$$c_T = \exp \left(\frac{T_A}{T_{\text{ref}}} - \frac{T_A}{T} \right), \quad (9)$$

232 where $c(T)$ is the correction factor for a certain temperature T , T_A is the

233 Arrhenius temperature and T_{ref} is the reference temperature. For example,
 234 the mobilization flux (Table 1) at temperature T becomes: $\dot{p}_C(T) = \dot{p}_C(T_{ref}) \cdot$
 235 $c(T)$.

Table 2. Parameter values for the individual-level dynamics (equation 7) for the symbiotic *Thyasira* cf. *gouldi* and the asymbiotic *Parathyasira* sp. (Mariño et al., 2019). Notation: square brackets ([]) indicate quantities related to structural volume, curly brackets ({ }) denote quantities related to structural surface-area, dots (·) indicate rates.

Description	Symbol	<i>Thyasira</i> cf. <i>gouldi</i>	<i>Parathyasira</i>	Unit
Maximum assimilation rate	$\{\dot{p}_{Am}\}$	1.427	2.547	J/day · cm ²
Assimilation efficiency	κ_X	0.8	0.8	-
Energy conductance rate	$\dot{v}$	0.02	0.02	cm/day
Allocation fraction to soma	κ	0.883	0.958	-
Somatic maintenance cost	$[\dot{p}_M]$	15.78	23.61	J/day · cm ³
Maturity maintenance coefficient	$\dot{k}_J$	0.002	0.002	1/day
Specific cost for structure	$[E_G]$	2355	2348	J/cm ³
Maturity at birth	E_H^b	2.639e-4	7.193e-5	J
Maturity at metamorphosis	E_H^j	0.011	0.002	J
Maturity at puberty	E_H^p	1.283	0.96	J
Weibull aging acceleration	$\dot{h}_a$	9.844e-8	1.262e-7	1/day ²
Shape coefficient	δ_M	0.507	0.64	-
Arrhenius temperature	T_A	8000	8000	K
Reference temperature	T_{ref}	293.15	293.15	K

236 2.4. Population dynamics

237 We represent the population by a density n , which is a function of the four
 238 individual DEB model (or i-states) variables ($n(t, E(t), V(t), E_H(t), E_R(t))$)
 239 and its dynamic in time is given by:

$$\frac{\partial n}{\partial t} + \frac{\partial n}{\partial E} \frac{dE}{dt} + \frac{\partial n}{\partial V} \frac{dV}{dt} + \frac{\partial n}{\partial E_H} \frac{dE_H}{dt} + \frac{\partial n}{\partial E_R} \frac{dE_R}{dt} = -\mu(n + n^2), \quad (10)$$

240 where μ is the per capita mortality rate. The set of all the possible i-states
 241 defines the population state space $\Omega \subset \mathbb{R}^n$. To prevent individuals from
 242 leaving the domain, we included no-flux boundary conditions for each i-state
 243 variable: $E|_{\partial\Omega} \equiv 0, V|_{\partial\Omega} \equiv 0, E_H|_{\partial\Omega} \equiv 0, E_R|_{\partial\Omega} \equiv 0$.

244 The population state space is divided into subsets that represent the
 245 different life stages of the individuals. For simplicity, we group the two

juvenile stages together, and consider the domains Ω_J , and Ω_A , corresponding to the juvenile and adult stages. The boundary between these subsets is given by the cumulative maturity energy threshold parameter E_H^p . Here, we assume that once individuals are adults they cannot rejuvenate and decrease their maturity level. Hence, we further suppose the no-flux boundary:

$$E_H(x) = \begin{cases} E_H(x) & \text{if } E_H(x) \geq 0, \\ 0 & \text{otherwise,} \end{cases} \quad \forall x \in \partial\Omega_J. \quad (11)$$

The reproduction of the adult population gives the boundary condition at age zero:

$$n(t, E_0, V_0, E_{H_0}, E_{R_0}) = \int_{\Omega_A} \beta n dE dV dE_H dE_R, \quad (12)$$

where we consider that the per capita fecundity rate β is a constant. Additionally, we assume that individuals are born in the population at the origin of the domain.

