1 Highly scaled measurements of *C. elegans* development suggest that physical

2 constraints guide growth trajectories and animal shape

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25 Abstract

Growth control establishes organism size, requiring mechanisms to sense and adjust growth. Studies of single 26 cells revealed that size homeostasis uses distinct control methods: Size, Timer, and Adder. In multicellular 27 organisms, mechanisms that regulate single cell growth must integrate control across organs and tissues 28 during development to generate adult size and shape. We leveraged the roundworm Caenorhabditis elegans 29 as a scalable and tractable model to collect precise growth measurements of thousands of individuals, 30 measure feeding behavior, and quantify changes in animal size and shape. Using quantitative measurements 31 and mathematical modeling, we propose two models of physical mechanisms by which C. elegans can control 32 33 growth. First, constraints on cuticle stretch generate mechanical signals through which animals sense body size and initiate larval-stage transitions. Second, mechanical control of food intake drives growth rate within 34 larval stages. These results suggest how physical constraints control developmental timing and growth rate in 35 36 C. elegans.

37 Introduction

Growth is a complex process fundamental to development. Individual cells and whole animals must reach an 38 appropriate size to remain competitive in their environment. A larger body size conveys many selective 39 advantages to an organism, including increased predation success or defense against predation, increased 40 success in mating, and increased success in intraspecific as well as interspecific competition. Offsetting these 41 advantages, larger organisms require more food resources to grow, take longer to develop, and produce fewer 42 offspring (Hone and Benton, 2005). Therefore, it is critical for multicellular organisms to effectively coordinate 43 the growth of both individual cells and the whole body. Additionally, growth at both of these scales must be 44 coupled with developmental progression to ensure the proper timing of irreversible developmental events. 45

In recent years, efforts have focused on understanding how organisms control growth to achieve size 46 homeostasis (Björklund, 2019; Turner et al., 2012; Willis and Huang, 2017). Many of these studies are 47 motivated by the decades-long debate about whether growth is linear or exponential; two separate models 48 each having unique implications for size regulation. In a linear model with constant growth rate, smaller 49 organisms must grow proportionally more than larger organisms to maintain size homeostasis. In this 50 paradigm, organism size can be controlled simply by specifying growth duration. Subsequently, this method of 51 growth control was named the 'Timer' model (Donnan and John, 1983; Wang et al., 2000). Instead of 52 regulating growth duration, organisms can monitor size and adjust duration of growth to reach an optimal size, 53 often named the 'Sizer' model (Pavelescu et al., 2018; Sveiczer et al., 1996; Tzur et al., 2009). In an 54 exponential model, growth rate is proportional to size. Here, a time-based control mechanism alone would fail 55 to maintain size homeostasis because larger organisms would grow proportionally more during a specified 56 period of time. This difference in growth requires a size-based control mechanism to ensure that growth is 57 halted once a maximum size is reached. Although 'Timer' and 'Sizer' are the most often proposed size-control 58 models, other models have been suggested, including 'Adder' in which a fixed volume is added to a cell or 59 organism during growth (Campos et al., 2014; Taheri-Araghi et al., 2015), and 'Folder' in which the organism 60 increases in volume by a fixed proportion (Towbin and Grosshans, 2021). It is not trivial to determine which 61

model most accurately describes growth of individual cells or whole organisms because quantitative 62 measurements of growth must be collected at high precision and throughput under tightly controlled 63 experimental conditions. In unicellular organisms, the development of high-throughput experimental techniques 64 in combination with theoretical models have advanced the understanding of size control (Cadart et al., 2018; 65 Jorgensen and Tyers, 2004; Osella et al., 2014; Soifer et al., 2016; Wang et al., 2010). Progress has been 66 slower for multicellular organisms because cell growth within tissues and tissue growth within organisms often 67 progress at different rates, suggesting that they are likely not regulated in the same ways (Moss-Taylor et al., 68 2019; Spence, 2009; Uppaluri et al., 2016). 69

