The effects of introgression across thousands of quantitative traits revealed by gene expression in wild tomatoes

Mark S. Hibbins* and Matthew W. Hahn*,†

*Department of Biology and †Department of Computer Science, Indiana University, Bloomington, IN 47405

Abstract

It is now understood that introgression can serve as powerful evolutionary force, providing genetic variation that can shape the course of trait evolution. Introgression also induces a shared evolutionary history that is not captured by the species phylogeny, potentially complicating evolutionary analyses that use a species tree. Such analyses are often carried out on gene expression data across species, where the measurement of thousands of trait values allows for powerful inferences while controlling for shared phylogeny. Here, we present a Brownian motion model for quantitative trait evolution under the multispecies network coalescent framework, demonstrating that introgression can generate apparently convergent patterns of evolution when averaged across thousands of quantitative traits. We test our theoretical predictions using whole-transcriptome expression data from ovules in the wild tomato genus *Solanum*. Examining two sub-clades that both have evidence for post-speciation introgression, but that differ substantially in its magnitude, we find patterns of evolution that are consistent with histories of introgression in both the sign and magnitude of ovule gene expression. Additionally, in the sub-clade with a higher rate of introgression, we observe a correlation between local gene tree topology and expression similarity, implicating a role for introgressed *cis*-regulatory variation in generating these broad-scale patterns. Our results have important implications for the study of gene expression evolution—and quantitative trait evolution more broadly—in systems with evidence of introgression.

Introduction

Introgression—the hybridization and subsequent backcrossing between previously isolated lineages—has come to the forefront of phylogenomics with the availability of genome sequencing (reviewed in Mallet et al 2016, Taylor and Larson 2019). Introgression has been recognized as a powerful and frequent source of adaptive variation, with many charismatic examples including wing pattern mimicry in butterflies (Pardo-Diaz et al. 2012, Zhang et al. 2016), coat color in snowshoe hares (Jones et al. 2018), herbivore resistance in sunflowers (Whitney et al. 2006), and high-altitude adaptation in humans (Huerta-Sánchez et al. 2014). Introgressed alleles do not have to underlie discrete traits to influence the course of evolution: alleles that contribute to quantitative trait variation can also lead to more similarity than expected between the introgressing lineages (Bastide et al. 2018).

Empirically investigating the effects of introgressed ancestry on quantitative trait evolution remains a challenge, despite recent theoretical and methodological advances (Bastide et al. 2018, Hibbins et al. 2020, Wang et al. 2020). This is because many processes besides introgression can shape the distribution of any particular character, including incomplete lineage sorting and convergence. It is therefore necessary to sample a large number of traits in order to demonstrate a genome-wide effect of introgression. Gene expression is commonly used in comparative analyses between species (e.g. Rifkin et al. 2003, Brawand et al. 2011, Davidson et al. 2012), allowing for the study of thousands of quantitative traits in a phylogenetic framework. Introgressed variants acting on gene expression either in *cis* or in *trans* may affect the evolution of gene expression across the genome. This could have systematic consequences on fitness, which would be consistent with previous evidence for widespread selection against introgressed alleles (Brandvain et al. 2014, Sankararaman et al. 2014, Schumer et al. 2018, Martin et al. 2019).

In order to accurately evaluate the effects of introgression on quantitative traits, the shared history due to both incomplete lineage sorting (ILS) and introgression must be taken into account. It is necessary to include the topological discordance due to ILS and introgression in phylogenetic comparative methods, in order to avoid errors inherent to methods that typically only consider the species topology (Hahn and Nakhleh 2016). Mendes et al. (2018) showed that when gene tree discordance is unaccounted for, standard comparative approaches will return inflated evolutionary rate estimates and will underestimate phylogenetic signal. Despite these challenges, no approach has included all sources of gene tree discordance into a single framework. Some methods have extended the classic Brownian motion model for quantitative trait evolution to include shared histories due to ILS alone (Mendes et al. 2018), while other work has applied the Brownian motion model to a phylogenetic network with introgression but no ILS (Bastide et al. 2018). A method including both sources of discordance would provide a complete picture of the most common causes of shared evolutionary history and their effects on quantitative traits.

To address the effects of introgression on quantitative traits, we leverage whole-transcriptome gene expression data from the wild tomato clade in the genus *Solanum*. This clade includes 13 species that have radiated within the last 2.5 million years, and contains high rates of gene tree

discordance due to both ILS and introgression (Pease et al. 2016, Hamlin et al. 2020). We first present an updated Brownian motion model that includes both ILS and introgression, showing the expected effects of introgression on the similarity in quantitative traits across species. This model leads directly to predictions about patterns of trait-sharing on a three-taxon tree, predictions we test using gene expression data from two independent species triplets with different levels of introgression (Moyle et al. 2021). We find that transcriptome-wide patterns of variation in both triplets are consistent with histories of introgression, with quantitatively stronger signals in the sub-clade with greater introgression. Our analyses demonstrate that introgression can have measurable effects across the genome, on thousands of quantitative traits.

Results

Brownian motion on a species tree

To accurately model trait variation among species, we require an understanding of the evolutionary history that relates those species, and a model for how traits are expected to evolve given that history. We present results using Brownian motion, a statistical model that is commonly applied to quantitative traits. The evolutionary history relating species has classically been provided by a species phylogeny. Under Brownian motion, the character states on the tips of this phylogeny follow a multivariate normal distribution, with the variance and covariances of this distribution provided by the branch lengths of the phylogeny (Felsenstein 1973).

Consider a phylogeny of three species with the topology ((A,B),C) (Figure 1). In units of $2N$ generations, species A and B split at time t_1 , and C split from the ancestor of A and B at time t_2 . The expected phylogenetic variances and covariances for three species can be expressed in a 3×3 matrix, which we denote T :

$$T = \begin{bmatrix} \text{Var}(A) & \text{Cov}(AB) & \text{Cov}(AC) \\ \text{Cov}(BA) & \text{Var}(B) & \text{Cov}(BC) \\ \text{Cov}(CA) & \text{Cov}(CB) & \text{Var}(C) \end{bmatrix} \quad [1]$$

This matrix is multiplied by the evolutionary rate parameter of the Brownian motion model, σ^2 , to obtain trait variances and covariances. When only the species phylogeny is considered (i.e. there is no ILS or introgression), the trait variances (the diagonal elements of T) are determined by the total time along which evolution can occur for each lineage, so $\text{Var}(A) = \text{Var}(B) = \text{Var}(C) = t_2$. The covariances are determined by the length of shared internal branches. In the species tree, only species A and B share an internal branch, so:

$$\text{Cov}(AB \mid \text{no ILS or introgression}) = \sigma^2(t_2 - t_1) \quad [2]$$

Where σ^2 corresponds to the trait evolutionary rate per unit time, and $\text{Cov}(AB) = \text{Cov}(BA)$. All the other covariance terms are equal to 0.

A widespread phenomenon in phylogenomics is gene tree discordance, the disagreement of trees from individual loci with each other and with the species tree (e.g. Pollard et al. 2006, White et al. 2009, Hobolth et al. 2011, Fontaine et al. 2015, Pease et al. 2016, Wu et al. 2018, Vanderpool et al. 2020, Hime et al. 2021). Discordance has multiple biological causes (Degnan and

Rosenberg 2009), and this variation has consequences for the shared history that contributes to trait evolution. Gene trees with the topologies ((B,C),A) or ((A,C),B) contain internal branches shared by species B+C and A+C, respectively (Figure 1). This results in non-zero covariance terms between these two species pairs in T , covariance that cannot arise from evolution solely on the species phylogeny. The consequence of this discordance is that some traits may be closer in value between species that are not closely related in the species tree. We must therefore include discordance in our model to appropriately capture this trait covariance.

