1 Highly scaled measurements of *C. elegans* development suggest that physical 2 constraints guide growth trajectories and animal shape

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25 **Abstract**

26 Growth control establishes organism size, requiring mechanisms to sense and adjust growth. Studies of single
 27 cells revealed that size homeostasis uses distinct control methods: Size, Timer, and Adder. In multicellular
 28 organisms, mechanisms that regulate single cell growth must integrate control across organs and tissues
 29 during development to generate adult size and shape. We leveraged the roundworm *Caenorhabditis elegans*
 30 as a scalable and tractable model to collect precise growth measurements of thousands of individuals,
 31 measure feeding behavior, and quantify changes in animal size and shape. Using quantitative measurements
 32 and mathematical modeling, we propose two models of physical mechanisms by which *C. elegans* can control
 33 growth. First, constraints on cuticle stretch generate mechanical signals through which animals sense body
 34 size and initiate larval-stage transitions. Second, mechanical control of food intake drives growth rate within
 35 larval stages. These results suggest how physical constraints control developmental timing and growth rate in
 36 *C. elegans*.

37 Introduction

38 Growth is a complex process fundamental to development. Individual cells and whole animals must reach an
 39 appropriate size to remain competitive in their environment. A larger body size conveys many selective
 40 advantages to an organism, including increased predation success or defense against predation, increased
 41 success in mating, and increased success in intraspecific as well as interspecific competition. Offsetting these
 42 advantages, larger organisms require more food resources to grow, take longer to develop, and produce fewer
 43 offspring (Hone and Benton, 2005). Therefore, it is critical for multicellular organisms to effectively coordinate
 44 the growth of both individual cells and the whole body. Additionally, growth at both of these scales must be
 45 coupled with developmental progression to ensure the proper timing of irreversible developmental events.

46 In recent years, efforts have focused on understanding how organisms control growth to achieve size
 47 homeostasis (Björklund, 2019; Turner et al., 2012; Willis and Huang, 2017). Many of these studies are
 48 motivated by the decades-long debate about whether growth is linear or exponential; two separate models
 49 each having unique implications for size regulation. In a linear model with constant growth rate, smaller
 50 organisms must grow proportionally more than larger organisms to maintain size homeostasis. In this
 51 paradigm, organism size can be controlled simply by specifying growth duration. Subsequently, this method of
 52 growth control was named the ‘Timer’ model (Donnan and John, 1983; Wang et al., 2000). Instead of
 53 regulating growth duration, organisms can monitor size and adjust duration of growth to reach an optimal size,
 54 often named the ‘Sizer’ model (Pavelescu et al., 2018; Sveiczzer et al., 1996; Tzur et al., 2009). In an
 55 exponential model, growth rate is proportional to size. Here, a time-based control mechanism alone would fail
 56 to maintain size homeostasis because larger organisms would grow proportionally more during a specified
 57 period of time. This difference in growth requires a size-based control mechanism to ensure that growth is
 58 halted once a maximum size is reached. Although ‘Timer’ and ‘Sizer’ are the most often proposed size-control
 59 models, other models have been suggested, including ‘Adder’ in which a fixed volume is added to a cell or
 60 organism during growth (Campos et al., 2014; Taheri-Araghi et al., 2015), and ‘Folder’ in which the organism
 61 increases in volume by a fixed proportion (Towbin and Grosshans, 2021). It is not trivial to determine which

62 model most accurately describes growth of individual cells or whole organisms because quantitative
63 measurements of growth must be collected at high precision and throughput under tightly controlled
64 experimental conditions. In unicellular organisms, the development of high-throughput experimental techniques
65 in combination with theoretical models have advanced the understanding of size control (Cadart et al., 2018;
66 Jorgensen and Tyers, 2004; Osella et al., 2014; Soifer et al., 2016; Wang et al., 2010). Progress has been
67 slower for multicellular organisms because cell growth within tissues and tissue growth within organisms often
68 progress at different rates, suggesting that they are likely not regulated in the same ways (Moss-Taylor et al.,
69 2019; Spence, 2009; Uppaluri et al., 2016).

70 The nematode *Caenorhabditis elegans* presents both a scalable and tractable multicellular animal model to
71 study growth control. With an adult body length of approximately 1 mm, hundreds of thousands of individuals
72 are easily cultured in controlled laboratory conditions (Wood, 1988). Moreover, *C. elegans* post-embryonic
73 development is marked by several molts that provide clear developmental milestones (Page and Johnstone,
74 2007a). Each molt is initiated by a period of inactivity (lethargus) and terminated once the animal successfully
75 sheds its collagen-rich outer cuticle (ecdysis) (Singh and Sulston, 1978). Four molts separate the *C. elegans*
76 life cycle into five distinct stages: four larval stages (L1-L4) and adult. The timing of these molts determines the
77 completion of stage-specific development (Monsalve et al., 2011; Zaidel-Bar et al., 2010) and underscores the
78 importance of growth regulation during *C. elegans* larval development.

79 A full description of an organism's development includes the assessment of how growth and body size are
80 regulated. Initial studies of *C. elegans* development described whole-organism growth as a sigmoidal curve
81 characterized by continuous larval growth in length that reaches saturation in adulthood (Byerly et al., 1976).
82 These early studies hypothesized that molt events had little effect on continuous growth as the *C. elegans*
83 cuticle allowed for stretch during larval stages. Later work determined that larval progression was not
84 continuous but rather piecewise in nature (Knight et al., 2002). This study showed that *C. elegans* volumetric
85 growth rate increased from stage to stage such that L1 animals had the slowest rate of growth and L4 animals

86 had the fastest. This finding suggests that *C. elegans* have a mechanism for regulating growth rate, potentially
 87 at each molt. Next, researchers using single-animal imaging strategies observed that animals did not advance
 88 to the next developmental stage until a critical volume was reached (Uppaluri and Brangwynne, 2015). This
 89 finding suggests that *C. elegans* growth follows a ‘Sizer’ model with each molt decision controlled by a volume
 90 threshold and further implies that individual cells are able to communicate information about body size to
 91 precisely regulate growth. Most recently, live imaging and characterization of body volume heterogeneity
 92 revealed that with respect to the start of a larval stage, *C. elegans* volume fold change within a stage is nearly
 93 invariant thereby preventing rapid divergence in volume between fast and slow growing animals (Towbin and
 94 Grosshans, 2021).

95 Extensive characterization of *C. elegans* body size mutants has revealed several processes that influence
 96 growth rate and body size (Tuck, 2014). A number of genes act through signaling pathways to influence growth
 97 and body size (McKeown et al., 1998; Patterson and Padgett, 2000). Some of these pathways contribute to
 98 body size control by regulating cuticle collagen genes (Madaan et al., 2018). Alternatively, mutations in some
 99 cuticle collagen genes directly disrupt the physical structure of the cuticle (Page and Johnstone, 2007b). These
 100 structural changes act as physical constraints on growth as opposed to regulatory mechanisms of growth
 101 control. Environmental factors also play a significant role in *C. elegans* growth control. Food restriction is
 102 known to decrease growth rate or, when extreme, induce complete developmental arrest (Baugh, 2013; Hu,
 103 2018; Uppaluri and Brangwynne, 2015). In *C. elegans*, mutations that disrupt the ability to properly consume
 104 food also cause individuals to be small and thin, indicating that food intake can act as a physical constraint on
 105 growth and body shape (Mörck and Pilon, 2006).

106 To understand *C. elegans* growth control at the whole-organism level, precise measurements of body size and
 107 shape for large numbers of individuals are required. Using a combination of quantitative growth measurements
 108 and mathematical modeling, we performed a high-resolution longitudinal study of *C. elegans* larval progression
 109 and captured high-precision details about animal length, width, volume, and feeding dynamics. By investigating

110 *C. elegans* feeding and growth in tandem for thousands of individual animals, we found decreases in feeding
 111 behavior associated with each larval transition that were also correlated in time with changes in growth. We
 112 used our large-scale measurements of body size to further analyze the periods of time surrounding each larval
 113 transition. At each molt, we observed simultaneous increases in length, decreases in width, and maintenance
 114 of volume, suggesting that body shape in addition to size plays a role in the control of *C. elegans* growth.
 115 Given these data, we propose a “Stretcher” mechanism for growth control whereby *C. elegans* senses body
 116 size through physical constraints on cuticle stretch and undergoes larval-stage transitions when the cuticle
 117 reaches its maximum capacity for stretch. Additionally, we propose that *C. elegans* are able to physically
 118 constrain growth rate by modulating food intake. We used quantitative models of eating and growth to evaluate
 119 our data and predicted that the rate of volumetric growth is controlled by animal feeding rate and metabolic
 120 regulation. Food allocated toward growth reached maxima and minima at larval transitions, indicating
 121 increased metabolic control at these points in development.

122 **Results**

123 **Quantitative measurements of *C. elegans* growth**

124 We have optimized a quantitative growth assay that reliably measures small changes in *C. elegans* body size
 125 throughout development (Fig 1). Our method provides both high-throughput and high-precision assessment of
 126 developmental growth. In brief, populations of 100,000 animals were cultured in flasks. We cultured six
 127 replicate populations of *C. elegans* for a total of 600,000 synchronized and growing animals. Every hour after
 128 feeding, a sample of the population from each flask (~300 animals/flask) was collected to measure animal
 129 length, width, and feeding rate. Feeding rate, examined using fluorescent microspheres, and body size were
 130 measured using the COPAS BIOSORT (Union Biometrica). Then, the ImageXpress system (Molecular
 131 Devices) was used to collect images of sampled animals. This platform allowed for the further analysis of life
 132 stage and body size, contributing added precision to our measurements.

Fig 1. An overview of the quantitative growth assay.

Schematic of the experimental workflow was created with BioRender.com. Synchronized animals were cultured in flasks where six flasks contained replicate populations of nematodes, one flask had a population of unfed animals, and one flask only contained bacterial food. At each hour of the experiment, all eight flasks were sampled. In step 1, animals were transferred from each flask to a single well of a 96-well microtiter plate. In step 2, fluorescent beads were added to each well. Following a 10-minute incubation period, animals from each well of the deep-well plate were transferred to several wells of a 96-well microtiter plate for step 3. In step 4, animals in each well of the microtiter plate were imaged. In step 5, the same animals were measured using the COPAS BIOSORT. This process was repeated every hour after feeding for 72 consecutive hours (see Methods).