2.5. Model analysis

We implemented our population model in the R language (R Core Team, 2019) and solved it as an initial value problem through the methods of lines. For this, we discretized the evolution equations with finite differences and performed the time integration using the **lsoda** initial value problem solver from the package **deSolve** (Soetaert et al., 2010). Our simulations represented experimental populations that start with 5 embryos, for either species (as in Martin et al., 2012, 2013). Thus, the initial conditions for our numerical simulations were:

$$n(t = 0, x) = \begin{cases} 5, & \text{if } x = (E_0, V_0, E_{H_0}, E_{R_0}), \\ 0, & \text{otherwise.} \end{cases} \quad (13)$$

To investigate how symbiosis affects population dynamics, we conducted simulations at constant and fluctuating environments for both species. The environment and population parameters are given in Table 3, the parameters for the individual dynamics are given in Table 2. For these simulations, we assumed that the abundance of the symbionts was equal to the mean abundance of the free-living bacterial resource ($S = \bar{R}$). Further, we assumed that symbionts provide 25% of the diet of symbiotic individuals ($\alpha = 0.25$).

Table 3. Parameter values for the environment and population-level dynamics for the symbiotic *Thyasira* cf. *gouldi* and asymbiotic *Parathyasira* sp. We assume that the parameter values are equal for both populations.

Description	Symbol	Value	Unit	Reference
<i>Environment</i>				
Temperature	T	variable	K	(Laurich et al., 2015)
Mean temperature	$\bar{T}$	279.15	K	(Laurich et al., 2015)
Temperature amplitude	T_a	7	-	(Laurich et al., 2015)
Lower temperature limit for survival	T_L	273.15	K	-
Upper temperature limit for survival	T_H	303.15	K	-
Reference temperature	T_0	288.15	K	$(T_H + T_L)/2$
Mean activation energy	$\mathcal{E}$	0.43	J	(Savage et al., 2004)
Lower tolerance limit inactivation energy	$\mathcal{E}_L$	1.9	-	-
Upper tolerance limit inactivation energy	$\mathcal{E}_H$	1.9	-	-
Boltzman constant	k_B	$8.617e^{-5}$	eV/K	-
Free-living bacterial resource	R	variable	-	-
Free-living bacterial resource growth rate at T_0	r_0	$5e^6$	day ⁻¹	-
Free-living bacterial resource density at T_0	K_0	$5e^7$	day ⁻¹	-
Maximum free-living bacterial resource density	R_{max}	variable	-	-
Symbiont scaled abundance	S	variable	-	-
<i>Population</i>				
Birth rate	β	0.005	day ⁻¹	-
Death rate	μ	0.001	day ⁻¹	(De Roos and Persson, 2001)

272 To analyse the effect of the abundance of symbionts in a host population
 273 inhabiting a fluctuating environment, we investigated three possible cases:
 274 i) the abundance of the symbionts is equal to the average abundance of the
 275 resource ($S = \bar{R}$); ii) the symbionts are more abundant than the resource
 276 ($S = R_{max}$); and iii) the symbionts are less abundant than the resource
 277 ($S = R_{min}$). Here, we also assumed that the contribution of symbionts to a
 278 host individuals' diet is 25% ($\alpha = 0.25$). Further, to assess how the reliance
 279 on symbionts alters the abundance of the host population, we evaluated the
 280 impact of the dependence on symbionts (α) for the case $S = \bar{R}$. This way,
 281 we consider several values of α , ranging from individuals that do not rely on
 282 symbionts ($\alpha = 0$), to those that rely solely on symbionts as their resource
 283 ($\alpha = 1$). The results presented for these sections correspond to the values of
 284 the population after transient dynamics have disappeared.

3. Results

3.1. The symbiotic population has a greater proportion of adults

In the constant environment, both the asymbiotic and the symbiotic ($\alpha = 25\%$) species reach carrying capacity and stabilize after two years (Fig. 2A). Both populations are dominated by individuals in the juvenile classes, with all the stages following the same growth pattern (Fig. 2B, C). However, the symbiotic *T. cf. gouldi* population shows a faster growth rate and reaches a higher carrying capacity, relative to the asymbiotic *Parathyasira* (Fig. 2A-C) since individuals of *T. cf. gouldi* allocate more energy to reproduction (Mariño et al., 2019). Further, in the symbiotic population, a larger proportion of individuals are in the adult stage (Fig. 2C).