Modelling the effects of only incomplete lineage sorting on quantitative trait variances and covariances

One of the most common causes of gene tree discordance is incomplete lineage sorting, which occurs when ancestral lineages persist through successive speciation events (Hudson 1983, Pamilo and Nei 1988). For a rooted triplet, there are four possible gene trees in the presence of ILS: one concordant tree that occurs by lineage sorting with probability $1 - e^{-(t_2 - t_1)}$, and three trees produced by ILS, each with probability $\frac{1}{3} e^{-(t_2 - t_1)}$. One of the three ILS trees is concordant, while the other two are discordant. These probabilities are the basis for the multispecies coalescent model. To obtain the expected trait variances and covariances in T , Mendes et al. (2018) weight the expected gene tree heights and internal branch lengths, respectively, by their expected frequencies under the multispecies coalescent model. We present those results here with a slightly different formulation for consistency with the new results presented below. For the covariance between A and B, we have:

$$\begin{aligned} &Cov(AB \mid \text{no introgression}) \\ &= \sigma^2 \left[(1 - e^{-(t_2 - t_1)}) \left(\frac{e^{t_2}(t_2 - t_1)}{e^{t_2} - e^{t_1}} \right) + \left(\frac{1}{3} e^{-(t_2 - t_1)} \right) \right] \end{aligned} \quad [3]$$

In equation 3, σ^2 corresponds to the trait evolutionary rate per $2N$ generations, which is the scale over which time is measured in the multispecies coalescent model. Inside the square brackets, the first term is the probability of the gene tree produced by lineage sorting, multiplied by that tree's expected internal branch length in units of $2N$ generations. The second term is the probability of the concordant tree produced by ILS, which has an expected internal branch length of 1 in units of $2N$ generations.

Species pairs BC and AC can only have covariance from discordant trees produced by ILS, which gives:

$$\begin{aligned} &Cov(BC \mid \text{no introgression}) = Cov(AC \mid \text{no introgression}) \\ &= \sigma^2 \left(\frac{1}{3} e^{-(t_2 - t_1)} \right) \end{aligned} \quad [4]$$

Again, in these trees the internal branches are of length 1 in units of $2N$ generations, and so are not shown explicitly.

For the expected trait variances, all three species share the same expected variance, which is the total height of all the gene trees weighted by their probabilities. These are:

$$\begin{aligned} \text{Var}(A \mid \text{no introgression}) &= \text{Var}(B \mid \text{no introgression}) = \text{Var}(C \mid \text{no introgression}) = \\ &\sigma^2 \left[(1 - e^{-(t_2-t_1)})(t_2 + 1) + (e^{-(t_2-t_1)})(t_2 + 1 + 1/3) \right] \end{aligned} \quad [5]$$

Where the first term in the square brackets is the contribution from the lineage sorting tree, and the second term is the contribution from the three ILS trees.

Modelling the effects of introgression and ILS on quantitative trait variances and covariances

Now, we extend these expressions for species variances and covariances to include both ILS and introgression. We envision an instantaneous introgression event between species B and C (Figure 1), which occurs at time t_m . This event can be in either direction, with the probabilities of a locus following a history of $C \rightarrow B$ introgression or $B \rightarrow C$ introgression represented using δ_2 or δ_3 , respectively. To capture the processes of ILS and introgression simultaneously, we imagine that each possible history at an individual locus can be represented by a “parent tree” within which lineage sorting or ILS occurs according to the multispecies coalescent process (Meng and Kubatko 2009, Liu et al. 2014, Hibbins and Hahn 2019, Hibbins et al. 2020). This is sometimes referred to as the multispecies network coalescent (Wen et al. 2016, Degnan 2018). For our model, we consider three parent trees (see Supplementary Figure 2): one with no introgression, which occurs with probability $1 - (\delta_2 + \delta_3)$, and two parent trees for the two possible directions of introgression, which occur with probabilities of either δ_2 or δ_3 (these probabilities represent the “rate” of introgression in our model). Each of these three parent trees can generate four possible gene trees with three possible topologies (Figure 1, arrow 1), which vary in the frequency of topologies and expected branch lengths depending on each parent tree's parameters (as in the model of ILS-only described in the previous section).

To obtain expressions for the expected variances and covariances under this model, we must sum the contributions of all gene trees within each parent tree, and then sum the contribution of each parent tree (Figure 1, arrow 2). For the covariance between A and B, this gives:

$$\begin{aligned} \text{Cov}(AB \mid \text{ILS and introgression}) &= \sigma^2 \left[(1 - (\delta_2 + \delta_3)) \left[(1 - e^{-(t_2-t_1)}) \left(\frac{e^{t_2}(t_2 - t_1)}{e^{t_2} - e^{t_1}} \right) + \left(\frac{1}{3} e^{-(t_2-t_1)} \right) \right] \right. \\ &\quad \left. + \delta_2 \left(\frac{1}{3} e^{-(t_2-t_m)} \right) + \delta_3 \left(\frac{1}{3} e^{-(t_1-t_m)} \right) \right] \end{aligned} \quad [6]$$

Note that the term inside the inner square brackets in equation 6 is the same as in equation 3, but is now weighted by the probability of a history with no introgression. In addition, there are two additional terms denoting the contributions of trees generated by ILS that follow a history of introgression (because ILS occurs regardless of the history at a locus). For a complete derivation, including the expectations of each gene tree within each parent tree, see the Supplementary Materials and Methods.

For the covariance between B and C, we have:

$$\begin{aligned}
 & Cov(BC \mid ILS \text{ and } introgression) \\
 &= \sigma^2 \left[(1 - (\delta_2 + \delta_3)) \left[\frac{1}{3} e^{-(t_2-t_1)} \right] \right. \\
 &+ \delta_2 \left[(1 - e^{-(t_2-t_m)}) \left(\frac{e^{t_2}(t_2 - t_m)}{e^{t_2} - e^{t_m}} \right) + \left(\frac{1}{3} e^{-(t_2-t_m)} \right) \right] \\
 &+ \left. \delta_3 \left[(-e^{-(t_1-t_m)}) \left(\frac{e^{t_1}(t_1 - t_m)}{e^{t_1} - e^{t_m}} \right) \left(\frac{1}{3} e^{-(t_1-t_m)} \right) \right] \right] \quad [7]
 \end{aligned}$$

Introgression occurs between B and C in our model, so B and C are sister in the parent trees that represent the two directions of introgression (see Supplementary Materials and Methods, Supplementary Figure 2). This means that these parent trees can each produce two gene trees with BC as sister species: one from lineage sorting and one from ILS. The contributions of these two gene trees in each parent tree are captured in the last two terms of equation 7. The first term corresponds to the contribution of ILS from the parent tree without introgression, i.e. equation 4.

Finally, for the covariance between A and C, we have

$$\begin{aligned}
 Cov(AC \mid ILS \text{ and } introgression) &= \sigma^2 \left[(1 - (\delta_2 + \delta_3)) \left(\frac{1}{3} e^{-(t_2-t_1)} \right) + \right. \\
 &\left. \delta_2 \left(\frac{1}{3} e^{-(t_2-t_m)} \right) + \delta_3 \left(\frac{1}{3} e^{-(t_1-t_m)} \right) \right] \quad [8]
 \end{aligned}$$

Since gene trees where A and C are sister can only be produced by ILS in our model, equation 8 is simply the sum of the gene trees with this topology produced by each of the three parent trees.