The raw data from the quantitative growth assay provides measurements of body size and feeding behavior, which are traits related to animal growth. Two measurements of body size were collected from raw data taken from the COPAS BIOSORT: time of flight (TOF) and optical extinction (EXT) (S1 Fig). Time of flight is a measurement of body length, and optical extinction corresponds to optical density, a measurement influenced by body length, thickness, and composition (Andersen et al., 2015; Pulak, 2006). We investigated whether optical extinction could be correlated to a different measure of body size using the collection of manual size measurements from images (see Methods). We calculated the median length, width, area, and volume of animals in a subset of imaged wells from each hour of the experiment. We then compared these values to well median statistics from the processed COPAS BIOSORT data. We found a strong correlation between manual measurements of animal length from the image analysis and TOF measurements from the COPAS BIOSORT

153 (S2 Fig). We also observed an equally strong correlation between manual measurements of animal area and
 154 EXT as well as animal width and EXT normalized by body length (norm.EXT). We then approximated animal
 155 volume using measurements from the COPAS BIOSORT by using a cylindrical approximation for *C. elegans*
 156 shape (see Methods). This result expanded the number of body size parameters that we were able to assess
 157 using the COPAS BIOSORT data, allowing us to investigate growth dynamics in length, width, and volume (Fig
 158 2A-C). To disentangle nematode objects from non-animal objects (bacteria clumps, detritus, shed cuticles), we
 159 employed model-based clustering to remove unwanted objects and better examine growth of animals (S3 Fig).
 160 Lastly, we converted COPAS BIOSORT measurements into microns (see Methods).

161 **Fig 2. Quantitative measurements of animal size.**

162 COPAS BIOSORT data of animal length (A), width (B), and volume (C) after the removal of non-animal objects
 163 using model-based clustering methods (see Methods).

We report body length, width, and volume of animals at each hour of development from L1 to adult (S1 Fig and Fig 2). Historically, growth of *C. elegans* has been shown as a sigmoidal curve where exponential growth during larval stages reaches a maximum rate in adulthood (Byerly et al., 1976). More recently, researchers have identified that growth curves are discontinuous during development punctuated by larval transitions (Knight et al., 2002; Uppaluri and Brangwynne, 2015). Using our quantitative growth assay, we captured these small-scale discontinuities in larval growth as well as an apparent growth maximum during early adulthood. We noticed that all size variables (length, width, and volume) displayed these dynamics. Objects identified as animals appear to grow in size. However, in particular time windows during development, growth dynamics visibly shift, producing discontinuities in animal growth rate. With these data, we were able to further investigate *C. elegans* growth and size control.

Fluorescence provides a quantitative measurement of animal feeding behavior and developmental progression

In addition to body size and shape, the raw data from the quantitative growth assay described above measured fluorescence of each animal object. To readily assess the thousands of measurements acquired at each hour, we generated summary statistics of median well measurements (S1 Table). With these summarized data, we investigated the relationship between feeding behavior and developmental stage. It is well established that temporary suspensions of *C. elegans* feeding occur during each molt (Byerly et al., 1976; Cassada and Russell, 1975). As such, active feeding is frequently used to distinguish growing animals from individuals in a molt. We quantified feeding behavior by exposing animals to fluorescent beads the approximate size of bacteria and measuring fluorescence of animals (Nika et al., 2016). Because larger animals are able to consume more food and therefore contain more ingested food, we normalized fluorescence by animal area to account for increases in body size (S4 Fig). The resulting fluorescence data showed a dynamic pattern (Fig 3A). At approximately 15 hours, fluorescence steadily increased to a peak before decreasing back to initial levels at approximately hour 27. This pattern, repeated three additional times, established clear time windows of local minimal fluorescence. These local minima represent periods of time where a large proportion of the

189 population had reduced or ceased feeding and therefore suggests time windows where a majority of animals
190 were likely not feeding because they were in a molt. We used a local kernel regression method to estimate a
191 smooth curve and calculate the derivative to identify the time associated with each local minimum (see
192 Methods). We then assessed images collected from the growth assay and demonstrated that periods of
193 decreased feeding are concurrent with the presence of shed cuticles, supporting that animals are undergoing a
194 molt during these periods of time (S5 Fig). When we overlaid the timing of each local minimum on the
195 population size data, we were able to outline the start and end of each larval stage (Fig 3B-D). Notably, local
196 minima occurred approximately every ten hours, consistent with well established observations of molt timing
197 (Byerly et al., 1976). Furthermore, we observed a clear relationship between changes in feeding behavior and
198 growth dynamics where decreases in feeding occurred simultaneously with discontinuous growth in length,
199 width, and volume.

200 **Fig 3. Fluorescence dynamics outline larval stages.**

201 (A) Median normalized red fluorescence (y-axis) over time (x-axis) is shown. The blue line represents the
 202 kernel regression fit to the data. The red vertical lines correspond to the local minima of the regression and
 203 represent the transition between larval stages. Median length (B), median width (C), and median log volume
 204 (D) are shown with larval-stage transitions as well. Upper and lower bounds of the box plots correspond to the
 205 first and third quartiles. The upper and lower whiskers extend to 1.5 times the value of the interquartile range.

206 **Changes in *C. elegans* body shape occur at larval-stage transitions**

207 Adult body size is ultimately determined by the coordination of developmental progression and rate of growth.
 208 To understand how *C. elegans* achieve final size, we must first examine how *C. elegans* grow. Quantitative
 209 studies of *C. elegans* growth frequently assess changes in length or volume over time; however, to fully
 210 characterize changes associated with growth, it is also important to consider the dynamics of width. Two
 211 general models were proposed for *C. elegans* growth in volume: linear and exponential (Byerly et al., 1976;
 212 Knight et al., 2002; Uppaluri and Brangwynne, 2015). Notably, these volume growth models require different
 213 dynamics in length and width. To achieve linear volume growth, length and width must increase at precise
 214 sublinear rates that together result in a linear increase in volume. If animal length and width increased at a
 215 constant linear rate, then volume would increase at a cubic rate. Alternatively, if both length and width grew
 216 exponentially, then volume would fit an exponential model. We sought to identify which model best described
 217 *C. elegans* growth behavior but were unable to consistently distinguish between linear, exponential, and cubic
 218 models using statistical information criterion because of the similarity in the shapes of the growth curves (S6
 219 Fig and S2 Table). This result is not surprising because computational simulations have shown that increases
 220 in experimental noise, above 2% added noise, limit the correct identification of growth models (Vuaridel-Thurre
 221 et al., 2020).

222 Growth has important implications for how animals regulate size. Size homeostasis requires that growth rate
 223 and developmental rate are coordinated. *C. elegans* reach a similar volume at each larval transition despite
 224 significant variation in individual growth rates (Uppaluri and Brangwynne, 2015). Because individuals in a
 225 population maintain similar sizes despite differences in growth rate, a control mechanism to regulate
 226 developmental progression must exist. Early work proposed a size-based growth control model in *C. elegans*

227 (*Uppaluri and Brangwynne, 2015*), while recent work suggests that size homeostasis is achieved through a
 228 folder mechanism where growth rate and development are coupled (Towbin and Grosshans, 2021). To assess
 229 changes in body size and shape during a larval transition, we examined the dynamics of animal length, width,
 230 and volume in the hours before, during, and after each molt. We find that for each shape variable, larger
 231 animals enter molt first (Fig 4). We also observe differences in the distributions of lengths during a larval
 232 transition compared to widths and volumes. Measurements of animal width and volume remain unimodal
 233 throughout a molt, but length does not. As larger animals begin to exit the molt, an increase in body length
 234 occurs that leads to the appearance of bimodality of lengths across the population. This length increase occurs
 235 simultaneously with a decrease in widths across the population. Importantly, volume remains constant while
 236 length increases and width decreases, indicating a change in body geometry not size (Fig 3 and Fig 4). These
 237 changes in the physical dimensions at each larval transition suggests that body shape, in addition to size, is
 238 involved in the control of *C. elegans* growth.

Fig 4. Density plots of population size dynamics during a single larval transition.

Population density curves of length (A), width (B) and volume (C) for the hours surrounding the L3 - L4 larval transition (red horizontal line at 36 hours corresponds to the molt). Each distribution was divided into five quantiles. The percentage of quiescent animals present within each quantile was calculated (see Methods), and each quantile was colored to reflect this percentage. In all shape variables, quantiles that contain the largest animals displayed an increase in quiescence earlier than quantiles that contain the smallest animals. These dynamics were consistent across all larval-stage transitions (S7 Fig).

Measurements of body shape suggest that cuticle stretch determines the timing of larval-stage transitions

Previous studies theorized that the internal mechanism for sensing body size and triggering molts in *C. elegans* is driven, in part, by the properties of the collagen-rich cuticle (Towbin and Grosshans, 2021; Uppaluri

250 and Brangwynne, 2015). Many cuticle collagen mutations cause morphological defects in nematode shape
 251 some of which cause animals to be shorter but do not impact animal width, implying that the cuticle affects
 252 length and width independently (Brenner, 1974). The *C. elegans* cuticle does not grow through the addition of
 253 new material, but rather stretches to accommodate increases in animal body size. Cuticle stretch is likely
 254 limited by the material properties of the cuticle. The *C. elegans* cuticle is primarily made of cross-linked
 255 collagens organized into lateral ridges and circumferential bands (Page and Johnstone, 2007b). Commonly
 256 found in many biological systems, collagen-based materials are fairly flexible under low stress conditions.
 257 However, as stress increases, collagen fibrils may become elongated and orient in the load bearing direction
 258 leading to a decrease in elasticity (Holzapfel, 2017). Previous work using atomic force microscopy revealed a
 259 high level of biomechanical stiffness at the circumferential bands (Essmann et al., 2017), leading others to
 260 speculate that mechanical strain on these structures is likely adjusted as internal body pressure changes
 261 (Dodd et al., 2018). Additionally, in *nekl-3(sv3)* molting mutants, the cuticle is not properly removed from the
 262 middle part of their body, leaving the free head and tail to grow normally while the encased middle is
 263 constricted by the old cuticle to pre-molt dimensions (Yochem et al., 2015). Given this body restriction, we
 264 speculate that the old cuticle stretches beyond its tolerance, becomes stiff, and constricts the center of the
 265 nematode relative to the growing head and tail size. We hypothesize that *C. elegans* sense when the cuticle
 266 becomes restrictive and use a threshold in the reduction of elasticity or “stretchiness” of the cuticle to
 267 determine when to initiate a molt.

268 To explain the initialization of molt behavior, we developed a “Stretcher” model for a cuticle-stretch-based
 269 threshold that triggers *C. elegans* larval-stage transitions. We propose that the nematode passes through three
 270 distinct regimes related to cuticle stretch: linear stretch dynamics, non-linear stretch dynamics, and larval stage
 271 transition (Fig 5). The cuticle structure is anisotropic, possibly leading to distinct properties in the length and
 272 width directions (Cox et al., 1981; Petzold et al., 2011). We approximated the cuticle as a hollow cylinder of
 273 negligible thickness filled by the body of the nematode. Growth was modelled as internal pressure evenly

274 applied to the cuticle in all directions. We hypothesized that the cuticle responds differently during linear
275 stretch, nonlinear stretch, and post-molt relaxation.