70 The nematode *Caenorhabditis elegans* presents both a scalable and tractable multicellular animal model to study growth control. With an adult body length of approximately 1 mm, hundreds of thousands of individuals 71 are easily cultured in controlled laboratory conditions (Wood, 1988). Moreover, C. elegans post-embryonic 72 development is marked by several molts that provide clear developmental milestones (Page and Johnstone, 73 74 2007a). Each molt is initiated by a period of inactivity (lethargus) and terminated once the animal successfully 75 sheds its collagen-rich outer cuticle (ecdysis) (Singh and Sulston, 1978). Four molts separate the C. elegans life cycle into five distinct stages: four larval stages (L1-L4) and adult. The timing of these molts determines the 76 completion of stage-specific development (Monsalve et al., 2011; Zaidel-Bar et al., 2010) and underscores the 77 importance of growth regulation during C. elegans larval development. 78

79 A full description of an organism's development includes the assessment of how growth and body size are 80 regulated. Initial studies of *C. elegans* development described whole-organism growth as a sigmoidal curve 81 characterized by continuous larval growth in length that reaches saturation in adulthood (Byerly et al., 1976). 82 These early studies hypothesized that molt events had little effect on continuous growth as the *C. elegans* 83 cuticle allowed for stretch during larval stages. Later work determined that larval progression was not 84 continuous but rather piecewise in nature (Knight et al., 2002). This study showed that *C. elegans* volumetric 85 growth rate increased from stage to stage such that L1 animals had the slowest rate of growth and L4 animals

86 had the fastest. This finding suggests that *C. elegans* have a mechanism for regulating growth rate, potentially at each molt. Next, researchers using single-animal imaging strategies observed that animals did not advance 87 to the next developmental stage until a critical volume was reached (Uppaluri and Brangwynne, 2015). This 88 finding suggests that C. elegans growth follows a 'Sizer' model with each molt decision controlled by a volume 89 threshold and further implies that individual cells are able to communicate information about body size to 90 precisely regulate growth. Most recently, live imaging and characterization of body volume heterogeneity 91 revealed that with respect to the start of a larval stage. C. elegans volume fold change within a stage is nearly 92 invariant thereby preventing rapid divergence in volume between fast and slow growing animals (Towbin and 93 Grosshans, 2021). 94

Extensive characterization of C. elegans body size mutants has revealed several processes that influence 95 growth rate and body size (Tuck, 2014). A number of genes act through signaling pathways to influence growth 96 and body size (McKeown et al., 1998; Patterson and Padgett, 2000). Some of these pathways contribute to 97 body size control by regulating cuticle collagen genes (Madaan et al., 2018). Alternatively, mutations in some 98 cuticle collagen genes directly disrupt the physical structure of the cuticle (Page and Johnstone, 2007b). These 99 structural changes act as physical constraints on growth as opposed to regulatory mechanisms of growth 100 control. Environmental factors also play a significant role in C. elegans growth control. Food restriction is 101 known to decrease growth rate or, when extreme, induce complete developmental arrest (Baugh, 2013; Hu, 102 2018; Uppaluri and Brangwynne, 2015). In C. elegans, mutations that disrupt the ability to properly consume 103 food also cause individuals to be small and thin, indicating that food intake can act as a physical constraint on 104 growth and body shape (Mörck and Pilon, 2006). 105

To understand *C. elegans* growth control at the whole-organism level, precise measurements of body size and shape for large numbers of individuals are required. Using a combination of quantitative growth measurements and mathematical modeling, we performed a high-resolution longitudinal study of *C. elegans* larval progression and captured high-precision details about animal length, width, volume, and feeding dynamics. By investigating