Lastly, we consider the expected trait variance with introgression. As with the covariances, we sum the total contribution of each gene tree within a parent tree, and then sum these contributions across each parent tree. All three share the same gene tree heights and therefore have the same expected variances. This gives:

$$\begin{aligned}
 Var(A) &= Var(B) = Var(C) \\
 &= \sigma^2 \left[(1 - (\delta_2 + \delta_3)) \left[(1 - e^{-(t_2-t_1)}) (t_2 + 1) + (e^{-(t_2-t_1)}) (t_2 + 1 + 1/3) \right] \right. \\
 &+ \delta_2 \left[(1 - e^{-(t_2-t_m)}) (t_2 + 1) + (e^{-(t_2-t_m)}) (t_2 + 1 + 1/3) \right] \\
 &+ \left. \delta_3 \left[(1 - e^{-(t_1-t_m)}) (t_1 + 1) + (e^{-(t_1-t_m)}) (t_1 + 1 + 1/3) \right] \right] \quad [9]
 \end{aligned}$$

The first term represents the contribution of the parent tree with no introgression, the same as in equation 5. The second two terms represent the contributions to the total variance from $C \rightarrow B$ and $B \rightarrow C$ introgression, respectively. When $\mathbf{T}$ is updated to include all these expectations, it becomes possible to model character states under Brownian motion while accounting for both ILS and introgression.

Testing for the effect of introgression on quantitative traits

To evaluate whether patterns of quantitative trait variation are consistent with a history of introgression, we use a simple test statistic that employs the same logic as the D_3 test for introgression (Hahn and Hibbins 2019; see also the f_3 statistic of Reich et al. 2009). Imagine that species A, B, and C have values q_1 , q_2 , and q_3 for a hypothetical quantitative trait, respectively. Given the species tree ((A,B),C), and assuming the Brownian motion model of trait evolution described in the previous sections, the expected distance between trait values q_2 and q_3 should be equal to the expected distance between q_1 and q_3 . This is because species C is equidistant to species A and B in the phylogeny, and this tree determines quantitative trait variances and covariances. The same relationship between distances is expected when considering the ILS-only model, because of symmetries in expected gene tree frequencies and branch lengths, and therefore in trait covariances (see equation 4).

However, introgression can introduce additional covariance between one pair of species, resulting in that pair having more similar trait values than the other non-sister pair (see equations 7 and 8). This naturally leads to the following test statistic:

$$Q_3 = \frac{|q_2 - q_3| - |q_1 - q_3|}{|q_2 - q_3| + |q_1 - q_3|} \quad [10]$$

The numerator of Q_3 takes the difference in trait distances between the two pairs of non-sister species; when there is no introgression, this numerator—and therefore Q_3 —has an expected value of 0. When a significant non-zero value of Q_3 is observed, the statistic is consistent with a history of introgression. In addition, the sign of the statistic can tell us which species were involved in introgression (but not the direction of introgression). For example, a negative Q_3 value would be consistent with introgression between species B and C, since that would result in q_2 and q_3 having more similar values (and therefore a smaller distance between them). The denominator of Q_3 is the sum of the two trait distances, which normalizes the statistic between 0 and 1, allowing it to be compared across traits with different mean values. We imagine that this statistic will be applied to many individual quantitative traits, each providing a separate value of Q_3 . The significance for a dataset consisting of many traits can then be evaluated either by testing for a mean value of Q_3 significantly different from 0, or by using a sign test with the null expectation that positive and negative Q_3 values should be equally frequent (see the analyses below for more details).

To confirm the effects of introgression predicted by the model, and the ability of Q_3 to detect it, we performed a power analysis. First, we contrasted two conditions: an ILS-only condition and an ILS + introgression condition (Figure 2). Both scenarios use the three-taxon tree described in previous sections, simulating quantitative traits as the sum of contributions of many genes (and therefore gene trees; see Methods). For 20,000 independent traits we calculated the mean and standard error of the difference in trait value at the tips of the tree between each pair of species (Figure 2). As predicted by our model, the taxa involved in introgression had a higher covariance and more similar trait values than the non-introgressing pair of taxa when averaging across the 20,000 traits (Figure 2).

Second, we performed a power analysis across 81 different parameter combinations: three values each of the rate and timing of introgression, the level of ILS, and the number of genes. We simulated 100 datasets for each set of parameters and asked how often Q_3 was significantly different from 0 in the direction predicted by introgression. We found the most important parameter to be the rate of introgression: at a rate of 1% (i.e. 1% of the genome has been introgressed), power was consistently low (1-6%) regardless of other simulation parameters (Figure 3, Supplementary Figure 1). At higher rates of introgression, power was increased when introgression was more recent relative to speciation, when the level of ILS was lower, and when more genes (traits) were considered. When 5,000 genes were used, power reached 67% under the best-case scenario (Supplementary Figure 1); this increased to 97% with 15,000 genes (Figure 3).

Gene expression variation is consistent with inferred histories of introgression in *Solanum*

To empirically test the effects of introgression across thousands of quantitative traits, we used previously published datasets from the wild tomato clade, *Solanum* section *Lycopersicon*. This clade includes the domesticated tomato, *S. lycopersicum*, and its 12 wild relatives, which have all speciated in the last 2.5 million years. The first dataset is a phylogenetic analysis of 29 accessions (i.e. populations) across these 13 tomato species and two outgroups (Pease et al. 2016). This dataset includes an introgression analysis based on D -statistics (Green et al. 2010, Durand et al. 2011) across all possible quartets, which provides a comprehensive overview of patterns of introgression in the clade. The second dataset is normalized quantitative expression of 14,556 genes expressed in ovules from eight accessions across seven tomato species. Expression levels for each gene are represented as reads per kilobase of transcript, per million mapped reads (RPKM). Samples were collected on the day of flower opening for 1-4 individuals of each species grown in a common greenhouse (Moyle et al. 2021).

Combining these two datasets, we sought to identify triplets of species with both evidence of introgression (from sequence data) and available gene expression data, so that we could apply the Q_3 statistic. Additionally, we wanted these triplets to vary in the magnitude of introgression, so that the magnitude of the effect of introgression on trait variation could be evaluated in addition to the presence or absence of an effect. With these considerations in mind, we identified two triplets. The first consists of the accessions LA3475 (*S. lycopersicum*), LA1589 (*S. pimpinellifolium*), and LA0715 (*S. pennellii*), with LA3475 and LA1589 as sister taxa, and evidence of introgression between LA1589 and LA0716 ($D = 0.057$, $P = 0.0015$, Pease et al. 2016) (Figure 4A). Using the D_p statistic (Hamlin et al. 2020) on site pattern counts from Pease et al., we obtained a value of 0.0013, corresponding to a genomic rate of introgression of 0.13%. We hereafter refer to this triplet as the “low” triplet because of the relatively low observed rate of introgression. The other triplet consists of LA3778 (*S. pennellii*), LA1777 (*S. habrochaites*), and LA1316 (*S. chmielewskii*), with LA3778 and LA1777 as sister taxa, and significant introgression between LA1777 and LA1316 ($D = 0.135$, $P = 2.34 \times 10^{-35}$, Pease et al. 2016) (Figure 4A). We obtained a D_p value of 0.0744 for this triplet, corresponding to a rate of introgression of 7.44%; this value is likely an underestimate, as D_p tends to underestimate the true value at higher rates of

introgression (Hamlin et al. 2020). As the rate of introgression is much higher for this triplet, we refer to it as the “high” triplet.