276 **Fig 5. Cuticle stretch determines larval-stage transitions**

277 The "Stretcher" model describes each larval stage as a cycle. Nematodes are modeled as a cylindrical object
278 with a thin cuticle epidermis. (Box 1) Linear Stretch Dynamics: uniform growth pressure stretches the cuticle
279 linearly in both length and width. (Box 2) Nonlinear Stretch Dynamics: the cuticle has reached a stretch
280 threshold in length, and under uniform growth pressure the length stretches less (sub-linear) and width
281 stretches linearly. (Box 3) Larval Stage Transition: a new cuticle is formed and the old cuticle is shed (ecdysis),
282 removing constraints in length. The nematode body "relaxes" in length, causing an increase in length, a
283 decrease in width, and constant volume.

284 In the linear stretch regime (Fig 5), the cuticle would be linearly elastic in both the length and width directions,
285 stretching proportionally to the pressure exerted on the cuticle. Previous work found evidence for a linearly

286 elastic cuticle (Gilpin et al., 2015; Park et al., 2007) in animals expanded in a negative external pressure
 287 environment or after positive force was applied to the cuticle. Gilpin *et al.* have found evidence of linear
 288 elasticity in the nematode body. We conjecture that this linear elasticity is caused by the constraints applied by
 289 the cuticle ((Gilpin et al., 2015; Park et al., 2007). A linearly elastic cuticle will have ΔL stretch in the length
 290 direction and ΔW stretch in the width direction, each related to growth-applied pressure Δp by

$$291 \qquad \qquad \qquad \Delta L = a_L \Delta p \qquad \qquad \qquad (1)$$

$$292 \qquad \qquad \qquad \Delta W = a_W \Delta p. \qquad \qquad \qquad (2)$$

293 The “stretch coefficients” in length, a_L , and width, a_W , measure the stiffness of the cuticle (S5 File, Eq.
 294 S14-S23). Smaller values correspond to a stiffer material, which is less able to stretch in response to pressure.
 295 The stretch coefficients are constant in the linearly elastic regime and are determined by geometric constants
 296 and material properties. The ratio of the change in length (Eq. 1) and width (Eq. 2) produces a
 297 pressure-independent relationship that depends only on the ratio of the geometric and material properties,
 298 which can be verified using measurements of length and width (Fig. 3). During the linearly elastic regime, the
 299 ratio of growth in width to growth in length is constant throughout a larval stage where the cuticle properties are
 300 fixed as in

$$301 \qquad \qquad \qquad \frac{\Delta W}{\Delta L} = \frac{a_W}{a_L} = \text{constant}. \qquad \qquad \qquad (3)$$

302 In the non-linear stretch regime (Fig 5), growth continues to apply pressure to the cuticle uniformly in all
 303 directions. As observed in *nekl-3(sv3)* mutants, the cuticle can restrict body growth (Yochem et al., 2015).
 304 Once outside of the linearly elastic regime, the cuticle would hardly stretch, even under large forces. We
 305 hypothesized that this shift from linear to nonlinear regimes provides a mechanism for size-sensing and cues
 306 the larval-stage transition (Fig 5). In principle, this transition could occur in either the width or length directions.
 307 For ease of presentation, we assume a transition from linear to non-linear stretch in the length direction and

308 maintains linear stretch in the width direction. In the nonlinear regime, the stretch in the length direction in
309 response to pressure becomes

$$310 \quad \Delta L \approx \tilde{a}_L(p) \Delta p. \quad (4)$$

311 The nonlinear “stretch coefficient,” $\tilde{a}_L(p)$, is no longer constant and decreases with increasing pressure. It is
312 smaller than a_L because the cuticle has become less elastic than in the linear regime. If the length-direction
313 enters the nonlinear regime and has reduced stretch response, while width has the same constant stretch
314 response then, we expect the $\frac{\Delta W}{\Delta L}$ ratio to increase

$$315 \quad \frac{\Delta W}{\Delta L} \big|_{non-linear} = \frac{a_w}{\tilde{a}_L(p)} > \frac{a_w}{a_L} = \frac{\Delta W}{\Delta L} \big|_{linear}. \quad (5)$$

316 During the larval-stage transition (Fig 5), a new, larger cuticle is formed beneath the old cuticle that is shed
317 during ecdysis. Because the old cuticle constrained growth in length, we predict a rapid increase in the length
318 direction when the constraint is removed. Nematode volume is conserved as growth does not occur during this
319 process. Therefore, the relaxation in length is accompanied by a corresponding decrease in width.

Fig 6. Stretcher model analysis of replicate 2 COPAS BIOSORT data consistent with a length trigger for molting

(A) A grayscale histogram of the width (y-axis) vs length (x-axis) of all sampled animals in replicate 2. The range of all bootstrap regressions is in gold. (B) Demonstration of calculating the ratio of width-to-length stretch as the local slope using L3. Left panel is a repetition of L3 data from Fig 6A. Right panel is a repetition of results from Fig 6C. (C) Within a larval stage, the ratio of width to length stretch varies over time. The standard deviation captures population variation (grey) (S5 File, Eq. S26, S28).

To verify the shape dynamics predicted by the Stretcher model, we analyzed the relationship between nematode length and width over developmental time. All three regimes, linear stretch, non-linear stretch, and relaxation, predicted by the Stretcher model are detectable in the COPAS BIOSORT data (Fig 6). In all larval stages, the instantaneous ratio $\frac{\Delta W}{\Delta L}$ was approximately constant for the majority of the time, consistent with a linear stretch regime (Fig 6C). We observed a large slope decrease during the L1 stage, which could

correspond in time to the metabolic decision for entry into the dauer stage (Golden and Riddle, 1984) or divisions of the seam cells (Sulston and Horvitz, 1977). Near the end of L2 and L3 stages, we observed a sharp slope increase, supporting our predictions of a non-linear stretch regime in length prior to lethargus. Slope transitions are difficult to detect at all larval stages due to noise amplification present in slope calculations and population effects, making the larval stage boundaries difficult to define in a consistent manner. We note that the transitions between larval stages contain the expected increase in length and a decrease in width (Fig 6A and S8 Fig) consistent with a length threshold in the Stretcher model. Though the shape relaxation for an individual animal is expected to happen at a much shorter time scale than data collection (seconds to minutes), the measured shape change within the population occurs on a larger time scale of several hours. As different individuals reach the transition points at different times, the shape change is smoothed out and difficult to observe in the time-course data (Fig 3). However, we were able to more readily observe the sudden shape change at transitions by looking at the width and length because animals of similar shape are grouped together, regardless of the time they were observed (Fig 6A). These results suggest that the material properties of the cuticle could generate a mechanical signal for the start of larval transition. Additionally, sensing when the cuticle reaches a critical stiffness would allow the animal to detect when a certain fold change occurs.

Mechanical control of feeding and allocation of food energy likely constrain growth dynamics

We have shown that changes in physical properties of the *C. elegans* cuticle precede the decision to initiate molt and might serve as a cue for developmental timing. *C. elegans* must have mechanisms to control growth throughout development, particularly in response to these cues. Like most species, *C. elegans* do not increase their growth rate indefinitely in response to increased food availability (Uppaluri and Brangwynne, 2015). The animals could control growth entirely using feeding rate, as they actively control the feeding rate (Fang-Yen et al., 2009) and stop feeding at the initiation of a molt (Singh and Sulston, 1978). In addition to this mechanical control, they could use metabolic control to preemptively divert ingested resources toward or away from growth. Metabolic processing of stored resources could be especially useful if animals complete their molt and

enter a food-limited environment. For these reasons, we investigated the possible mechanical control of feeding (Fig 7) and the metabolic control of the allocation of ingested food toward organismal growth and development (Fig 8). Using a quantitative feeding model, we calculated the rate of mechanical feeding behavior from animal volume and food intake data. Additionally, we calculated an estimate for allocation of ingested food toward volumetric growth.

Fig 7. Visualization and analysis of Feeding Model

Schematics for food intake and utilization models are shown. (A) The buccal cavity is the opening through which food enters. The pharyngeal lumen is the cavity opened and closed by pharyngeal muscles that drives food intake. (B) Product of pumping frequency and pharyngeal lumen fraction, $f(t)g(t)$.

Fig 8. Visualization and analysis of Food Utilization model.

(A) Dynamics of volume growth rate. (B) Dynamics of the estimated food utilization towards growth ($\alpha(t)$). (C) Dynamics of red fluorescence. (D) Dynamics of food allocation breakdown. Food allocated toward maintenance is proportional to animal size (pink). Food allocated toward growth is calculated from food intake (B) and utilization (C) to produce low (dark green) and high (combined green) estimates (S5 File). Food allocated to other metabolic processes consists of remaining food resources (grey). In panels A-C, the solid blue line represents the mean bootstrap regression. Standard deviation on the regression is marked by the shaded blue region. In panels A-D, Vertical red lines mark molt times. Green regions correspond to times during which volumetric growth rate and red fluorescence are both increasing, red regions correspond to times during which volumetric growth rate and red fluorescence are both decreasing, and white regions correspond to times during which volumetric growth rate and red fluorescence do not vary together. Errors on shaded regions are ± 0.7 hours. These data are from replicate 2 and are representative of all replicates (S11 Fig).

378 Variation in pumping rate controls food uptake

379 *C. elegans* is a filter feeder that pumps its food through a cycle of pharyngeal muscle contractions and
380 relaxations that alternatively open and close the pharyngeal cavity. *C. elegans* are capable of actively
381 modulating the length of time used to contract or open a subset of the pharyngeal muscles (Fang-Yen et al.,
382 2009). Our feeding model describes how control of this time length and thus the control of the overall pumping
383 period, defined as the length of time of one full pumping cycle, translates to changes in the rate of food uptake.

384 A single cycle in which animals take up and transport food to the gut consists of four general steps (Fig 7A).
385 The cycle begins with relaxed pharyngeal muscles and a closed pharyngeal lumen (step 1). The animal opens
386 the pharyngeal lumen so that fluid and food flow through the buccal cavity and into the pharyngeal lumen (step
387 2). The animal cannot create a vacuum, so the volume of the cavity produced must be filled entirely by media
388 and bacteria at the same concentration as the external environment. The animal relaxes the muscles that
389 control the opening, stopping the flow of fluid through the buccal cavity and trapping a volume of media
390 approximately equal to the maximum volume of the pharyngeal lumen (step 3). Finally, the pharynx closes,
391 extruding excess media and trapping bacteria and beads that are then 'swallowed' (step 4). The period of a
392 single cycle varies throughout the life cycle of *C. elegans* (Fang-Yen et al., 2009).