In the seasonal environment, the populations of both species experience yearly cycles of low temperatures and low abundances of free-living bacteria (Fig. 1A, B), which cause a decrease in the individual growth and maturity rates as well as in the production of offspring (Fig. 1D, F). Consequently, both populations exhibit similar amplitude fluctuations with a one-year periodicity (Fig. 2D). During the periods of low free-living bacteria abundance, the symbiotic and asymbiotic thysirid populations have similar sizes (Fig. 2D). Individuals in all the stages follow the same regular oscillations, with juveniles being the most abundant class in both populations (Fig. 2E). However, the proportion of adults is higher in the symbiotic population, reaching a greater abundance and a larger minimum size than the asymbiotic population (Fig. 2F).

3.2. Increasing symbiont abundance increases the population size of the host

In the seasonal environment, the dynamics of the population of symbiotic *T. cf. gouldi* vary according to the abundance of symbiotic bacteria (Fig. 3A). The population attains the largest size when the abundance of symbionts is greater than the abundance of the free-living bacteria (i.e. $S > R$, Fig. 3A). In this case, the mean population size and the amplitude of the yearly cycles are larger than in the other scenarios. As the abundance of the symbionts decreases (i.e. $S < R$), the host population exhibits cycles of smaller amplitudes and reaches a smaller mean size (Fig. 3A).

In the three scenarios of symbiont abundance that we considered, the dynamics of the different age classes of symbiotic *T. cf. gouldi* follow the same pattern as the population (Fig. 3B). Individuals in the juvenile stage dominate the populations and exhibit the largest amplitude in abundance when

Figure 2. Modelled long term population dynamics for the symbiotic *T. cf. gouldi* and asymbiotic *Parathyasira sp.* in a constant (A-C) or fluctuating environment (D-F). For all cases, the initial population consists of five embryos. The reliance of *T. cf. gouldi* on symbionts is assumed to correspond to 25% of their diet. The symbiotic strategy allows individuals to invest more energy in reproduction, resulting in larger population sizes than the asymbiotic population in the constant environment (A). In the seasonal environment (D), both populations exhibit yearly cycles due to the combined effect of temperature and resource fluctuations. The stage dynamics for juvenile individuals (B, E) and adult individuals (C, F) exhibit the same pattern as the total population, with juveniles dominating both species' populations. In both environment scenarios, the proportion of adults is greater in the symbiotic population.

Figure 3. Effect of different symbiont abundances (S) relative to the free-living bacteria (R) on the host population of *T. cf. gouldi* in a seasonal environment. For all cases, the initial population consists of five embryos, and the reliance of *T. cf. gouldi* on symbionts corresponds to 25% of their diet. Points represent the average population size after discarding transient dynamics, and lines correspond to the yearly cycle's amplitude. An increasing relative symbiont abundance is predicted to increase the average, minimum and maximum population sizes in *T. cf. gouldi* (A). The stage dynamics exhibit the same pattern as the total population, with juveniles dominating both species' populations (B).

the conditions for the symbionts are favourable. In contrast, fluctuations in
amplitude are smaller for the adult stage. Nevertheless, an increase in the
abundance of symbionts favours a higher mean number of adults.

3.3. Increasing reliance on symbionts reduces the amplitude of the population cycles of the host

For populations of symbiotic *T. cf. gouldi* in a seasonal environment, the amplitude of the yearly cycles depends on the reliance of each individual host on the symbiotic bacteria (Fig. 4A). The largest mean population size and annual cycles with the highest amplitude occur in the population where individuals do not obtain nutrients from symbionts (i.e. $\alpha = 0$, equivalent to asymbiotic individuals, Fig. 4A). An increasing reliance on symbionts reduces the effect of seasonal fluctuations in the free-living bacterial resource. Consequently, both the amplitude of the population cycles and the mean population size decrease. The smallest amplitudes and mean population sizes occur in the population where hosts rely entirely on symbionts (i.e.

$\alpha = 1$, equivalent to obligate symbiosis), given that they are not affected by fluctuations in resource availability. However, populations that rely entirely on symbionts still experience fluctuations in abundance since temperature affects the metabolic rates. Furthermore, the minimum population size rises with increasing reliance on symbionts, the highest minimum occurring in the population where individuals are obligate symbionts. Therefore, in a seasonal environment, populations with a greater dependence on symbionts are less likely to experience extinction.

As in our previous results, the dynamics of the two stages of symbiotic *T. cf. gouldi* follow the same fluctuating pattern as the combined population (Fig. 4B). In all the scenarios considered, juvenile individuals predominate and show the greatest variation in abundance, whereas individuals in the adult class exhibit cycles of smaller amplitude. Both the adult and juvenile stages reach a greater average population size when they have a low reliance on symbionts. Similarly, the mean population size of both stages decreases with an increase in the individual specialization on the symbionts. For the two stages, the minimum population size shows an increase as the dependence on symbionts increases.