We used expression values from 14,556 genes available in both the low and high triplets. For each gene we calculated a separate value Q_3 , averaging across genes to obtain a mean value for each triplet. We obtained transcriptome-wide mean Q_3 values of -0.012 and -0.019 for the low and high triplet, respectively (Figure 4B). The values we observe are consistent with the histories of introgression inferred from the sequence data in both sign and magnitude. Both triplets have negative values, which is consistent with introgression between *S. pimpinellifolium* and *S. pennellii* in the low triplet, and between *S. habrochaites* and *S. chmielewskii* in the high triplet (see Figure 4A for the accessions assigned as q_1 , q_2 , and q_3 in each triplet). The Q_3 value is also more negative in the high triplet, which is consistent with the higher level of introgression inferred from sequence data.

The signal of introgression from quantitative traits was also statistically significant in both triplets, using either method for assessing significance. Using a bootstrapping approach to ask whether the mean values were different from 0 (see Methods), we obtained $P = 0.0012$ and $P < 0.0001$ for the low and high triplets, respectively (Figure 4B). We obtained similar results when testing for a significant excess of either positive or negative Q_3 values at individual genes (Figure 4C; see Methods). For the low triplet, we observed 7432 negative and 7124 positive genes ($P = 0.0134$); for the high triplet, 7533 negative and 7020 positive genes ($P < 0.0001$). Again, the larger number of negative Q_3 values in the high triplet is consistent with a higher amount of introgression.

Gene-level analysis of expression data

The expression level of genes can be affected by either *cis*-acting or *trans*-acting variants. Because *cis*-acting variants are most often found near the gene they affect (Wray et al. 2003, Hill et al 2020), we might expect these regulatory elements to share the same local gene tree topology as the nearby genic protein-coding region. While recombination either before or after introgression will uncouple the tree topology in the regulatory region from that in the coding region, we might expect to see an association between patterns of similarity in expression levels and patterns of gene tree discordance if *cis*-acting variants are common.

To test for such a relationship, we looked for an association between coding-region tree topologies and expression similarity among species in both triplets. Using trees estimated from each protein-coding gene (Pease et al. 2016), we identified 11,061 genes for which both the tree topology and expression values from all species were available. For each gene, we obtained the rooted tree topology for the relevant triplet and also determined which pair of species was most similar in expression value. We assume that expression similarity reflects the local topology at whichever locus has the largest effect on expression, such that the most similar pair of species represents the sister species in this topology.

In the low triplet, we found no significant relationship ($P = 0.776$, χ^2 test of independence) between protein-coding gene tree topology and expression similarity (Figure 5A). In the high triplet, however, we did observe a significant relationship ($P = 0.019$, Figure 5B). For gene trees

with a topology consistent with introgression (where *S. habrochaites* and *S. chmielewskii* are sister), there were significantly more genes where expression was also most similar between these species than expected by chance (476 observed vs. 449 expected). In other words, we found that gene expression similarity is correlated with the tree topology of protein-coding genes in the high triplet, in a fashion consistent with *cis*-acting effects of introgressed variation on expression (see Discussion for caveats).

Discussion

Phylogenetic comparative methods have revealed a great deal about the origins of trait variation among species. However, the rampant gene tree discordance uncovered in many phylogenomic studies paints a more complicated picture of the shared history among species. To date, most models of trait evolution employed by comparative methods have assumed that only the species phylogeny contributes to trait covariance, and have ignored covariance due to discordant gene trees. Our updated model builds on previous work (Mendes et al. 2018, Bastide et al. 2018) to incorporate both ILS and introgression into a single framework that captures the most common causes of discordance. We show that introgression leads to more discordance and stronger patterns of covariance in quantitative traits among non-sister species than ILS alone, paralleling results for binary traits under the same multispecies network coalescent framework (Hibbins et al. 2020). However, our model comes with several assumptions that should be addressed further, as well as implications for the analysis of quantitative traits.

Our model makes several assumptions and simplifications related to expected levels of genetic covariance between species. We have modeled post-speciation introgression as an instantaneous pulse of exchange between a single pair of non-sister species. Many other possible introgression scenarios are possible, such as multiple pulses or continuous periods of gene flow. Although each of these scenarios will increase the variance in gene tree topologies, we expect that they will still leave a detectable signature on quantitative traits because they still lead to gene tree asymmetries. Other gene flow scenarios—such as introgression between sister taxa, or between both pairs of non-sister taxa in a triplet at equal rates—will not result in a detectable signature of gene tree asymmetry. We have also assumed that the expected frequencies and coalescence times of loci contributing to trait variation follow neutral expectations. Through a local reduction in N_e , directional selection may reduce the rate of gene tree discordance due to ILS, while increasing the rate of discordance due to introgression (Pease and Hahn 2013, Munch et al. 2016, Martin et al. 2019). We show in our power analysis that lower rates of ILS relative to introgression allow for greater power to detect a signal of introgression in quantitative traits. This implies that selection, especially on introgressed variants (e.g. Setter et al. 2020), will make it more likely for quantitative traits to covary between non-sister taxa.

We also make key assumptions about the model of trait evolution. Our model assumes that traits evolve under a Brownian motion process, rather than alternative processes such as the Ornstein-Uhlenbeck (OU) (Hansen 1997) or early-burst (Simpson 1944, Blomberg et al. 2003) models. While it may be uncommon for traits to evolve according to an early-burst model (Harmon et al. 2010), many quantitative characters are likely to be constrained in some way, which can be modelled by the OU process. For gene expression in particular, evidence suggests that over long

phylogenetic timescales the OU process is a better fit to the data (Bedford and Hartl 2009, Catalán et al. 2019, Chen et al. 2019). However, multiple non-biological factors may favor the fit of OU models over Brownian motion, including small amounts of error in measured quantitative traits (Cooper et al. 2016). While we do not expect the model of trait evolution to affect asymmetries between species in thousands of traits, future work incorporating additional models of trait evolution, and their effect on trait covariances in particular, would be useful.

A key assumption of our statistical analysis is that each gene expression trait evolves independently. However, many genes show correlated patterns of expression, either because of locally shared *cis*-acting elements or because of *trans*-acting factors that affect the expression of many genes across the genome (Wray et al. 2003, Hill et al 2020). If, for instance, such a *trans*-acting factor is introgressed and affects many genes in a similar way, then treating each gene as an independent observation would constitute pseudoreplication of measurements. However, there are a few pieces of evidence that suggest this is not a major problem here. First, previous data from experimental introgression lines between *S. lycopersicum* and *S. pennellii* are not consistent with a large role of introgressed loci on background gene expression: Guerrero et al. (2016) found that each introgressed gene had downstream effects on the expression of only 0.4 genes on average. Second, we find here that the number of genes where expression is more similar between introgressing species is higher in the triplet with a higher rate of introgression. This is again consistent with largely local effects of each introgressed locus on gene expression. Based on these observations, we conclude that we likely have many thousands of independent data points testing the relationship between introgression and expression variation, even if the true correlation structure is unknown.