393 We find a relationship between eating rate and animal volume. It has previously been suggested that the
394 cross-sectional area of the buccal cavity is a limiting factor in the rate of food intake (Knight et al., 2002).
395 However, the volume of the pharyngeal lumen is filled with media each cycle, so the volume of the pharyngeal
396 lumen, not the cross-sectional area, sets food uptake rate. We express the volume of the pharyngeal lumen as
397 a fraction, $g(t)$, of nematode volume, $V_{lumen:max}(t) = g(t) \cdot V_{worm}(t)$. As the pumping period is much faster
398 (roughly 200 ms in adults) (Fang-Yen et al., 2009) than the rate of measured growth (hours), we averaged the
399 food intake rate, $\frac{dV_{food}}{dt}$, over a single pumping period (S5 File, Eq. S1-S6) to obtain

$$400 \quad \frac{dV_{food}}{dt} = Cf(t)g(t)V_{worm} \cdot \quad (6)$$

Here, C is the concentration of bacteria in the culture where animals are grown and $f(t)$ is the pumping frequency and the inverse of the period of a single pump. Both pumping frequency, $f(t)$, and the fractional pharyngeal lumen size, $g(t)$, vary over the animal's life cycle. Though any individual bacterium may take multiple pumps to travel down to the gut, we assume that, once food has entered the pharyngeal lumen, it will eventually be metabolized. With this assumption, we are only interested in the rate at which food enters so we do not model the dynamics of food traveling through the gut.

We verify that red fluorescence (denoted as “*Red*”) can be treated as a proxy measurement for food intake rate given defecation rates (S9 Fig, S5 File). We use red fluorescence and calculated volume as the product of pumping rate and pharyngeal lumen fraction, $f(t)g(t) \propto \frac{Red}{V_{worm}}$, over time. The product oscillated within a larval stage and decreased across larval stages (Fig 7B). The minima of the product of pumping frequency and pharyngeal lumen fraction occurred during molt times, consistent with prior knowledge (Byerly et al., 1976; Singh and Sulston, 1978). The relative length of the pharynx to animal length has been shown to decrease over development (Avery, 2003) and a similar trend in the volume of the pharyngeal lumen could explain the slow decrease in the product of pumping frequency and pharynx fraction.

Changes in food utilization coincide with molts

To understand whether animals control growth rate primarily using the mechanical feeding process or metabolic regulation, we describe how food is utilized once it is ingested by *C. elegans*. We assumed three general categories of food utilization: maintenance, observed volumetric growth, and all other processes. We assume that resources required for maintenance are proportional to the volume of the animal. Other processes may include the development of tissues and structures, such as reproductive components, within the worm which are resource intensive, but are not detected during the measurements of the width, length, or volume. The rate of food conversion to growth can be described by:

423

$$\frac{dV_{worm}}{dt}(t) = \eta(t)\alpha(t)\frac{dV_{food}}{dt}(t). \quad (7)$$

424 Here, $\frac{dV_{food}}{dt}$ is the instantaneous rate of food intake (averaged over a single pump), $\eta(t)$ is the metabolic
 425 efficiency of converting food to growth, and $\alpha(t)$ is food utilization, meaning the fraction of food used for
 426 volumetric growth as opposed to maintenance or other metabolic processes. If both $\eta(t)$ and $\alpha(t)$ are constant,
 427 then Eq. (4) predicts the rate of volumetric growth is directly proportional to the rate of food consumption, which
 428 would be equivalent to controlling growth through feeding with no changes in metabolic regulation (through
 429 enzyme expression or other direction of flux between pathways). Efficiency captures the maximum efficiency of
 430 metabolism, and we assume it does not vary significantly when the food source is constant, $\eta(t) = \eta$.
 431 Therefore, utilization captures the dynamics of metabolic regulation. If the fraction of food utilized for growth is
 432 not constant, then volumetric growth rate is no longer proportional to food consumption rate and metabolic
 433 control must play a role in driving the growth rate.

434 We calculate the value of the product of metabolic efficiency and food utilization, $\alpha(t)\eta$, from the data by
 435 manipulating Eq. (7):

$$\alpha(t)\eta = \left(\frac{dV_{worm}}{dt}(t)\right) / \left(\frac{dV_{food}}{dt}(t)\right). \quad (8)$$

437 By using the red fluorescence as a proxy for food intake rate in Eq. (8), we can estimate the dynamical
 438 behavior up to scaling factors for the metabolic efficiency times food utilization, $\alpha(t)\eta \propto \left(\frac{dV_{worm}}{dt}(t)\right) / Red$ (Fig
 439 8B). Because only utilization varies in time, it captures the dynamics of metabolic regulation:

$$\alpha(t) \propto \left(\frac{dV_{worm}}{dt}(t)\right) / Red. \quad (9)$$

441 Feeding rate (using red fluorescence as a proxy) and volume growth rate (numerically differentiated from the
 442 volume regression) follow similar dynamics throughout much of *C. elegans* development (Fig 8A, Fig 8C). The
 443 regressions for volume growth rate and food intake rate (as measured through red fluorescence) demonstrate
 444 a greater than 90% correlation when using synchronized populations (through the end of L4). Each larval stage

consists of three types of dynamics: steady growth during which food intake and growth rate are both increasing (green), preparation for molt during which food intake and growth rate are both decreasing (red), and transition regions where food intake and growth rate do not vary together (white). To illustrate how the dynamics of food intake rate and growth rate (Fig. 8A, 8C) correspond to the progression within a larval stage, consider the L3 larvae in replicate 2. At hour 24.5, both growth rate and food intake rate increased corresponding to the start of the third larval stage for the population average. Until hour 29.8, the population grew steadily, and food intake and growth rate both increased (green). Between hour 29.8 and 30.8 (white), food intake decreased and growth rate increased, marking a transition from the steady growth (green) to the molt preparation regime (red). Between hours 30.8 and 32.1, the animals prepared to initiate molts, and both the growth rate and food intake rate decreased (red). Between hours 32.1 and 34.4 (white), the animals' growth rate increased once again while the food intake rate continued to decrease corresponding to the end of the molt and start of the L4 larval stage. Similar dynamics occurred in the L2 and L3 larval stages. The L1 larval stage followed different dynamics, likely due to the dauer decision or divisions of the seam cells.

During steady growth (green) and molt initiation (red), mechanical food intake rate and allocation of food resources towards observable growth have similar dynamics. At transition points (white) the allocation of food resources towards growth, $\alpha(t)$, reaches a local minimum or maximum (Fig 8B). These local extrema in $\alpha(t)$ at transition points likely indicate large changes in metabolic regulation. One might expect growth rate to lag food intake, but time-lag analysis showed no consistent lag across L1 to L4. During the L1 and L2 stages, volume growth rate lagged behind food intake rate (with correlation ~86%); during the L3 and L4 stages, food intake rate lagged behind growth rate (with correlation ~94%) (S14 Fig). The switch to food intake lagging growth rate at later larval stages might be indicative of increased regulation of resource allocation.

One might assume that the high correlation (S15 Fig) between dynamics of growth (Fig. 8A) and food intake (Fig. 8C) imply that animals control their growth rate entirely through the control of mechanical food intake rate with no variation in how food resources are allocated. Instead we saw variation in food allocated toward

469 growth, $\alpha(t)$, both between larval stages and within individual larval stages. We examined the dynamic range
 470 of total food intake (Fig. 8C) and the dynamic range of food allocated toward growth (combined green Fig. 8D)
 471 to quantify whether control through food intake or control through metabolic regulation play a larger role in
 472 growth regulation. Across a larval stage, both methods of regulation had dynamic ranges of the same order of
 473 magnitude. We also calculated the dynamic range within each period of steady growth (green), molt initiation
 474 (red), and transition (white) (Fig. 8). Within each region, the dynamic range of food intake and food allocated
 475 toward growth differed by a factor of 0.5 to 5, but we found no noticeable trends by region (S3 Table). It is
 476 possible that the interpolation and smoothing required to calculate derivatives necessary to this analysis are
 477 masking some sharper transitions, which could be resolved with higher resolution temporal experiments.
 478 These results suggested that both the total intake rate (governed by mechanical feeding behavior) and
 479 metabolic regulation of food resources are crucial for growth control in all regions of development. Additionally,
 480 we compared the food allocated toward other metabolic processes with food allocated toward growth over the
 481 four larval stages. Using the low growth utilization estimate, food allocated toward growth increases with an
 482 approximately 86-fold increase while the other resource allocation increases with an approximately six-fold
 483 increase. Resource requirements for other metabolic processes such as development of new tissues and
 484 animal mobility might vary much less during development than the resource requirements for volumetric
 485 growth.

486 Feeding rate and volumetric growth rate share a complex relationship with *C. elegans* development; food
 487 intake and growth rate vary together, except at larval stage transitions and possible key developmental
 488 transitions. Notably, the changes in metabolic resource allocation at the transition from increasing to
 489 decreasing growth and food intake rates (Fig 8A, 8C) occurred at approximately the same times as the
 490 increase in slope predicted as a cue for molt initiation by the Stretcher model (Fig 6). This correlation suggests
 491 that the cuticle reaches its maximum stretch in length and a metabolic decision to reallocate food resources
 492 growth occurs at the same time, supporting the hypothesis that a physical threshold in stretch triggers
 493 metabolic decisions to enter a molt (S10 Fig).

494 Discussion

495 Using an integrated image-based and flow-based phenotyping strategy to precisely evaluate feeding, growth,
 496 and molt dynamics at high replication, we detected oscillations in feeding behavior consistent with larval
 497 progressions and used these dynamics to define larval stages. We observed changes in body shape at each
 498 larval-stage transition that are consistent with differences in physical cuticle properties along length or width
 499 (anisotropy). These results suggest that animals sense their size and control molt timing by detecting the
 500 physical stretch of the cuticle. To understand whether *C. elegans* control growth using the moderation of the
 501 physical uptake of nutrients or through metabolic regulation of the allocation of consumed resources, we
 502 applied mathematical models of feeding-limited growth to our data. We predicted that the volumetric growth
 503 rate was controlled by both *C. elegans* feeding rate and other metabolic regulation and provided a modeling
 504 framework to decouple the relative effects. These results demonstrate two mechanisms by which physical
 505 constraints can influence developmental timing and growth rate.