4. Discussion

We show how the host's individual physiology and the abundance of and dependence on symbionts affect thysirid population dynamics in constant and seasonal environments. Our simulations for a constant environment reveal that the mixotrophic species reaches a higher population size than the asymbiotic species. In a seasonal environment, the population of symbiotic adults has a higher growth rate during periods of the year with higher temperatures and a greater abundance of free-living resources. Similarly, in periods where the temperatures are low, and resource is limiting, the mixotrophic adult population is less prone to extinction due to the assimilation of symbiotic bacteria. Moreover, the symbiont abundance and the degree of specialization in the host's diet modulate the effect of symbiosis. Thus, our results support our initial hypothesis that symbiosis with an intermediate level of reliance on the symbionts mitigates the impact of resource seasonality.

4.1. Population dynamics

We found that symbiotic thysirids reach larger population sizes and have faster population growth than the asymbiotic species in a constant environ-

Figure 4. Effect of varying symbiont reliance (α) on the host populations in a seasonal environment. For all simulations, the initial population consists of five embryos. *T. cf. gouldii*, which has a dependence on symbionts assumed to be 25%, is highlighted for reference. Points represent the average population size after discarding transient dynamics, and lines correspond to the amplitude of the yearly cycle. An increasing symbiont dependence decreases the magnitude of the annual population cycles (A). As dependence on symbionts increases, the average and maximum population sizes decrease; however, the minimum population size increases. The stage dynamics exhibit the same pattern as the total population, with juveniles dominating both species' populations (B).

ment (Fig. 2A). A similar pattern has been found in *T. sarsi*, which has an intermediate reliance on bacterial symbionts (between 26 to 76%) and exhibits a faster population growth rate, reaching larger population sizes when compared to the sympatric and less symbiont dependent *T. equalis* (which has a reliance below 26%) (Dando and Spiro, 1993). However, unlike *T. equalis*, the asymbiotic *Parathyasira* have higher somatic growth rates and reach larger sizes at maturity, relative to the symbiotic *T. cf. gouldi* (Mariño et al., 2019). Further, our results show that both populations are composed mostly of juvenile individuals (Fig. 2B, E). A comparable population structure has been observed in *Thyasira gouldi*, which exhibits a bimodal distribution year-round (Blacknell, 1973). Our findings for a seasonal environment show that both populations experience yearly cycles. Similarly, for *Thyasira gouldi*, *T. sarsi*, and *T. equalis* empirical data has suggested that they have variable population sizes (Blacknell, 1973; Dando and Southward, 1986). Thus, despite the limited empirical evidence from other thyasirid bivalves or symbiotic animals, our results broadly agree with the literature.

4.2. Effect of symbiosis on the host population

In our simulations, the symbiotic population of *T. cf. gouldi* experiences oscillations of a similar amplitude relative to the asymbiotic population (Fig. 2D). When we consider a symbiotic population in which the symbionts are more abundant, the amplitude of the population cycles increases (Fig. 3). Conversely, when the individuals have a higher dependency on the symbionts, the yearly cycles have smaller amplitudes (Fig. 4). Broadly, our results indicate that the magnitude of these population cycles is likely an effect of the mixotrophic diet and reduced energy reserves of the individual hosts (Mariño et al., 2019). In general, when the free-living bacteria become a limiting resource, the symbionts provide a stable alternative nutritional source for the host (Gori et al., 2012; Viladrich et al., 2017; Rossi et al., 2017), which does not need to rely on an energy reserve. As a consequence, when the resource is abundant, hosts do not need to build up a large energy reserve. Instead, the individual hosts can allocate more energy to reproduction. This effect is evident in the constant environment when the resource is not limiting, where symbiotic thyasirids reach higher abundances than the asymbiotic population (Fig. 2A).

Benefits of symbiosis at low resource concentrations have been documented before, theoretically and experimentally, in photomixotrophic and

aprosymbiotic organisms (e.g. in ciliates and in hydra Goetsch, 1924; Muscatine and Lenhoff, 1965; Karakashian, 1963; Stabell et al., 2002). The literature agrees that, at low resource concentrations, mixotrophic populations have significantly higher growth rates than aposymbiotic populations, which is sufficient to prevent extinction. At high resource availability, theory suggests that the benefits of symbiosis are in reducing loss rates (Stabell et al., 2002), which agrees with our previous finding of lower somatic maintenance costs for the symbiotic *T. cf. gouldi* when compared to the asymbiotic *Parathyasira* (Marino et al., 2019). The role of symbionts in building-up and performing the primary energy and carbon storage for a host has only recently been described (in the chemosymbiotic flatworm *Paracatenula*; Jäckle et al., 2019). Therefore, evidence agrees with our analysis and suggests a potential role of symbiosis in mitigating environmental fluctuations in populations of mixotrophic individuals.