Our analysis of gene expression is consistent with the idea that introgression between wild tomato species has broadly influenced the evolution of gene expression. An alternative explanation is that species with more similar gene expression may be more likely to introgress, possibly due to reduced negative fitness consequences from hybrid dysregulation. There are again a number of pieces of evidence that argue against the latter interpretation. Guerrero et al. (2016) found no evidence for an association between the magnitude of differential expression between tomato introgression lines and the sterility of hybrids. While those experiments were limited to early-generation hybrids grown in a greenhouse, they do not indicate that general expression levels are a barrier to introgression. Furthermore, here we observe a correlation between expression similarity at specific genes and the tree topology inferred from their protein-coding sequences (Figure 5B). This association suggests a direct causal role of introgressed genes on gene expression: *cis*-regulatory differences at introgressed loci lead to a relationship between local tree topologies and expression levels (cf. Scally et al. 2012). Such a relationship is highly unlikely to instead be due to a barrier to introgression. The fact that we do not observe the same correlation in the "low" triplet (Figure 5A) could be due either to a comparative lack of statistical power in this triplet, or due to more recombination between the protein-coding regions the tree topologies were inferred from and the *cis*-regulatory regions driving expression. Introgression will reduce the opportunities for recombination, which could explain why the "high" triplet retains a higher signal. Alternatively, it may be that *trans*-acting variation is much more common in this triplet, a scenario that would not lead to an association between local gene

tree topologies and local gene expression. We cannot definitively distinguish among these possibilities given only the data presented here. Finally, it is possible that some form of experimental bias—for instance, non-sister species grown closer together in the greenhouse—could be responsible for asymmetries in many traits. While this is always a concern with quantitative traits, we note that the sister species in both triplets examined here always show the greatest similarity in gene expression (Supplementary Tables 1 and 2). The association we observe between tree topologies and expression similarity at individual genes is also inconsistent with a general experimental bias.

Overall, our results demonstrate both theoretically and empirically that introgression can affect patterns of quantitative trait evolution. While considerable attention and excitement has justifiably been devoted to the power of introgression as an evolutionary force shaping trait variation, this is a double-edged sword, as most phylogenetic comparative methods do not account for gene tree discordance. Previous work has shown that discordance due solely to ILS can lead to overestimates of the rate of quantitative trait evolution and to underestimates of phylogenetic signal (Mendes et al. 2018). The effects of introgression in misleading our inferences will be worse, as it both increases overall discordance and generates asymmetries in trait sharing. Modern phylogenetic comparative methods should strive to account for the consequences of gene tree discordance, in order to paint a more accurate picture of how quantitative traits evolve among species.

Materials and Methods

Description of datasets

We use ovule gene expression data that is described in Moyle et al. (2021). The dataset consists of normalized quantitative expression for 14,556 genes measured in eight accessions across seven species. We used six accessions across five of these species for our analyses (two different accessions of *S. pennellii* were used in the two triplets). For each accession, samples were collected on the day of flower opening for 1-4 biological replicates (individual plants) grown in a common greenhouse. When applicable, we took the average expression value across replicates within each accession for our analyses. Raw sequencing reads for this dataset are available on the SRA under BioProject PRJNA714065. The dataset containing normalized expression for each replicate, in addition to the scripts for all analyses, are available from https://github.com/mhibbins/intro_quant_traits.

We use phylogenomic data that is described in Pease et al. (2016). The dataset consists of transcriptomes from 29 accessions across 13 species, including the six accessions used in our analyses. Pease et al. used MVFtools to estimate transcriptome-wide *D*-statistics for all possible rooted triplets (2925 total values) across the 27 ingroup accessions. From this dataset we selected the two triplets to use in our analyses. Pease et al. also inferred gene trees for each individual protein-coding region (19,116 genes total) using *RAxML* (Stamatakis 2014); we used this data in our gene-level analyses. Both datasets are published in the Dryad repository <https://doi.org/10.5061/dryad.182dv>.

Simulation of quantitative traits & power analyses

We simulated the effect of introgression on quantitative trait values (as shown in Figure 2) under two models: an ILS-only model and a model with ILS and introgression. For the ILS-only model, we used values of 1 and 1.3 for the speciation time of A and B, and the speciation of C from the ancestor of A and B, respectively (all in units of $2N$ generations). The introgression condition maintained the same speciation times, with the addition of an introgression event from C into B at a time of 0.5, with $\delta_2 = 0.1$. Using these parameters, we used our model to construct expected variance/covariance matrices with $\sigma^2 = 1$ using a custom R function (script available at [zzzz](#)). We then simulated trait values by drawing from a multivariate normal distribution using the R function *mvrnorm* with means of 0 and the constructed matrices.

We performed a power analysis to assess the statistical power of Q_3 . Using the simulation approach described above, we simulated 100 trait datasets under all combinations of the following parameters: 5000, 10000, and 15000 for the number of genes; 0.1, 0.5, and 1 for $t_2 - t_1$; 0.1, 0.25, and 0.5 for $t_1 - t_m$; and 0.01, 0.05, and 0.1 for the rate of introgression. We evaluated significance for each dataset using a one-sample t -test with $H_0: Q_3 = 0$. A result was considered a true positive for our analysis when $P < 0.05$ and the sign of the mean simulated Q_3 value was consistent with the simulated history of introgression.

Testing quantitative traits for introgression

We calculated average expression values across individual replicates of each accession before estimating Q_3 for each gene. To assess the significance of both our estimated Q_3 means and signs, we used bootstrap-resampling. For the mean Q_3 values, we tested the null hypothesis of $Q_3 = 0$ by randomly sampling 10,000 datasets of 14,556 genes each with replacement from the empirical gene expression dataset, and estimating the mean value of each. We assessed the rank i of the observed Q_3 values among these resampled datasets, and a two-tailed P -value was estimated using the following formula:

$$P = 1 - 2 * |0.5 - i|$$

For the sign of individual genes' Q_3 values, we tested the null hypothesis that the number of negative and positive signs are equal by randomly sampling 10,000 datasets of 14,556 genes each. For each resampled dataset we counted the number of negative and positive Q_3 values, ranking the datasets from the one with the greatest excess of negative values to the greatest excess of positive values. The rank of the observed data against these resampled datasets was calculated, and two-tailed P -values were evaluated using the same formula as above.

For the analysis of the relationship between gene-level tree topology and expression similarity, we made use of gene trees inferred using *RAxML* by Pease et al. (2016). We used the Python package *ete3* (Huerta-Cepas et al. 2016) to prune these gene trees down to the accessions involved in our test triplets. We then obtained the overlapping set of genes for which both topologies and expression data were available, and recorded the expression “topology” based on the minimum pairwise distance in expression values. The counts of gene tree topology and

expression topology were placed into a 3x3 contingency table for each triplet, and we tested for a significant association using a χ^2 test of independence.

Acknowledgements

We thank Leonie Moyle and Matthew Gibson for sharing data, and for comments on the manuscript. This work was supported by a grant from the National Science Foundation (DEB-1936187).

Figures

Figure 1: Modelling quantitative trait evolution under the combined effects of ILS and introgression. 1) From a phylogenetic network with known parameters, the multispecies network coalescent model can be used to predict the expected frequency and branch lengths of each gene tree topology. 2) These gene trees contribute to trait covariances through their internal branches, and to trait variances through their total heights. The contribution of each gene tree to the overall quantities in T is weighted by its expected frequency. 3) Once the values of T are estimated, character states under Brownian motion can be simulated by drawing from a multivariate normal with a mean of 0 and variance of $\sigma^2 T$.

Figure 2: Quantifying the effect of introgression on quantitative trait variation. For ILS-only (top row) and ILS + introgression (bottom row) conditions, we show the expected variance/covariance matrix (middle-left column, variances not shown for clarity) and the average difference in quantitative trait values between each pair of species across 20,000 simulated traits (middle-right column). The expectations for the Q_3 statistic are also shown (far-right column).

Figure 3: Power analysis of the ability of Q_3 to detect a signature of introgression from 15,000 simulated genes ($\sigma^2 = 1$). Each cell reports the proportion of 100 simulated datasets where Q_3 was significantly different from 0 in the direction expected from the simulated history of introgression. Within each matrix, the x-axis is the time of introgression relative to speciation (larger values mean relatively more recent introgression), and the y-axis is the rate of introgression. There is one matrix for each of three times between speciation events, which determine the levels of ILS (decreasing from left to right, as the times increase). The greatest power comes in scenarios with little ILS, high rates of introgression, and recent introgression events.