506 Cuticle stretch controls the timing of larval-stage transitions

507 Measurement of both animal length and width allowed us to observe changes in body shape as well as body
 508 size. We propose that a stretch threshold along the body length axis acts as a trigger to larval-stage
 509 transitions. Importantly, mechanical stretch sensing could also provide organisms a way to couple the rate of
 510 growth and development to maintain a constant volume fold change within a larval stage and achieve size
 511 homeostasis within a population. In this way, smaller animals would reach a stretch limit at a smaller size as
 512 the cuticle would only stretch a percentage of its original size before reaching a threshold. A folder mechanism
 513 for *C. elegans* growth has been previously suggested (Towbin and Grosshans, 2021). For cuticle stretch to
 514 trigger larval-stage transitions, animals must either have the ability to measure the amount the cuticle has
 515 stretched or the stiffness of the cuticle. Across biological systems, cells can respond to the stiffness of their
 516 environment using mechanosensitive components (Schiller and Fässler, 2013; Wolfenson et al., 2011), but few
 517 examples in tissues or whole-organisms are known. In *C. elegans*, it has been demonstrated that

hemidesmosomes, which connect the cuticle and the epidermis, are mechanosensitive during embryogenesis (Suman et al., 2019; Zhang et al., 2011). Additionally, dense bodies, which connect the epidermis and muscles, are hypothesized to be mechanosensitive as well (Broday et al., 2007; Costa et al., 1997; Moerman and Williams, 2006; Zaidel-Bar et al., 2010). Changes in cuticle composition, and presumably stiffness, have been shown to also affect well known growth controlling pathways such as the BMP signaling pathway (Madaan et al., 2020). These possible mechanosensitive components could monitor the stiffness of the cuticle and be part of the signaling pathways that regulate larval-stage transitions. Further experiments are required to explicitly test whether these components control larval-stage transitions.

Our analysis of width-to-length ratio variation over larval stages provides a first approximation of the timing of larval-stage transition cues and cuticle stretch properties (Fig 8). The sudden increase we observed in the width-to-length ratio suggests a length stretch threshold. Interestingly, when observing the L4 to adult transition, others have detected anisotropic constriction on the transverse (width) axis followed by gradual relaxation driven by rearrangements in cortical actin networks (Katz et al., 2018). Single-worm, high frequency measurements targeting hours surrounding the sudden width-to-length ratio increase, are needed to better resolve cuticle shape dynamics. Higher time resolution would also minimize edge effects (S12 Fig), which likely caused the unpredicted width-to-length ratio increase observed at the start of larval stage L2 (Fig 8C). Measurements of animal length and width provide a total stiffness estimate but do not allow us to distinguish the contributions of cuticle stiffness from other tissues. To investigate cuticle properties, independent of other nematode tissues and organs, experiments must probe the stiffness of free cuticles.

Physical constraints on feeding influence growth dynamics

Our mechanical feeding model defines a relationship between food availability, food intake rate, food utilization, and growth rate. We distinguished between food intake rate and pumping rates by modeling the physical process of feeding. The results of our analysis are consistent with both an oscillation in pumping rates (Singh and Sulston, 1978) and a slow change in pharyngeal lumen size throughout development (Avery, 2003).

542 Previous research suggested that pumping frequencies within a larval stage are constant with sudden
543 transitions between lethargus and pumping (Nika et al., 2016). However, we were unable to resolve sudden
544 transitions because of the continuous smoothing of the kernel regression method used and population effects
545 (Fig 7B). Previous work has shown that growth rate increases with increasing food availability up to a
546 saturation limit (Uppaluri and Brangwynne, 2015). Varying bacterial concentration levels in future experiments
547 would allow us to distinguish whether mechanical control of food intake or metabolic control of food utilization
548 determine the upper bound on growth rate.

549 Our analysis of the relationship between growth rate and food intake rate quantified the interplay of metabolic
550 regulation and mechanical food intake. Mechanical food intake provides the upper bound of available food
551 resources for growth, but metabolic regulation substantially changes how much of this available food is utilized
552 for volumetric growth across development. Local extrema in metabolic regulation dynamics coincide with the
553 start of transition times. Within the L2 and L3 stages we observed a decoupling between growth rate and food
554 intake dynamics (Fig. 8 white region) twice. The first of these time periods corresponds to the times at which
555 the width-to-length ratio drastically changes and the second corresponds to ecdysis (S10 Fig). We estimated
556 that throughout larval stages metabolic resources allocated to non-growth processes varies much less than
557 food resources required for growth and maintenance. The oscillatory behavior of food utilization motivates the
558 need for further metabolomic experiments to probe metabolic regulatory dynamics. Higher time resolution
559 experiments on single animals in future experiments may be able to better resolve the existence of sudden
560 changes in metabolic regulation.

561 In the analysis of both the Stretcher and feeding models, we found that the L1 larval stage has different
562 dynamics than other larval stages. We observed a decrease in growth rate with no associated decrease in
563 feeding rate, corresponding to a mid-stage resource reallocation, that does not occur in any other larval stage,
564 possibly showing the dauer decision (Golden and Riddle, 1984) or the divisions of seam cells. Additionally,
565 within the L1 stage, the relative stretch measured in width and length did not follow the pattern observed in

other larval stages. We observed a mid-stage dip in the width-to-length ratio that is otherwise approximately constant throughout the L1 stage. As animals reallocate food resources in mid-L1, they also undergo a change in shape suggesting either directed growth or structural changes to either the cuticle or animal body (Fig 3, Fig 6, S8 Fig). Future experiments exploring the structural properties of cuticles at all larval stages may help to determine where the L1 shape changes originate.

Development comprises complex interactions of growth regulation across diverse scales

Our results demonstrate that *C. elegans* may use physical constraints on animal size and feeding rate to control growth rate and determine developmental transitions. This type of regulation could be applicable to organisms with stiff cuticles or other physical barriers to growth, like many species of Ecdysozoa. The control of whole-organism growth requires cells, tissues, and organs to orchestrate final size and cell number. In *C. elegans*, cell number is precisely defined and invariant from animal to animal (Horvitz and Sulston, 1980), so the final adult size of an individual must come from cell size as opposed to number. Future studies should focus on how whole-organism size is determined by the integration of cell, tissue, and organ size. By incorporating these different developmental scales, the Stretcher model can be refined to completely describe how physical constraints on parts of the organism impact the whole. *C. elegans* gives investigators a method to investigate animal-to-animal variation in developmental trajectories across each of these scales.

Methods

Worm culture

The canonical laboratory strain N2 was obtained from the *C. elegans* Natural Diversity Resource (Cook et al., 2016). Animals were cultured at 20°C on 6 cm plates of modified nematode growth media (NGMA), which contained 1% agar and 0.7% agarose seeded with *E. coli* OP50 bacteria (Andersen et al., 2014).

587 **Bacterial food**

588 *E. coli* HB101 bacteria were prepared from cultures grown for 15 hours in Superbroth and then pelleted by
589 centrifugation. HB101 bacteria were diluted to OD100 in K medium (51 mM NaCl, 32 mM KCl, 3 mM CaCl₂,
590 and 3 mM MgSO₄ in distilled water) and stored at -80°C. Bacteria were thawed and fed to animals at a
591 concentration sufficient to sustain population growth from hatching to adulthood (OD20).

592 **Growth of the animals**

593 Populations of animals were propagated on NGMA plates for two generations without starvation. In the third
594 generation, gravid adults were bleach-synchronized (Stiernagle, 2006). Embryos were resuspended in K
595 medium, aliquoted into a 500 mL flask at a concentration of one embryo per µL, and allowed to hatch
596 overnight. The following day, arrested L1s were fed HB101 bacteria at a final concentration of OD20 in a final
597 flask volume of 100 mL K medium and HB101 food. Animals were grown for three days at 20°C with constant
598 shaking. Following these three days, adult animals were bleach-synchronized once more and embryos were
599 aliquoted to seven replicate 500 mL flasks at a concentration of one embryo per µL in 100 mL. The following
600 morning, six flasks were fed HB101 bacterial food at a final concentration of OD20 in a final flask volume of
601 100 mL K medium and HB101 food. Two additional flasks were included to control for L1 animal size and
602 possible clumping of bacterial food: one flask contained L1 larvae but did not have food added and one flask
603 contained no larvae but the same concentration of HB101 bacteria as the six flasks containing L1 larvae. All
604 replicate flasks were kept in an incubator at 20°C with shaking for the duration of the experiment. A small
605 temperature gradient of 1.25°C was recorded in the shaking incubator with the highest temperature readings
606 on the right side and lowest temperature readings on the left side (S1 File). This slight variation in temperature
607 contributed to variation in developmental rate among replicates based on position within the incubator
608 (replicates were placed in numerical order with replicate 1 positioned on the far right side of the incubator).

609 **High-throughput measurements of body size and fluorescence**

610 Flasks were sampled each hour beginning one hour after feeding and continuing for 72 consecutive hours. At
 611 each hour, 500 μ L was removed from each flask and transferred to a well of a deep 96-well plate. Each flask
 612 was sampled at each time point. Fluorescent polychromatic beads (Polysciences, 19507-5) with a 0.5 μ m
 613 particle size were added to each well at a final concentration of 3.64×10^8 beads/mL and incubated at 20°C for
 614 10 minutes with shaking. Following the bead incubation, 30 μ L from each well of the deep 96-well plate was
 615 aliquoted to a 96-well microtiter plate. The process was repeated 11 times to 11 separate wells of the same
 616 microtiter plate with pipetting to mix the well contents from the deep 96-well plate. Animals were then treated
 617 with sodium azide at a final concentration of 50 mM to paralyze and prevent defecation of the ingested beads.
 618 The 96-well plate was imaged with an ImageXpress Nano (Molecular Devices, SanJose, CA) using both 2x
 619 (Nikon MRD00025) and 10x (Nikon MRH00101) objectives. The ImageXpress Nano acquires brightfield
 620 images using a 4.7 megaPixel CMOS camera. Images are stored in 16-bit TIFF format. Finally, animals were
 621 scored using a large-particle flow cytometer (COPAS BIOSORT, Union Biometrica, Holliston MA). The COPAS
 622 BIOSORT sheath flow rate was kept at a constant 10.3 ± 0.1 mL per minute to reduce variability in length
 623 measurements.

624 **Image processing**

625 Manual measurements of animal size were performed using the free Java image-processing program ImageJ
 626 (Abràmoff et al., 2004). Well images for the six replicate flasks, excluding controls were loaded into ImageJ
 627 software. Length was measured from head to tail, and width was measured at the widest point of the animal.
 628 Five animals were measured per well across thirty total wells for each hour. Measurements were repeated for
 629 all 72 time points in the assay. Body length and width were used to estimate cross-sectional area
 630 (length*width). This metric was used to describe animal area for the extent of the text. Volume was calculated
 631 from body length and width by approximating the animal as a cylinder. Pixels were converted to μ m using a
 632 conversion factor of 3.2937 pixels/ μ m.