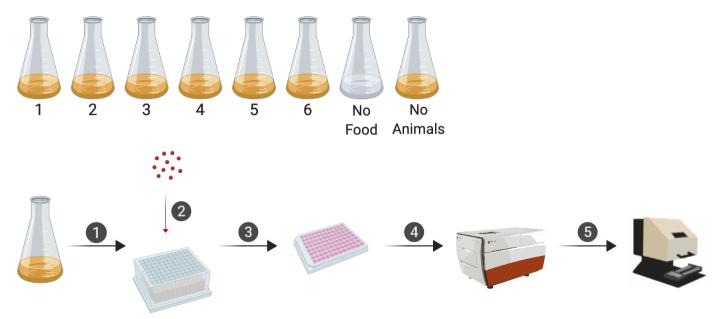
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110 C. elegans feeding and growth in tandem for thousands of individual animals, we found decreases in feeding behavior associated with each larval transition that were also correlated in time with changes in growth. We 111 used our large-scale measurements of body size to further analyze the periods of time surrounding each larval 112 transition. At each molt, we observed simultaneous increases in length, decreases in width, and maintenance 113 of volume, suggesting that body shape in addition to size plays a role in the control of C. elegans growth. 114 Given these data, we propose a "Stretcher" mechanism for growth control whereby *C. elegans* senses body 115 size through physical constraints on cuticle stretch and undergoes larval-stage transitions when the cuticle 116 reaches its maximum capacity for stretch. Additionally, we propose that C. elegans are able to physically 117 constrain growth rate by modulating food intake. We used guantitative models of eating and growth to evaluate 118 our data and predicted that the rate of volumetric growth is controlled by animal feeding rate and metabolic 119 regulation. Food allocated toward growth reached maxima and minima at larval transitions, indicating 120 increased metabolic control at these points in development. 121

122 **Results**

123 Quantitative measurements of C. elegans growth

We have optimized a quantitative growth assay that reliably measures small changes in *C. elegans* body size 124 125 throughout development (Fig 1). Our method provides both high-throughput and high-precision assessment of developmental growth. In brief, populations of 100,000 animals were cultured in flasks. We cultured six 126 replicate populations of *C. elegans* for a total of 600,000 synchronized and growing animals. Every hour after 127 feeding, a sample of the population from each flask (~300 animals/flask) was collected to measure animal 128 length, width, and feeding rate. Feeding rate, examined using fluorescent microspheres, and body size were 129 measured using the COPAS BIOSORT (Union Biometrica). Then, the ImageXpress system (Molecular 130 Devices) was used to collect images of sampled animals. This platform allowed for the further analysis of life 131 132 stage and body size, contributing added precision to our measurements.



133 Fig 1. An overview of the quantitative growth assay.

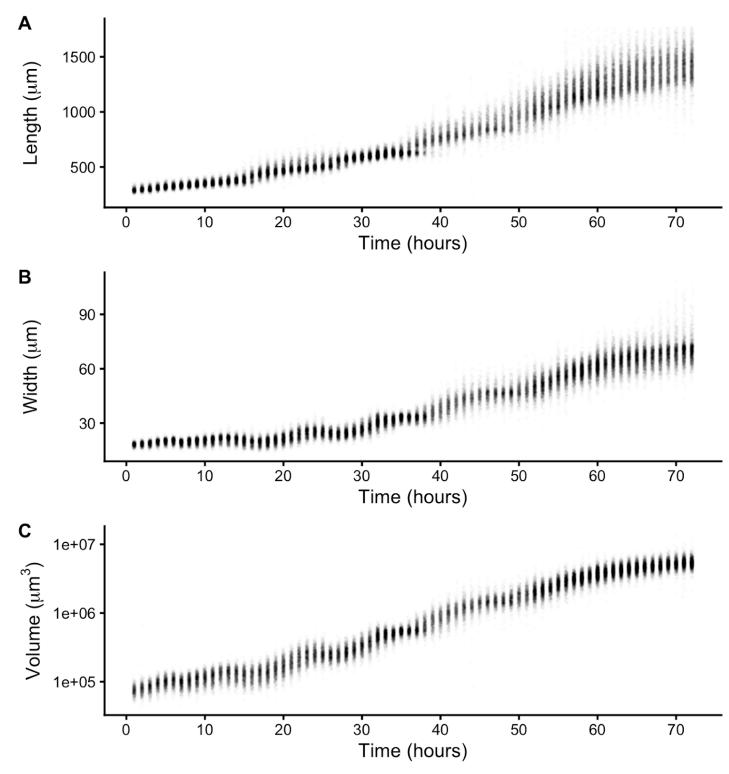
Schematic of the experimental workflow was created with BioRender.com. Synchronized animals were cultured in flasks where six flasks contained replicate populations of nematodes, one flask had a population of unfed animals, and one flask only contained bacterial food. At each hour of the experiment, all eight flasks were sampled. In step 1, animals were transferred from each flask to a single well of a 96-well microtiter plate. In step 2, fluorescent beads were added to each well. Following a 10-minute incubation period, animals from each well of the deep-well plate were transferred to several wells of a 96-well microtiter plate for step 3. In step 4, animals in each well of the microtiter plate were imaged. In step 5, the same animals were measured using the COPAS BIOSORT. This process was repeated every hour after feeding for 72 consecutive hours (see Methods).