*Figure 4: Ovule gene expression variation in tomatoes is consistent with inferred histories of introgression. A) Histories of speciation and introgression for our chosen triplets in *Solanum*. B) Mean and standard error of Q_3 across all genes in each triplet. C) Difference in the number of genes with a negative vs. positive Q_3 value for both triplets. Density plots show the distribution of this difference across 10,000 bootstrapped datasets. Observed values for the two triplets relative to the bootstrap distributions are shown with arrows.*

A) Low triplet

		Pattern of gene expression similarity	
Gene tree topology

O: 32 E: 34.8	O: 35 E: 32.28
	O: 22 E: 18.7	O: 18 E: 17.3

B) High triplet

		Pattern of gene expression similarity	
Gene tree topology

O: 476 E: 449.1	O: 404 E: 399.1
	O: 173 E: 187.5	O: 150 E: 166.5

*Figure 5: Relationships between coding sequence tree topology (rows) and gene expression similarity (columns) in the low (A) and high (B) triplets. Note that for expression similarity, we did not explicitly construct trees from expression data—the tree representation is simply meant to depict observed expression distances. Only discordant trees and expression patterns are shown, but χ^2 *P*-values (0.776 and 0.019 for panels A and B, respectively) are reported from the full 3x3 table (see Supplementary Tables 1 and 2 for the full tables). The cases where both the tree topology and pattern of expression are consistent with the inferred history of introgression for that triplet are highlighted in blue. Each cell reports the observed number of genes (O) in each category, and the number expected (E) from the χ^2 distribution.*

References

1. Bastide P, Solís-Lemus C, Kriebel R, William Sparks K, Ané C. Phylogenetic comparative methods on phylogenetic networks with reticulations. *Systematic Biology*. 2018;67(5):800-20.
2. Bedford T, Hartl DL. Optimization of gene expression by natural selection. *Proceedings of the National Academy of Sciences of the United States of America*. 2009;106(4):1133-8.
3. Blomberg SP, Garland T, Jr., Ives AR. Testing for phylogenetic signal in comparative data: behavioral traits are more labile. *Evolution*. 2003;57(4):717-45.
4. Brandvain Y, Kenney AM, Flagel L, Coop G, Sweigart AL. Speciation and introgression between *Mimulus nasutus* and *Mimulus guttatus*. *PLoS Genetics*. 2014;10(6):e1004410.
5. Brawand D, Soumillon M, Necsulea A, Julien P, Csardi G, Harrigan P, et al. The evolution of gene expression levels in mammalian organs. *Nature*. 2011;478(7369):343-8.
6. Catalan A, Briscoe AD, Hohna S. Drift and directional selection are the evolutionary forces driving gene expression divergence in eye and brain tissue of *Heliconius* butterflies. *Genetics*. 2019;213(2):581-94.
7. Chen J, Swofford R, Johnson J, Cummings BB, Rogel N, Lindblad-Toh K, et al. A quantitative framework for characterizing the evolutionary history of mammalian gene expression. *Genome Research*. 2019;29(1):53-63.
8. Cooper N, Thomas GH, Venditti C, Meade A, Freckleton RP. A cautionary note on the use of Ornstein Uhlenbeck models in macroevolutionary studies. *Biological Journal of the Linnean Society*. 2016;118(1):64-77.
9. Davidson RM, Gowda M, Moghe G, Lin H, Vaillancourt B, Shiu SH, et al. Comparative transcriptomics of three *Poaceae* species reveals patterns of gene expression evolution. *The Plant Journal*. 2012;71(3):492-502.
10. Degnan JH. Modeling hybridization under the network multispecies coalescent. *Systematic Biology*. 2018;67(5):786-99.
11. Degnan JH, Rosenberg NA. Gene tree discordance, phylogenetic inference and the multispecies coalescent. *Trends in Ecology and Evolution*. 2009;24(6):332-40.
12. Durand EY, Patterson N, Reich D, Slatkin M. Testing for ancient admixture between closely related populations. *Molecular Biology and Evolution*. 2011;28(8):2239-52.
13. Felsenstein J. Maximum-likelihood estimation of evolutionary trees from continuous characters. *American Journal of Human Genetics*. 1973;25(5):471-92.
14. Fontaine MC, Pease JB, Steele A, Waterhouse RM, Neafsey DE, Sharakhov IV, et al. Extensive introgression in a malaria vector species complex revealed by phylogenomics. *Science*. 2015;347(6217):1258524.

15. Green RE, Krause J, Briggs AW, Maricic T, Stenzel U, Kircher M, et al. A draft sequence of the Neandertal genome. *Science*. 2010;328(5979):710-22.
16. Guerrero RF, Posto AL, Moyle LC, Hahn MW. Genome-wide patterns of regulatory divergence revealed by introgression lines. *Evolution*. 2016;70(3):696-706.
17. Hahn MW, Hibbins MS. A three-sample test for introgression. *Molecular Biology and Evolution*. 2019;36(12):2878-82.
18. Hahn MW, Nakhleh L. Irrational exuberance for resolved species trees. *Evolution*. 2016;70(1):7-17.
19. Hamlin JAP, Hibbins MS, Moyle LC. Assessing biological factors affecting postspeciation introgression. *Evolution Letters*. 2020;4(2):137-54.
20. Hansen TF. Stabilizing selection and the comparative analysis of adaptation. *Evolution*. 1997;51(5):1341-51.
21. Harmon LJ, Losos JB, Jonathan Davies T, Gillespie RG, Gittleman JL, Bryan Jennings W, et al. Early bursts of body size and shape evolution are rare in comparative data. *Evolution*. 2010;64(8):2385-96.
22. Hibbins MS, Gibson MJ, Hahn MW. Determining the probability of hemiplasy in the presence of incomplete lineage sorting and introgression. *eLife*. 2020;9:e63753
23. Hibbins MS, Hahn MW. The timing and direction of introgression under the multispecies network coalescent. *Genetics*. 2019;211(3):1059-73.
24. Hill MS, Vande Zande P, Wittkopp PJ. Molecular and evolutionary processes generating variation in gene expression. *Nature Reviews Genetics*. 2020;22:203-215.
25. Hime PM, Lemmon AR, Lemmon ECM, Prendini E, Brown JM, Thomson RC, et al. Phylogenomics reveals ancient gene tree discordance in the amphibian tree of life. *Systematic Biology*. 2021;70(1):49-66.
26. Hobolth A, Dutheil JY, Hawks J, Schierup MH, Mailund T. Incomplete lineage sorting patterns among human, chimpanzee, and orangutan suggest recent orangutan speciation and widespread selection. *Genome Research*. 2011;21(3):349-56.
27. Hudson RR. Testing the constant-rate neutral allele model with protein sequence data. *Evolution*. 1983;37(1):203-17.
28. Huerta-Cepas J, Serra F, Bork P. ETE 3: Reconstruction, analysis, and visualization of phylogenomic data. *Molecular Biology and Evolution*. 2016;33(6):1635-8.
29. Huerta-Sanchez E, Jin X, Asan, Bianba Z, Peter BM, Vinckenbosch N, et al. Altitude adaptation in Tibetans caused by introgression of Denisovan-like DNA. *Nature*. 2014;512(7513):194-7.