4.3. Model assumptions and limitations

Our results are related to our assumptions regarding the fecundity, mortality, and competition of the individuals in the populations. For the thysirids of Bonne Bay, we do not have enough evidence to suggest that reproduction occurs in discrete events or that there is competition for resources between the species. Therefore, in our model, reproduction occurs continuously, and each species can graze independently of the other on the free-living bacterial resource. Likewise, for simplicity and lack of detailed information, we assumed that mortality was equal for both species in all the stages. The consequences of our assumptions could influence the population structure in our results. For example, in a population of *T. gouldi*, it has been proposed that juveniles do not uniformly predominate because early juveniles are likely to suffer a greater mortality rate, compared to late juveniles and adults (Blacknell, 1973). Nonetheless, these simplifying assumptions are unlikely to affect the overarching pattern regarding the effect of the symbiotic strategy.

The yearly cycles experienced by both populations are a direct result of the fluctuations in temperature and its effect on the resource. We modelled the temperature oscillations according to the natural variation pattern observed in Bonne Bay. The free-living bacteria are also known to be subject to seasonal variations (Laurich et al., 2015); therefore, we used a framework derived from the Metabolic Theory of Ecology to couple the environmental temperatures to the resource abundance. Even though the abundance

443 and digestion of the bacterial symbionts in *T. cf. gouldi* also show a cycli-
 444 cal trend (Laurich et al., 2015), in our formulation, we treat the symbiont
 445 abundance as constant, considering that they provide a more stable source
 446 of nutrition. Despite our assumptions, the strength of our physiologically
 447 structured model is illustrated by the differences that we revealed between
 448 the two species' populations.

449 4.4. Reliance on symbionts

450 Differences in individual energy allocation have suggested that for *T. cf.*
 451 *gouldi* the symbionts may buffer resource fluctuations (Mariño et al., 2019).
 452 Our simulations suggest that symbiotic and asymbiotic thyasirids have dif-
 453 ferent adaptations to persist during winter conditions when the temperatures
 454 are low, and free-living bacteria are rare. Asymbiotic thyasirids have physi-
 455 ological adaptations that allow them to build a larger energy reserve, which
 456 can be mobilized more when the resource is scarce. Symbiotic thyasirids have
 457 adapted via their symbionts: the reliance on a constant supply of symbiotic
 458 bacteria buffers against the effects of seasonal lows in the abundance of free-
 459 living bacteria. Thus, for the thyasirids from Bonne Bay, both the generalist
 460 mixotrophic and the specialist diet are equally successful strategies.

461 Our results motivate the question of why symbiotic thyasirids do not rely
 462 more on their symbionts, or equivalently, why asymbiotic thyasirids do not
 463 have a broader diet. Both alternatives could lead to individuals less sensitive
 464 to environmental fluctuations and more stable populations sizes (Fig. 4A,
 465 B). Such questions are associated with the phenotypic traits that determine
 466 resource acquisition, which are thought to be defined by an intraspecific cor-
 467 relation between the individual morphology, physiology and behavior. In
 468 general, it is understood that there are costs that prevent the evolution of
 469 niche generalism, for example, phylogenetic constraints (Ackermann and Doe-
 470 beli, 2004; Futuyma and Moreno, 1988). For symbiotic thyasirids, the gill
 471 size of the host imposes a limit to the space available for colonization by sym-
 472 bionts (Dufour, 2005). If the surface area of thyasirid gills shows a positive
 473 allometric relationship to body size, as observed in other chemosymbiotic
 474 bivalves with similarly filibranchiate gills (Duperron et al., 2016), the small
 475 body size of thyasirids may prevent them from harbouring the number of
 476 symbionts that would be necessary for a greater reliance (i.e., equivalent
 477 to the symbiont dependencies observed in larger bivalves). Another likely
 478 explanation is that the costs of maintaining symbionts may rise during the

479 winter, due to an increment in the bioirrigation necessary to control the sym-
 480 biont population size or to an increase in the digestion of symbionts (Zanzerl
 481 et al., 2019). For asymbiotic thyasirids, there may be similar phylogenetic
 482 limitations that have prevented a change in diet and have instead promoted
 483 faster somatic growth and maturation rates. Moreover, an environment with
 484 spatial variation, such as the infaunal habitat of the thyasirids, could equally
 485 favour diet specialization (Reboud and Bell, 1997). The limited evidence
 486 available for the thyasirids hinders a more robust inference; however, it is
 487 clear that both strategies are successfully maintained in the community.