633 Data processing

634 The COPAS BIOSORT was used to collect measurements of animal length (TOF), optical extinction (EXT),
 635 and fluorescence for every animal in each well. These traits measure properties of nematode development
 636 and, as such, increase as animals progress to adulthood (Andersen et al., 2015). Optical extinction
 637 measurements correspond to the amount of light absorbed over the full length of an animal as it passes
 638 through the instrument. An additional measurement (norm.EXT) can be calculated by normalizing optical
 639 extinction by length. The raw data collected were imported and processed using the *easysorter* R package
 640 (Shimko and Andersen, 2014).

641 The COPAS BIOSORT data were analyzed further using Gaussian finite mixture modeling as implemented in
 642 the *mclust* R package (Scrucca et al., 2016). These probabilistic models assume that data are generated from
 643 a mixture of multivariate normal distributions and, therefore, can be used to classify unstructured data into
 644 meaningful groups. Specifically, the *mclust* package fits a mixture model to data and selects the optimal
 645 number of clusters using an expectation-maximization algorithm and Bayes Information Criteria. For
 646 model-based clustering, log transformed animal length (logTOF) and log transformed optical extinction
 647 (logEXT) were used as inputs for the *Mclust* function. Data from each hour of the experiment was analyzed by
 648 replicate and clusters that did not appear to include majority animal objects were identified and removed as
 649 described previously (Smith et al., 2009). This processing removed non-animal objects such as bacterial
 650 clumps, shed cuticles, and next generation larval animals from the time-course data.

651 We used a numpy polyfit regression of well-median data from the COPAS BIOSORT and image measurements
 652 to convert TOF and norm.EXT data to microns (S5 File, Eq. S7-S9). Only the unit-corrected BIOSORT data
 653 were used for further analysis.

654 Molt analysis

655 Fluorescence data obtained from the COPAS BIOSORT was used as a proxy for feeding behavior to
 656 distinguish animals in a molt from growing animals. First, fluorescence was normalized by EXT to account for
 657 the ability of larger animals to consume more food and beads. Next, an analysis of variance statistical model
 658 was fit to the fluorescence data normalized by EXT to determine the amount of variance contributed by
 659 replicate and well (Table S1). A local kernel regression smoothing method was then applied to the residuals of
 660 the variance analysis using the *lokern* R package (Hermann, 2016). Residuals were used to address only the
 661 differences over time and ignore minor variation among replicates and wells. The local minima of the
 662 regression function were found by solving for where the first derivative of this function equaled zero. The time
 663 associated with each local minimum was used to represent the timing of each molt. Molts occurred at 14, 25,
 664 36, and 48 hours.

665 To identify periods of time that contained a majority of growing animals, the inflection points of the regression
 666 function were calculated by solving for where the second derivative of the function equaled zero. Time points
 667 between inflection points that did not contain a local fluorescence minimum were considered as growth
 668 periods. These hours were 1-13, 17-22, 27-32, and 39-45 corresponding to L1, L2, L3, and L4 growth periods.

669 Each molt is initiated when animals enter lethargus: a behavioral state where animals cease active feeding. To
 670 classify individual animals as in a molt or growing, we set a quiescence threshold using fluorescence
 671 measurements at each local minimum. The fluorescence measurement at each local minimum was as follows:
 672 0.07, 0.06, 0.06, 0.06. The average of these measurements (0.06) was used as the fluorescence threshold
 673 signifying quiescent behavior. Any individual animals that fell below this threshold fluorescence value were
 674 designated as in a molt and animals above this threshold value were classified as growing.

675 **Comparison of model fits**

676 To determine the volume growth model, we fit linear, exponential, and cubic functions to data designated as
 677 growth periods for each larval stage. Both linear and nonlinear functions were fitted using least-squares
 678 regression. Akaike's information criterion (AIC) (Sakamoto et al., 1986) and Bayesian information criterion
 679 (BIC) (Schwarz, 1978) were goodness of fit criteria used to evaluate candidate models. To assess the strength
 680 of evidence for each candidate model, we identified the model with the smallest AIC/BIC value and assessed
 681 the difference between this value and the AIC/BIC of the other two models. The magnitude of the difference
 682 was used to determine the level of support for each candidate model as previously described (Burnham and
 683 Anderson, 2007; Kass and Raftery, 1995). All model fits and analysis were performed using the *stats* R
 684 package.

685 **Stretcher and feeding model analysis**

686 To analyze shape dynamics, length and width data from growth time periods were extracted from the full
 687 COPAS BIOSORT population data and analyzed from each replicate separately to avoid issues with replicate
 688 variability. For replicate 2, the hours defining growth periods were 1-13, 16.37-22.39, and 26.93-32.96;
 689 corresponding to L1, L2, and L3. Hours defining larval stages were rounded as data was collected at exact
 690 hour increments. The L4 stage was excluded from the analysis because of the high variability within the
 691 population. We applied a local kernel regression, *lokern* R package ("Lokern: Kernel regression smoothing with
 692 local or global plug-in bandwidth," n.d.), to smooth the population dynamics of length and width. To calculate
 693 mean and standard deviation, the smoothed population measurements were bootstrapped using 2,000
 694 samples with replacement (S5 File, Algorithm S1). To determine cuticle properties throughout larval stages, we
 695 calculated the mean ratio of derivatives of regression width and length. Error for this ratio was calculated using
 696 error propagation to pass the bootstrap variation through the ratio (S5 File, Eq. S24-28).

697 To analyze volumetric growth dynamics and feeding dynamics, volume regression was calculated using a
 698 cylindrical approximation for animal shape (S5 File, Eq. S7-S9) and the same local kernel regression

699 previously described was applied to red fluorescence data. Volume growth rate was calculated using the
 700 python numpy gradient function applied to the volume regressions. An additional moving time window average
 701 (1.4 hours) was applied to smooth numerical errors in the derivative when determining feeding and growth
 702 regime transition points (S13 Fig).

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851 **Data availability**

852 The authors state that all data necessary to confirm the conclusions of this work are within the text, figures,
853 and supporting information files. All files and code for analysis and generation of figures and tables are
854 archived on GitHub (<https://github.com/AndersenLab/C.elegans-growth-manuscript>).

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Supporting Information Captions

S1 Fig. Raw measurements of animal size. Raw COPAS BIOSORT data of animal length (A), width (B), and volume (C) are shown here. After 60 hours, animals have developed to the adult stage. Smaller objects observed after 65 hours were the next generation of newly hatched L1 larvae laid by the animals that developed during the time course.

876

877 **S2 Fig. Correlation analysis of body size measurements.** Manual measurements of animal length, width,
878 and estimated area were compared to COPAS BIOSORT measurements of TOF, norm.EXT, and EXT. Kendall
879 correlation value is shown in each plot.

880 **S3 Fig. Mixture modeling of COPAS BIOSORT data was used to prune data.** Mixture models of Gaussian
881 distributions were fit to log transformed animal length (x-axis) and log transformed optical extinction (y-axis).
882 Data from each hour of the experiment was analyzed and processed to remove clusters that did not include
883 animal objects. All replicates were pruned independently; a subset of data from replicate 2 is shown here.
884 Panels indicate experimental hours from which data were taken.

S4 Fig. Fluorescence measurements normalized by body size. Red fluorescence beads were fed to animals during experimentation and fluorescence data was collected by the COPAS BIOSORT. Fluctuations in fluorescence indicate fluctuations in feeding behavior. Fluorescence data was normalized by body size measurements to account for increases in body size. Dividing fluorescence by area was most successful in normalizing fluorescence dynamics to account for changes in animal size over time.

S5 Fig. Cuticles identified during periods of decreased feeding. Images of wells collected during the experiment were examined for evidence of shed cuticles. (A) Experimental hours where cuticles were identified from images overlap with hours where population feeding behavior is low. Cuticles shed from the L4-Adult molt persisted longer than previous larval stage cuticle debris. (B) Example image of animal without visible cuticle during a period of elevated feeding. (C) Example image of an animal with visible cuticle indicating completion of molt during a period of decreased feeding.

S6 Fig. Volume growth data fit with linear, exponential, and cubic models. Volume data of individuals in 900 time points defined as growth periods are analyzed for each stage. L1 stage was further separated into two 901 periods to account for the volume dip that occurs mid-stage.

902

903 **S7 Fig. Density plots of population size dynamics across all larval transitions.** Density curves of length
904 (A), width (B) and volume (C). Curves are divided into five quantiles and colored by the percentage of
905 quiescent animals present within that quantile. Molts are estimated to occur at experimental hours 14, 25, 36,
906 and 48 (see Methods).

S8 Fig.

Animals in all replicates, measured from images. Animal length and width over *C. elegans* development captured from image data. Higher noise levels in these measurements preclude accurate regressions to individual larval stages. Length jumps and width dips are still apparent. Compare with Fig 6.

S9 Fig. Comparison of red fluorescence regression and food intake rate with defecation calculation. Regression of red fluorescence (dashed pink) is compared to the intake rate of red beads accounting for defecation rate (blue). Overlap of these two curves validates the use of red fluorescence as a proxy for food

S10 Fig. Timeline of Food Utilization and Stretcher events. In the first row (grey and white), we mark the slopes determined in the Stretcher model. Transition from lighter to darker grey indicates a step increase in slope corresponding to a stiffening cuticle in the length direction. White regions denote time between larval stages. L2 and L3 are the only stages at which we have useful slope information due to the change in slope observed during L1 making transitions difficult to determine and the high level of population desynchronization in L4. In the second row (green, red, and white), we mark the food and growth correlations found in Fig 5B. Green corresponds to times at which both growth rate and food rate are increasing. Red corresponds to times at which both growth rate and food rate are decreasing. White corresponds to times at which growth rate and food rate are uncorrelated. Transitions from green to red regions occur at roughly the same times as the transition to a stiffer cuticle in the length direction.

926

927 **S11 Fig. Analysis of Food intake and growth rate correlation for all replicates.** Summary of analysis in
928 Fig. 8 for all replicates. Until larval stage L4, most replicates followed the same pattern of transitions from one
929 growth regime to the next. The time delay at transitions in later replicates can be explained by the temperature
930 gradient and differences in growth between replicates.

Fit to Replicate 2

S12 Fig. Stretcher model analysis of replicate 2 COPAS BIOSORT data for different stage thresholding. Compare to Fig 5. Larval hours were defined by taking the ceiling of the lower boundary and the floor of the upper boundary. This rounding method for larval stage definition demonstrates the sensitivity of the analysis to edge effects. The unexpected step in the L2 larval stage (Fig 5) was significantly reduced with this rounding method.