30. Jones MR, Mills LS, Alves PC, Callahan CM, Alves JM, Lafferty DJR, et al. Adaptive introgression underlies polymorphic seasonal camouflage in snowshoe hares. *Science*. 2018;360(6395):1355-8.
31. Liu KJ, Dai J, Truong K, Song Y, Kohn MH, Nakhleh L. An HMM-based comparative genomic framework for detecting introgression in eukaryotes. *PLoS Computational Biology*. 2014;10(6):e1003649.
32. Mallet J, Besansky N, Hahn MW. How reticulated are species? *Bioessays*. 2016;38(2):140-9.
33. Martin SH, Davey JW, Salazar C, Jiggins CD. Recombination rate variation shapes barriers to introgression across butterfly genomes. *PLoS Biology*. 2019;17(2):e2006288.
34. Mendes FK, Fuentes-Gonzalez JA, Schraiber JG, Hahn MW. A multispecies coalescent model for quantitative traits. *eLife*. 2018;7:e36482
35. Meng C, Kubatko LS. Detecting hybrid speciation in the presence of incomplete lineage sorting using gene tree incongruence: a model. *Theoretical Population Biology*. 2009;75(1):35-45.
36. Moyle LC, Wu M, Gibson MJS. Reproductive proteins evolve faster than non-reproductive proteins among *Solanum* species. *Frontiers in Plant Science*. 2021;12:635990.
37. Munch K, Nam K, Schierup MH, Mailund T. Selective sweeps across twenty millions years of primate evolution. *Molecular Biology and Evolution*. 2016;33(12):3065-74.
38. Pamilo P, Nei M. Relationships between gene trees and species trees. *Molecular Biology and Evolution*. 1988;5(5):568-83.
39. Pardo-Diaz C, Salazar C, Baxter SW, Merot C, Figueiredo-Ready W, Joron M, et al. Adaptive introgression across species boundaries in *Heliconius* butterflies. *PLoS Genetics*. 2012;8(6):e1002752.
40. Pease JB, Haak DC, Hahn MW, Moyle LC. Phylogenomics reveals three sources of adaptive variation during a rapid radiation. *PLoS Biology*. 2016;14(2):e1002379.
41. Pease JB, Hahn MW. More accurate phylogenies inferred from low-recombination regions in the presence of incomplete lineage sorting. *Evolution*. 2013;67(8):2376-84.
42. Pollard DA, Iyer VN, Moses AM, Eisen MB. Widespread discordance of gene trees with species tree in *Drosophila*: evidence for incomplete lineage sorting. *PLoS Genetics*. 2006;2(10):e173.
43. Reich D, Thangaraj K, Patterson N, Price AL, Singh L. Reconstructing Indian population history. *Nature*. 2009;461(7263):489-94.
44. Rifkin SA, Kim J, White KP. Evolution of gene expression in the *Drosophila melanogaster* subgroup. *Nature Genetics*. 2003;33(2):138-44.

45. Sankararaman S, Mallick S, Dannemann M, Prufer K, Kelso J, Paabo S, et al. The genomic landscape of Neanderthal ancestry in present-day humans. *Nature*. 2014;507(7492):354-7.
46. Scally A, Dutheil JY, Hillier LW, Jordan GE, Goodhead I, Herrero J, et al. Insights into hominid evolution from the gorilla genome sequence. *Nature*. 2012;483(7388):169-75.
47. Schumer M, Xu C, Powell DL, Durvasula A, Skov L, Holland C, et al. Natural selection interacts with recombination to shape the evolution of hybrid genomes. *Science*. 2018;360(6389):656-60.
48. Setter D, Mousset S, Cheng X, Nielsen R, DeGiorgio M, Hermisson J. VolcanoFinder: Genomic scans for adaptive introgression. *PLoS Genetics*. 2020;16(6):e1008867.
49. Simpson GG. Tempo and mode in evolution. New York: Columbia University Press; 1944. 237 p.
50. Stamatakis A. RAxML version 8: a tool for phylogenetic analysis and post-analysis of large phylogenies. *Bioinformatics*. 2014;30(9):1312-3.
51. Taylor SA, Larson EL. Insights from genomes into the evolutionary importance and prevalence of hybridization in nature. *Nature Ecology and Evolution*. 2019;3(2):170-7.
52. Vanderpool D, Minh BQ, Lanfear R, Hughes D, Murali S, Harris RA, et al. Primate phylogenomics uncovers multiple rapid radiations and ancient interspecific introgression. *PLoS Biology*. 2020;18(12):e3000954.
53. Wang Y, Cao Z, Ogilvie HA, Nakhleh L. Phylogenomic assessment of the role of hybridization and introgression in trait evolution. *BioRxiv*. 2020.
54. Wen D, Yu Y, Nakhleh L. Bayesian inference of reticulate phylogenies under the multispecies network coalescent. *PLoS Genetics*. 2016;12(5):e1006006.
55. White MA, Ané C, Dewey CN, Larget BR, Payseur BA. Fine-scale phylogenetic discordance across the house mouse genome. *PLoS Genetics*. 2009;5(11):e1000729.
56. Whitney KD, Randell RA, Rieseberg LH. Adaptive introgression of herbivore resistance traits in the weedy sunflower *Helianthus annuus*. *The American Naturalist*. 2006;167(6):794-807.
57. Wray GA, Hahn MW, Abouheif E, Balhoff JP, Pizer M, Rockman MV, et al. The evolution of transcriptional regulation in eukaryotes. *Molecular Biology and Evolution*. 2003;20(9):1377-419.
58. Wu M, Kostyun JL, Hahn MW, Moyle LC. Dissecting the basis of novel trait evolution in a radiation with widespread phylogenetic discordance. *Molecular Ecology*. 2018.
59. Zhang W, Dasmahapatra KK, Mallet J, Moreira GR, Kronforst MR. Genome-wide introgression among distantly related *Heliconius* butterfly species. *Genome Biology*. 2016;17:25.

Supplementary Materials and Methods for Hibbins & Hahn 2021

Derivation of expected trait variances and covariances under the multispecies network coalescent

As discussed in the methods, we assume a rooted three-taxon tree with the topology ((A,B),C) (Figure 1). In coalescent units of $2N$ generations, A and B speciate at time t_1 , and C speciates from the ancestor of A and B at time t_2 . An instantaneous introgression event between species B and C occurs at time t_m . This may occur from C into B at a rate of δ_2 , and/or from B into C at a rate of δ_3 . These rates denote the probability that a locus has the specified introgression history. Each possible history generates a “parent tree” for the locus, within which incomplete lineage sorting occurs according to the multispecies coalescent model. We denote these parent trees 1, 2, and 3 for the history of no introgression, C into B introgression, and B into C introgression, respectively.

For each pair of species, the expected phylogenetic covariance is the weighted average of expected internal branch lengths across all gene trees where that species pair shares a subtending internal branch. This gives the following general expression:

$$E[cov(X, Y)] = \sum_{\tau_s} p_h p(\tau_{s,i}) L_{internal}(\tau_{s,i}) \quad [1]$$

Where p_h is the probability of the parent tree relevant to the gene tree of interest, $p(\tau_{s,i})$ is the probability of the gene tree $\tau_{s,i}$, and $L_{internal}(\tau_{s,i})$ is the expected internal branch length of that gene tree. This product is summed across the subset of gene trees τ_s where species X and Y share an internal branch.