143 The raw data from the quantitative growth assay provides measurements of body size and feeding behavior, 144 which are traits related to animal growth. Two measurements of body size were collected from raw data taken 145 from the COPAS BIOSORT: time of flight (TOF) and optical extinction (EXT) (S1 Fig). Time of flight is a measurement of body length, and optical extinction corresponds to optical density, a measurement influenced 146 147 by body length, thickness, and composition (Andersen et al., 2015; Pulak, 2006). We investigated whether optical extinction could be correlated to a different measure of body size using the collection of manual size 148 149 measurements from images (see Methods). We calculated the median length, width, area, and volume of 150 animals in a subset of imaged wells from each hour of the experiment. We then compared these values to well 151 median statistics from the processed COPAS BIOSORT data. We found a strong correlation between manual 152 measurements of animal length from the image analysis and TOF measurements from the COPAS BIOSORT

(S2 Fig). We also observed an equally strong correlation between manual measurements of animal area and EXT as well as animal width and EXT normalized by body length (norm.EXT). We then approximated animal volume using measurements from the COPAS BIOSORT by using a cylindrical approximation for *C. elegans* shape (see Methods). This result expanded the number of body size parameters that we were able to assess using the COPAS BIOSORT data, allowing us to investigate growth dynamics in length, width, and volume (Fig 2A-C). To disentangle nematode objects from non-animal objects (bacteria clumps, detritus, shed cuticles), we employed model-based clustering to remove unwanted objects and better examine growth of animals (S3 Fig).

160 Lastly, we converted COPAS BIOSORT measurements into microns (see Methods).

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161 Fig 2. Quantitative measurements of animal size.

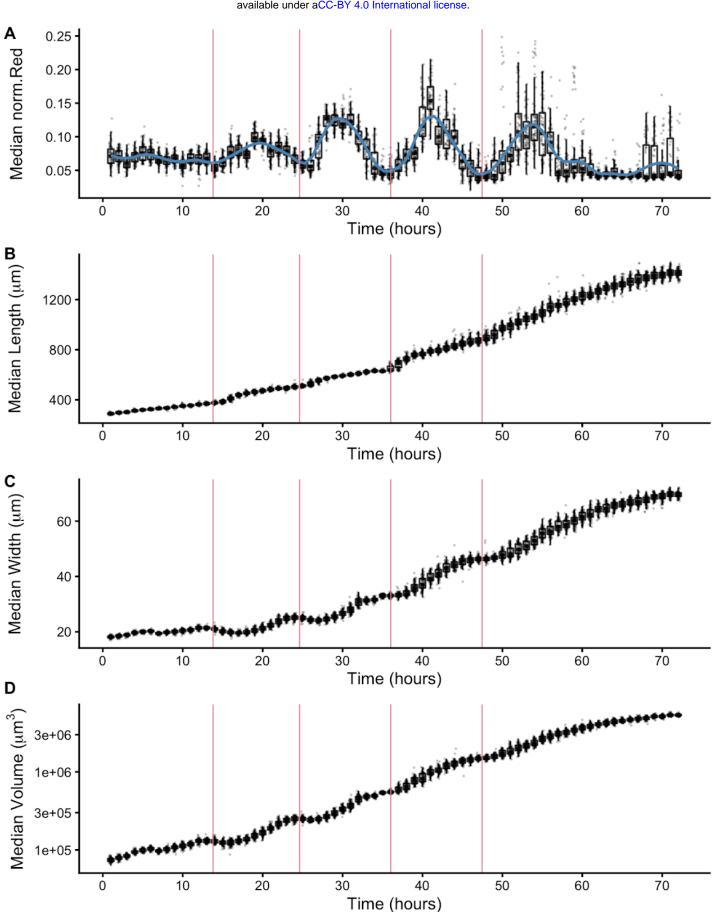
162 COPAS BIOSORT data of animal length (A), width (B), and volume (C) after the removal of non-animal objects 163 using model-based clustering methods (see Methods).