S13 Fig. Sensitivity analysis to moving average window size. Varying lengths of window sizes (0.14 to 2.16 hours) were calculated for the *lokern* growth rate regression. Window size was increased until the growth rate regression was smoothed. A window size of 1.44 hours (or 0.72 hours on either side of each time point) was chosen to calculate the start and end times of each regime (Fig 8). Continued increase of window size past 1.44 hours did not change the pattern of regimes or their boundaries significantly.

S14 Fig. Time Lag Analysis. Subsections of food intake rate and growth rate regressions were compared to determine the existing time lag between the two curves. The time shift is applied to the volume growth rate. A correlation coefficient was calculated for the new volume growth rate curve and the untouched red fluorescence regression curve for each bootstrap regression. The solid line corresponds to the mean of all the correlation coefficients over the bootstrapping iterations and the shaded regions correspond to the standard deviation. The blue curve corresponds to hours containing L1 and L2, the orange curve corresponds to hours containing L2 and L3, and the green curve corresponds to hours containing L3 and L4. The time lag at which the correlation between Red fluorescence and volume growth rate is at a maximum corresponds to the apparent time lag between the two curves. No single time lag captures the entirety of development.

S15 Fig. Time Lag Analysis. Dynamics over all development for food intake rate and growth rate regressions were compared to determine the existing time lag between the two curves. The time shift was applied to the volume growth rate. A correlation coefficient was calculated for the new volume growth rate curve and the untouched red fluorescence regression curve for each bootstrap regression. The solid line corresponds to the mean of all the correlation coefficients over the bootstrapping iterations and the shaded regions correspond to the standard deviation. Due to the qualitatively different dynamics in L1, we calculated correlation for L1-L4 (blue), the second half of L1 -L4 (orange), and L2-L4 (green). All curves show that there is an overall time shift of +1 hour (meaning changes in volume growth rate precede changes in food intake rate), matching the L3-L4 curve in S14 Fig but still a <90% correlation with no time lag.

Response = Norm.Red

<i>Terms</i>	<i>Df</i>	<i>Sum Sq</i>	<i>Mean Sq</i>	<i>F value</i>	<i>Pr(>F)</i>	<i>% Var Explained</i>
hour	1	439.46	439.46	217762.01	0	54.34
replicate	6	165.82	27.64	13694.48	0	20.51
well	10	0.32	0.03	15.62	0	0.04
Residuals	100619	203.06	0	NA	NA	25.11

Response = Length

<i>Terms</i>	<i>Df</i>	<i>Sum Sq</i>	<i>Mean Sq</i>	<i>F value</i>	<i>Pr(>F)</i>	<i>% Var Explained</i>
hour	1	86190107879	86190107879	8223506	0	98.4
replicate	6	349438944	58239824	5557	0	0.4
well	10	834970	83497	8	0	0
Residuals	100619	1054582098	10481	NA	NA	1.2

Response = Width

<i>Terms</i>	<i>Df</i>	<i>Sum Sq</i>	<i>Mean Sq</i>	<i>F value</i>	<i>Pr(>F)</i>	<i>% Var Explained</i>
hour	1	209090438.47	209090438.47	6950760.3	0	97.99
replicate	6	1266985.87	211164.31	7019.7	0	0.59
well	10	1495.32	149.53	4.97	0	0
Residuals	100619	3026786.99	30.08	NA	NA	1.42

Response = Volume

<i>Terms</i>	<i>Df</i>	<i>Sum Sq</i>	<i>Mean Sq</i>	<i>F value</i>	<i>Pr(>F)</i>	<i>% Var Explained</i>
hour	1	621712474191714688	621712474191714688	843342	0	84.08
replicate	6	43356968850687072	7226161475114512	9802	0	5.86
well	10	152458715405862	15245871540586	21	0	0.02
Residuals	100619	74176459811167296	737201321929	NA	NA	10.03

S1 Table. Results of analysis of variance models fit to COPAS BIOSORT data. Analysis of variance tests were used to quantify the amount of variance in our data contributed by the sampling technique. The sampling technique involved unbiased sampling of animals from six replicate populations and subsequent distribution into multiple wells of a microtiter plate for analysis. We quantified the amount of variance contributed by

replicate and well. We find that the variance explained by well is nearly negligible whereas replicate contributes minor variance in some measurements. Given this information, we deem the generated summary statistics an appropriate representation of the population.

Stage	ΔAIC			ΔBIC			Best model by AIC	Best model by BIC
	Linear	Exponential	Cubic	Linear	Exponential	Cubic		
L1_1	17	21	0	4	9	0	Cubic	Likely Cubic
L1_2	2	4	0	0	2	12	Can't distinguish	Can't distinguish
L2	142	43	0	128	28	0	Cubic	Cubic
L3	374	145	0	360	131	0	Cubic	Cubic
L4	4	44	0	0	40	10	Likely Cubic	Linear

S2 Table. Model fit criteria used to assess candidate growth models. To determine the level of support for each model, the candidate model with the smallest raw AIC/BIC was identified and compared to other AIC/BIC values. If the delta value was greater than 6, the model with the smallest AIC/BIC value was denoted as the best model. If the delta value was less than 6 but greater than 2, the model with the smallest AIC/BIC value was determined to likely be the best model. If the delta value was less than 2, we are unable to distinguish the model of best fit.

Green Regions

Stage	Food Intake Dynamical Range (AFU)	Food to Growth Dynamical Range - Lower Estimate (AFU)	Food to Growth Dynamical Range - Higher Estimate (AFU)
L1 (1)	1	0	0
L1 (2)	1	2	2
L2	15	12	15
L3	29	21	27
L4	65	54	69

Red Regions

Stage	Food Intake Dynamical Range (AFU)	Food to Growth Dynamical Range - Lower Estimate (AFU)	Food to Growth Dynamical Range - Higher Estimate (AFU)
L1	--	--	--
L2	1	4	5
L3	6	3	4
L4	16	27	35

White Regions Preceding Molt

Stage	Food Intake Dynamical Range (AFU)	Food to Growth Dynamical Range - Lower Estimate (AFU)	Food to Growth Dynamical Range - Higher Estimate (AFU)
L1 -> L2	2	3	4
L2 -> L3	3	1	2
L3 -> L4	5	2	3
L4 -> Adult	5	2	3

Whole Larval Stage

Stage	Food Intake Dynamical Range (AFU)	Food to Growth Dynamical Range - Lower Estimate (AFU)	Food to Growth Dynamical Range - Higher Estimate (AFU)
L1	4	2	3
L2	19	12	15
L3	29	21	28
L4	70	52	67

974 **S3 Table.** Comparison of dynamical ranges between total food intake and food used for growth.

975 **S1 File. Incubator temperature data.** Temperature recordings of each position within the shaking incubator

976 used for the growth experiment. (CSV)

977 **S2 File. COPAS BIOSORT growth data.** Raw growth data collected from the COPAS BIOSORT and
 978 processed using the *easysorter* R package to compile information from each well. (CSV)

979 **S3 File. Pruned COPAS BIOSORT growth data.** Processed data from the COPAS BIOSORT following
 980 implementation of the *mclust* R package and removal of clusters containing non-animal objects. (CSV)

981 **S4 File. Image growth data.** Manual measurements of animal size acquired from images. (CSV)

982 **S5 File. Model derivations.**

Model Derivations

Bootstrapping Algorithm

To calculate a robust regression of the measured COPAS BIOSORT data we bootstrap the regression using case-resampling (Davison and Hinkley 1997, pages 261-266). Each iteration of the algorithm (**Algorithm S1**) involves resampling the data of interest with replacement and maintaining the size of the sample. At each iteration the lokern regression is calculated for Red, Length, and Width data. Additionally any desired function (for example, volume, pumping frequency times pharynx fraction, or derivatives) of these regressions is calculated at each iteration. Regressions at each iteration are saved and the mean and variance of these regressions at each regression time point are used to determine the statistics of the regression.

Algorithm S1 Regression Bootstrapping with Case Resampling

Ndata = # animals in sample;

iterations = # resamplings;

for $i = 0$ to iterations **do**

 Resample Ndata points with replacement. Collect Red, Length, Width data;

 Apply lokern regression to resampled Red, Length, Width;

 Calculate desired functions of Red, Length, Width regressions;

 Save Red, Length, Width, and combined regressions;

end for

 Calculate Standard deviation at each regression time point of saved regressions;

Derivation of eating model

We begin by defining the instantaneous rate of food intake as a function of the flow rate of media through the buccal cavity and the cross sectional area of the buccal cavity.

$$\frac{dV_{food}}{dt} = A_{buccal} \quad (S1)$$

We then make the assumption that the uptake of media fills the pharyngeal lumen we have

$$\frac{dV_{food}}{dt} = C \frac{dV_{lumen}}{dt} \quad (S2)$$

We average both sides of the equation under the assumption that the pumping period is significantly shorter than the time scale of growth

$$\frac{1}{T} \int_0^T \frac{dV_{food}}{dt} dt = \frac{1}{T} \int_0^T C A_{buccal} \quad (S3)$$

The integral on the right hand side is the total food intake during a single pumping period.

$$\frac{1}{T} \int_0^T \frac{dV_{food}}{dt} dt = \frac{1}{T} \Delta V_{food} \quad (S4)$$

We then take into account that food is not transported to the gut in the same step as its uptake. Thus the total food intake during a single pump can be calculated by the amount of food that fills the fully opened pharyngeal lumen

$$\frac{1}{T} \int_0^T \frac{dV_{food}}{dt} dt = \frac{C}{T} V_{lumen:max} \quad (S5)$$

We then replace the average on the right hand side with the average food intake rate over the pumping period. For simplicity and because we will deal entirely with the average food intake rate, we do not use a different notation for this average rate.

$$\frac{dV_{food}}{dt} = \frac{C}{T} V_{lumen:max} = C f(t) V_{lumen:max} \quad (S6)$$