488 The ubiquity of symbiosis makes it a crucial factor that can determine the
 489 outcome of ecological and evolutionary processes (Moran, 2006). Neverthe-
 490 less, how symbiosis affects ecology and evolution remains mostly unknown.
 491 In this study, we show how trophic symbiosis can mitigate the effect of a
 492 seasonal environment in a population of bivalve hosts. Although we param-
 493 eterized our model for the particular system of thyasirid bivalves from the
 494 fjord of Bonne Bay, Canada, our approach has a general nature, and our
 495 results are relevant in a variety of trophic symbiosis. Our results highlight
 496 the relevance of linking individual energetics and life history to population
 497 dynamics and are the first step towards a general understanding of the role
 498 of symbiosis in populations' resilience.

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506 **6. Author contribution statement**

507 All authors conceived the ideas for the project. JM and AH designed the
 508 methodology; JM analysed the results and led the writing of the manuscript.
 509 All authors contributed critically to the drafts and gave final approval for
 510 publication.

511 7. Appendix

512 7.1. Individual model

513 7.1.1. Metabolic acceleration: DEB-abj model

514 In the DEB theory framework, species with larval development typically
 515 exhibit a slow embryonic development combined with a faster development
 516 during the late juvenile and adult stages (Kooijman, 2014). This permanent
 517 increase in the metabolic rate is called metabolic acceleration. The most
 518 common type of acceleration, called $\mathcal{M}$ acceleration, involves a simultaneous
 519 increase in the assimilation and reserve mobilization rates between birth and
 520 metamorphosis, as well as an increase in growth, maturation, reproduction
 521 and respiration. We quantified the metabolic increase in type $\mathcal{M}$ acceleration
 522 according to the shape correction function:

$$\mathcal{M} = \max(L_b, \min(L, L_j)) / L_b,$$

523 where L is the length in structure, and L_b and L_j represent the structural
 524 lengths at the beginning and at the end of the acceleration, which correspond
 525 to the structural lengths at birth and at metamorphosis.

526 7.1.2. Observables: fecundity

527 The state variables of the DEB model are quantities that are not directly
 528 measurable. Hence, to calculate how the cumulative energy invested into
 529 reproduction (E_R) translates to number of embryos per time, we used the
 530 following relation (Eq. 2.56 in Kooijman, 2010):

$$\dot{R} = \frac{\kappa_R E_R}{E_0},$$

531 where κ_R is the reproduction efficiency (set to the standard value of 0.95)
 532 and E_0 (J) is the amount of initial energy reserve invested into each embryo
 533 (i.e. the cost of an egg). To calculate E_0 (Eq. 2.42 in Kooijman, 2010)
 534 we used the routine `initial_scaled_reserve` in the DEBtool MATLAB
 535 package (Lika et al., 2014).

536 7.2. Grid resolution and computational time

537 We ran the models for Section 3.1 using a grid resolution of 30^3 cells for
 538 ten years, measuring each day's population density. In Section 3.2, we used
 539 a grid resolution of 20^3 cells for six years, with output also given every day.

Similarly, for Section 3.3, we integrated the model for six years with output each day, but using a grid of 15^3 cells.

We used an Intel Xeon E5-1650 v2 @ 3.50GHz processor to run the models. We measured the integration time in core-years (calculated as hours $\cdot$ (nodes $\cdot$ cores) / (365 $\cdot$ 24)). The integration time for the models for *Thyasira* cf. *gouldi* and *Parathyasira* sp. in a constant environment at a resolution of 30^3 cells was 0.002 and 0.012 core-years respectively. For the same grid size in the seasonal scenarios, the running time was 0.218 core-years for *T.* cf. *gouldi* and 0.232 core-years for *Parathyasira*. The simulations for *T.* cf. *gouldi* at a 20^3 resolution took 0.018 core-years to complete, and 0.004 core-years using a grid size of 15^3 cells.

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