164 We report body length, width, and volume of animals at each hour of development from L1 to adult (S1 Fig and 165 Fig 2). Historically, growth of C. elegans has been shown as a sigmoidal curve where exponential growth during larval stages reaches a maximum rate in adulthood (Byerly et al., 1976). More recently, researchers 166 have identified that growth curves are discontinuous during development punctuated by larval transitions 167 (Knight et al., 2002; Uppaluri and Brangwynne, 2015). Using our quantitative growth assay, we captured these 168 small-scale discontinuities in larval growth as well as an apparent growth maximum during early adulthood. We 169 noticed that all size variables (length, width, and volume) displayed these dynamics. Objects identified as 170 animals appear to grow in size. However, in particular time windows during development, growth dynamics 171 visibly shift, producing discontinuities in animal growth rate. With these data, we were able to further 172 173 investigate *C. elegans* growth and size control.

174 Fluorescence provides a quantitative measurement of animal feeding behavior and 175 developmental progression

In addition to body size and shape, the raw data from the quantitative growth assay described above measured 176 fluorescence of each animal object. To readily assess the thousands of measurements acquired at each hour. 177 we generated summary statistics of median well measurements (S1 Table). With these summarized data, we 178 investigated the relationship between feeding behavior and developmental stage. It is well established that 179 180 temporary suspensions of C. elegans feeding occur during each molt (Byerly et al., 1976; Cassada and Russell, 1975). As such, active feeding is frequently used to distinguish growing animals from individuals in a 181 molt. We quantified feeding behavior by exposing animals to fluorescent beads the approximate size of 182 bacteria and measuring fluorescence of animals (Nika et al., 2016). Because larger animals are able to 183 184 consume more food and therefore contain more ingested food, we normalized fluorescence by animal area to account for increases in body size (S4 Fig). The resulting fluorescence data showed a dynamic pattern (Fig 185 3A). At approximately 15 hours, fluorescence steadily increased to a peak before decreasing back to initial 186 levels at approximately hour 27. This pattern, repeated three additional times, established clear time windows 187 188 of local minimal fluorescence. These local minima represent periods of time where a large proportion of the

189 population had reduced or ceased feeding and therefore suggests time windows where a majority of animals 190 were likely not feeding because they were in a molt. We used a local kernel regression method to estimate a smooth curve and calculate the derivative to identify the time associated with each local minimum (see 191 Methods). We then assessed images collected from the growth assay and demonstrated that periods of 192 decreased feeding are concurrent with the presence of shed cuticles, supporting that animals are undergoing a 193 molt during these periods of time (S5 Fig). When we overlaid the timing of each local minimum on the 194 195 population size data, we were able to outline the start and end of each larval stage (Fig 3B-D). Notably, local minima occurred approximately every ten hours, consistent with well established observations of molt timing 196 (Byerly et al., 1976). Furthermore, we observed a clear relationship between changes in feeding behavior and 197 198 growth dynamics where decreases in feeding occurred simultaneously with discontinuous growth in length, 199 width, and volume.



200 Fig 3. Fluorescence dynamics outline larval stages.

(A) Median normalized red fluorescence (y-axis) over time (x-axis) is shown. The blue line represents the
kernel regression fit to the data. The red vertical lines correspond to the local minima of the regression and
represent the transition between larval stages. Median length (B), median width (C), and median log volume
(D) are shown with larval-stage transitions as well. Upper and lower bounds of the box plots correspond to the
first and third quartiles. The upper and lower whiskers extend to 1.5 times the value of the interquartile range.