Transformation of sorter measurements to volume units

To utilize sorter measurements and convert them to meaningful units we define a linear transformation from the correlation plots (S1 Fig)

$$L = a_1 TOF + b_1 \quad (S7)$$

$$W = a_2 norm.EXT + b_2. \quad (S8)$$

Using Equations (S7) and (S8) we can approximate the volume of any object that passes through the sorter by the expression

$$V = \frac{\pi}{4} (a_1 TOF + b_1) (a_2 norm.EXT + b_2)^2. \quad (S9)$$

Defecation analysis

We use the defecation results found in (Liu and Thomas 1994) to determine if red fluorescent measurements can be used as a proxy for food intake rate as opposed to the instantaneous food volume in the gut. Defecation in adults happens very regularly, with a period of $T_d = 45 \pm 3s$, with $h_d = 43 \pm 10\%$ of their intestinal volume being expelled each time. The volume expelled is well mixed. Defining V_f as the current amount of food in the nematode gut. We can use conservation of mass to state that the rate of change in the amount of food in the gut is equal to the rate of food intake through eating less the defecation rate and the rate at which food volume is metabolized into cell products:

$$\frac{dV_f}{dt} = \frac{dV_f}{dt}\Big|_{\text{eating}} - \frac{dV_f}{dt}\Big|_{\text{defecating}} - \frac{dV_f}{dt}\Big|_{\text{metabolized}} \quad (\text{S10})$$

Using red fluorescence as a proxy for food intake we can ignore the metabolism term as the fluorescent beads are not metabolized.

$$\frac{dV_f}{dt} = \frac{dV_f}{dt}\Big|_{\text{eating}} - \frac{dV_f}{dt}\Big|_{\text{defecating}} \quad (\text{S11})$$

Equation (S11) states that the rate of change of the volume of fluorescent beads in the gut is equal to the difference between the intake of red fluorescent beads minus the defecation rate of red fluorescent beads. Using the results of (Liu and Thomas 1994) for the second term, and defining $V_{f:\max}$ as the volume of food in the gut just prior to defecation, h_d as the fraction of food expelled during a single defecation cycle, and T_d as the period of defecation. We average Equation (S11) over short time periods to remove the pumping and defecation period oscillations.

$$\frac{dV_{\text{red}:\max}}{dt} = \frac{dV_{\text{red}}}{dt}\Big|_{\text{eating}} - \frac{V_{\text{red}:\max}h_d}{T_d} \quad (\text{S12})$$

On the left hand side, the instantaneous rate of the gut red fluorescence in Equation (S11) is replaced by the rate of change of the maximum or “full” gut fluorescence. The second term on the right hand side of Equation (S11) has been replaced by the average defecation rate over a cycle calculated by multiplying the full gut fluorescence by the fraction expelled and dividing by the defecation period. We solve Equation (S12) for the average eating rate.

$$\frac{dV_{\text{red}}}{dt}\Big|_{\text{eating}} = \frac{dV_{\text{red}:\max}}{dt} + \frac{V_{\text{red}:\max}h_d}{T_d} \quad (\text{S13})$$

We take the local regression of the red fluorescence to determine $V_{\text{red}:\max}(t)$. This value is plugged into

the second term on the right hand side of Equation (S13) and its derivative is used to approximate the first term on the right hand side of Equation (S13). We take the adult values of h_d and T_d (Liu and Thomas 1994) as a first approximation. Figure (S6) demonstrates a comparison of the red fluorescence and the red intake rate with defecation taken into account at the constant adult rates and quantities. We have scaled both the pink curve denoting red fluorescence and the blue curve denoting red intake rate by their maximum. This scaling allows us to see that the two curves are only a multiplicative factor apart up to error bars. This allows us to use the red measurement as a proxy for both red and food intake rates.

Food Allocation Breakdown Calculation

We calculate an example of resource allocation breakdown. We begin with the expression in Equation (8) of the main text relating food intake rate and animal growth rate and repeated here:

$$\frac{dV_{worm}}{dt} = \eta(t)\alpha(t)\frac{dV_{food}}{dt} \quad (S14)$$

Here $\eta(t)$ is metabolic efficiency and is characteristic of the nematodes and food source used. $\alpha(t)$ is the fraction of total ingested food allocated towards growth.

We make an additional assumption that food needed to maintain life is proportional to animal volume:

$$\frac{dV_{food:maint}}{dt} = \beta V_{worm}(t) \quad (S15)$$

Here we define $\frac{dV_{food:maint}}{dt}$ as the rate of food intake required to maintain life and β is the constant of proportionality that relates animal size to required maintenance food levels. We assume that β is a constant over developmental time and depends on the food source available.

From the analysis from the previous section we can use red fluorescence as a proxy for food intake rate such that

$$\frac{dV_{food}}{dt} \propto Red \quad (S16)$$

$$\frac{dV_{worm}}{dt} \propto \eta(t)\alpha(t)Red \quad (S17)$$

$$\eta(t)\alpha(t) \propto \left(\frac{dV_{worm}}{dt}\right)/Red \quad (S18)$$

The constant of proportionality in Equation (S18) is unknown due to the unknown relationship between food volume and red fluorescence. We make the assumption that metabolic efficiency is constant over time

and any variation in the value calculated by Equation (S18) is due to changes in $\alpha(t)$, the allocation of food toward growth.

To calculate an estimate for the breakdown of food allocation, we assume a set of constants of proportionality for Equations (S15) and (S18). We assume that at the time at which the $\eta(t)\alpha(t)$ curve is at its maximum (hour 40), 10% of food resources are allocated towards maintenance, 70% (low growth estimate) or 90% (high growth estimate) are allocated towards growth, and the remainder is allocated to other metabolic processes. The resulting scaling factors are applied over developmental time to calculate an estimated food allocation breakdown and presented in Figure (8) of the main text.

Derivation of Stretcher Model

We model the cuticle as a thin walled pressure vessel made of orthotropic, linear materials to capture the relationship between how much the cuticle stretches and the force applied to the cuticle. The relationship between the amount of stretch and the amount of applied pressure is described by the matrix:

$$\begin{bmatrix} \varepsilon_L \\ \varepsilon_{Circ} \end{bmatrix} = \begin{bmatrix} \frac{1}{E_L} & \frac{-v_{cl}}{E_c} \\ \frac{-v_{lc}}{E_L} & \frac{1}{E_c} \end{bmatrix} \begin{bmatrix} \sigma_L \\ \sigma_{Circ} \end{bmatrix} \quad (\text{S19})$$

Here E_L and E_C are the Young's modulus in the length and circumferential direction, and v_{cl} and v_{lc} are the appropriate Poisson's ratios. These material properties can be measured experimentally. Normalized stretch, ε , is defined as the change in size normalized by the initial size of a cuticle in length (L) and circumference (Circ) (Equations S20 - S21). Here σ is the normalized force applied along the length and circumferential directions of the cuticle (Equations S23 - S24).

$$\varepsilon_L = \frac{\Delta L}{L_0} \quad (\text{S20})$$

$$\varepsilon_{Circ} = \frac{\Delta Circ}{Circ_0} \quad (\text{S21})$$

Here L_0 and $Circ_0$ are the length and circumference of the cuticle at the onset of stretch, or in other words at the start of a larval stage. Experimentally we measure width, not circumference, but the circumference of a circle is proportional to the width of the circle, so we can replace the circumference with the measured width:

$$\frac{\Delta Circ}{Circ_0} = \frac{\pi \Delta W}{\pi W_0} = \frac{\Delta W}{W_0} \quad (\text{S22})$$

By approximating *C. elegans* as cylindrical, and assuming the only force working on the cuticle is isotropic internal pressure, we can determine the normalized force in terms of pressure and geometric properties:

$$\sigma_L = \frac{r}{2t} \Delta p \quad (\text{S23})$$

$$\sigma_{Circ} = \frac{r}{t} \Delta p \quad (\text{S24})$$

Where r is the radius of the cylinder and t is the thickness of the cuticle. We can now rewrite Equation (S19) in terms of measurable quantities (length and width) by multiplying out the matrices making the appropriate substitutions.

$$\Delta L = \frac{L_0 r}{t} \left(\frac{1}{2E_L} - \frac{v_{cl}}{E_c} \right) \Delta p = a_L \Delta p \quad (\text{S25})$$

$$\Delta W = \frac{W_0 r}{t} \left(\frac{1}{E_C} - \frac{v_{lc}}{E_L} \right) \Delta p = a_W \Delta p \quad (\text{S26})$$

Here we compress the coefficients fixed by material and geometric properties into one constant

$$a_L = \frac{L_0 r}{t} \left(\frac{1}{2E_L} - \frac{v_{cl}}{E_c} \right) \quad (\text{S27})$$

$$a_W = \frac{W_0 r}{t} \left(\frac{1}{E_c} - \frac{v_{lc}}{E_L} \right) \quad (\text{S28})$$

Stretcher Slope Calculations

The Stretcher model predicts a constant ratio between stretch in width, ΔW , and stretch in length, ΔL . These measures of stretch are changes in the length and width measurements over some period of time. To see how the ratio of $\frac{\Delta W}{\Delta L}$ changes throughout a larval stage, we need to measure the stretch instantaneously. To do this we take advantage of the derivative approximation

$$\Delta W \approx \frac{dW}{dt} \Delta t \quad (\text{S29})$$

$$\Delta L \approx \frac{dL}{dt} \Delta t \quad (\text{S30})$$

Equations (S29, S30) are combined in the ratio found in Equation (3) to give:

$$\frac{\Delta W}{\Delta L} \approx \frac{W'(t)}{L'(t)} \quad (\text{S31})$$

Here $W' = \frac{dW}{dt}$ and $L' = \frac{dL}{dt}$. We differentiate the time series from the local regressions of length and width data. The ratio of derivatives gives the instantaneous stretch ratio as it changes over time. Due to the numerical difficulty of calculating both derivatives and ratios with accuracy, we expect large error bars for this ratio. To estimate the size of error bars we apply a first order error propagation formula to Equation (S31).

$$\sigma_{Ratio}^2 \approx \left| \frac{\partial Ratio}{\partial (W')} \right|^2 \sigma_{(W')}^2 + \left| \frac{\partial Ratio}{\partial (L')} \right|^2 \sigma_{(L')}^2 + 2 \frac{\partial Ratio}{\partial (W')} \frac{\partial Ratio}{\partial (L')} \sigma_{(W')(L')} \quad (\text{S32})$$

$$\sigma_{Ratio}^2 \approx \left| \frac{1}{L'} \right|^2 \sigma_{(W')}^2 + \left| \frac{-(W')^2}{(L')^3} \right|^2 \sigma_{(L')}^2 - 2 \frac{W'}{(L')^3} \sigma_{(W')(L')} \quad (\text{S33})$$

The variance in Equation (S33) is calculated for each time point in the regressions of length and width. We resample the data for each larval stage 2,000 times with replacement (see Methods for larval stage determination). For each of these resampled sets of data, we numerically differentiate the length and width regression to determine an estimate of the length and width derivatives over time. At each time point the mean regression length and width derivatives are used in place of W' and L' . The covariance matrix for the length and width derivatives is calculated at each time point using the 2,000 resampled regressions in the bootstrap analysis and used as the variance terms in Equation (S33).