For three taxa, the exact expectations for these gene tree frequencies, and expected coalescence times within them, are known (Hibbins and Hahn 2019). The expected internal branch lengths are then simply the difference of the two expected coalescence times for each gene tree. We begin with the species pair AB, which share an internal branch in four gene trees: one the result of lineage sorting at non-introgressed loci, and the others the result of incomplete lineage sorting in each of the three possible parent trees. These gene trees will be denoted $AB1_1$, $AB2_1$, $AB2_2$, and $AB3$. In this notation, the subscript denotes the parent tree from which the gene tree originates, while the non-subscripted number indicates whether the tree is the result of lineage sorting (1) or incomplete lineage sorting (2) for topologies where both are possible. For the first two terms, we have:

$$p(AB1_1) = 1 - e^{-(t_2-t_1)} \quad [2]$$

$$L_{internal}(AB1_1) = [t_2 + 1] - \left[t_1 + \left(1 - \frac{t_2 - t_1}{e^{t_2-t_1} - 1} \right) \right] = \frac{e^{t_2}(t_2 - t_1)}{e^{t_2} - e^{t_1}} \quad [3]$$

$$p(AB2_1) = \frac{1}{3} e^{-(t_2-t_1)} \quad [4]$$

$$L_{internal}(AB2_1) = \left[t_2 + \frac{1}{3} + 1 \right] - \left[t_2 + \frac{1}{3} \right] = 1 \quad [5]$$

Note in equation 5 that the expected internal branch length is 1 coalescent unit. This holds true for any gene tree produced by incomplete lineage sorting. For gene tree AB_2 , which comes from a history of C into B introgression, the lower bound to coalescence is t_m rather than t_1 , giving the following:

$$p(AB_2) = \frac{1}{3} e^{-(t_2-t_m)} \quad [7]$$

$$L_{internal}(AB_2) = 1 \quad [8]$$

In parent tree 3 (B into C introgression), C traces its ancestry through B going backwards in time. This allows C to coalesce with A after t_1 , rather than t_2 . For the gene tree AB_3 , this gives:

$$p(AB_3) = \frac{1}{3} e^{-(t_1-t_m)} \quad [9]$$

$$L_{internal}(AB_3) = 1 \quad [10]$$

By applying equations 2-10 to the general formulation of equation 1 (and then simplifying), we obtain the expected trait covariance between A and B (equation 6 of the main text).

For the species pair BC, there are five gene trees where the internal branch is shared. Two are the result of lineage sorting at introgressed loci, and the others are the result of incomplete lineage sorting at either introgressed or non-introgressed loci. These will be denoted $BC1_2$, $BC1_3$, $BC2_2$, $BC2_3$, and $BC1_1$, respectively. The expected gene tree frequencies and branch lengths often mirror those for the AB species pair, but with t_m in the place of t_1 . From this we obtain the following equations:

$$p(BC1_2) = 1 - e^{-(t_2-t_m)} \quad [11]$$

$$L_{internal}(BC1_2) = [t_2 + 1] - \left[t_m + \left(1 - \frac{t_2 - t_m}{e^{t_2-t_m} - 1} \right) \right] = \frac{e^{t_2}(t_2 - t_m)}{e^{t_2} - e^{t_m}} \quad [12]$$

$$p(BC1_3) = 1 - e^{-(t_1-t_m)} \quad [13]$$

$$L_{internal}(BC1_3) = [t_1 + 1] - \left[t_m + \left(1 - \frac{t_1 - t_m}{e^{t_1-t_m} - 1} \right) \right] = \frac{e^{t_1}(t_1 - t_m)}{e^{t_1} - e^{t_m}} \quad [14]$$

$$p(BC2_2) = \frac{1}{3} e^{-(t_2-t_m)} \quad [15]$$

$$p(BC2_3) = \frac{1}{3} e^{-(t_1-t_m)} \quad [16]$$

$$p(BC1_1) = \frac{1}{3} e^{-(t_2-t_1)} \quad [17]$$

$$L_{internal}(BC_2) = L_{internal}(BC_3) = L_{internal}(BC_1) = 1 \quad [18]$$

Applying equations 11 through 18 to equation 1 and then simplifying, we obtain the expected trait covariance between B and C (equation 7 of the main text).

Finally, for the species pair AC, there are three possible gene trees where these species share an internal branch, produced by incomplete lineage sorting within each of the three parent trees (since we do not model introgression between this pair here). These are dubbed AC_1 , AC_2 , and AC_3 for the trees produced by parent trees 1, 2, and 3, respectively. For the expected gene tree frequencies and branch lengths, we have:

$$p(AC_1) = \frac{1}{3} e^{-(t_2-t_1)} \quad [19]$$

$$p(AC_2) = \frac{1}{3} e^{-(t_2-t_m)} \quad [20]$$

$$p(AC_3) = \frac{1}{3} e^{-(t_1-t_m)} \quad [21]$$

$$L_{internal}(AC_1) = L_{internal}(AC_2) = L_{internal}(AC_3) = 1 \quad [22]$$

Equations 19-22 applied to equation 1 and then simplified give us the expected trait covariance between A and C (equation 8 of the main text).

Finally, we consider the expected trait variance. Under Brownian motion, this variance is simply the total height of the tree from the root to the relevant tip. To obtain the expected variance with introgression, we take the sum of this height across all gene trees, weighted by their probability. Concordant trees produced by lineage sorting have a total height of $t_2 + 1$, and all other gene trees have a height of $t_2 + 1 + 1/3$. Owing to this consistency in expected gene tree heights, all three species have the same expected trait variances. To get these heights we have to consider the contribution of gene trees from all three parent trees. For parent tree 1, this variance is:

$$\begin{aligned} E[\text{var}(\text{Gene trees}|\text{parent tree 1})] \\ = [(1 - e^{-(t_2-t_1)})(t_2 + 1)] + [e^{-(t_2-t_1)}(t_2 + 1 + 1/3)] \end{aligned} \quad [23]$$

For parent tree 2:

$$\begin{aligned} E[\text{var}(\text{Gene trees}|\text{parent tree 2})] \\ = [(1 - e^{-(t_2-t_m)})(t_2 + 1)] + [e^{-(t_2-t_m)}(t_2 + 1 + 1/3)] \end{aligned} \quad [24]$$

And for parent tree 3:

$$\begin{aligned} E[\text{var}(\text{Gene trees}|\text{parent tree 3})] \\ = [(1 - e^{-(t_1-t_m)})(t_1 + 1)] + [e^{-(t_1-t_m)}(t_1 + 1 + 1/3)] \end{aligned} \quad [25]$$

Summing equations 23-25, weighted by the probabilities of their respective parent trees, gives equation 9 of the main text, the expected trait variance of the three species.

Supplementary Figures and Tables

A) 5000 genes

A) 10,000 genes

Supplementary Figure 1: Power analysis results using (A) 5000 and (B) 10,000 genes.

Supplementary Figure 2: Modelling introgression using parent trees. Parent trees represent the possible histories of speciation and/or introgression at a locus, with their probabilities determined by the rate of introgression. Within each parent tree, gene trees sort according to the multispecies coalescent process. Adapted from Hibbins et al. (2020).

	Pattern of expression similarity				
Gene tree topology		P1P2	P1P3	P2P3	Sum
	P1P2	4249 (4245.1)	3193 (3195.4)	3450 (3450.5)	10892
	P1P3	19 (23.0)	22 (18.7)	18 (17.3)	110
	P2P3	43 (42.9)	32 (34.8)	35 (32.28)	59
	Sum	4311	3504	3246	

Supplementary Table 1: Full 3x3 contingency table for relationship between gene-level expression and local gene tree topology in the low triplet.

	Pattern of expression similarity				
Gene tree topology		P1P2	P1P3	P2P3	Sum
	P1P2	3237 (3236.3)	2821 (2809.3)	3149 (3161.4)	9207
	P1P3	223 (191.9)	150 (166.59)	173 (187.5)	546
	P2P3	428 (459.8)	404 (399.1)	476 (449.1)	1308
	Sum	3888	3375	3798	

Supplementary Table 2: Full 3x3 contingency table for relationship between gene-level expression and local gene tree topology in the high triplet.