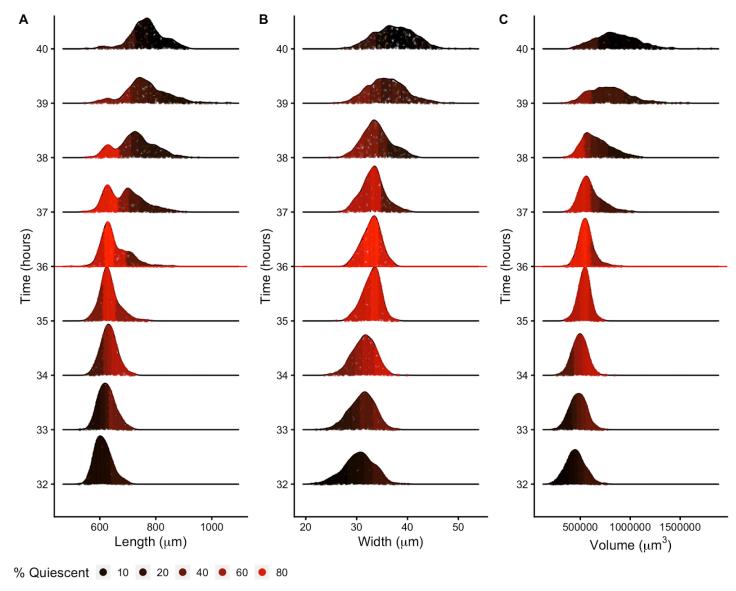
206 Changes in C. elegans body shape occur at larval-stage transitions

Adult body size is ultimately determined by the coordination of developmental progression and rate of growth. 207 To understand how C. elegans achieve final size, we must first examine how C. elegans grow. Quantitative 208 studies of C. elegans growth frequently assess changes in length or volume over time; however, to fully 209 characterize changes associated with growth, it is also important to consider the dynamics of width. Two 210 general models were proposed for *C. elegans* growth in volume: linear and exponential (Byerly et al., 1976; 211 Knight et al., 2002; Uppaluri and Brangwynne, 2015). Notably, these volume growth models require different 212 dynamics in length and width. To achieve linear volume growth, length and width must increase at precise 213 sublinear rates that together result in a linear increase in volume. If animal length and width increased at a 214 constant linear rate, then volume would increase at a cubic rate. Alternatively, if both length and width grew 215 exponentially, then volume would fit an exponential model. We sought to identify which model best described 216 C. elegans growth behavior but were unable to consistently distinguish between linear, exponential, and cubic 217 models using statistical information criterion because of the similarity in the shapes of the growth curves (S6 218 Fig and S2 Table). This result is not surprising because computational simulations have shown that increases 219 in experimental noise, above 2% added noise, limit the correct identification of growth models (Vuaridel-Thurre 220 et al., 2020). 221

222 Growth has important implications for how animals regulate size. Size homeostasis requires that growth rate 223 and developmental rate are coordinated. *C. elegans* reach a similar volume at each larval transition despite 224 significant variation in individual growth rates (Uppaluri and Brangwynne, 2015). Because individuals in a 225 population maintain similar sizes despite differences in growth rate, a control mechanism to regulate 226 developmental progression must exist. Early work proposed a size-based growth control model in *C. elegans*

227 (Uppaluri and Brangwynne, 2015), while recent work suggests that size homeostasis is achieved through a folder mechanism where growth rate and development are coupled (Towbin and Grosshans, 2021). To assess 228 changes in body size and shape during a larval transition, we examined the dynamics of animal length, width, 229 and volume in the hours before, during, and after each molt. We find that for each shape variable, larger 230 animals enter molt first (Fig 4). We also observe differences in the distributions of lengths during a larval 231 transition compared to widths and volumes. Measurements of animal width and volume remain unimodal 232 throughout a molt, but length does not. As larger animals begin to exit the molt, an increase in body length 233 occurs that leads to the appearance of bimodality of lengths across the population. This length increase occurs 234 simultaneously with a decrease in widths across the population. Importantly, volume remains constant while 235 length increases and width decreases, indicating a change in body geometry not size (Fig 3 and Fig 4). These 236 changes in the physical dimensions at each larval transition suggests that body shape, in addition to size, is 237 involved in the control of *C. elegans* growth. 238

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239 Fig 4. Density plots of population size dynamics during a single larval transition.

Population density curves of length (A), width (B) and volume (C) for the hours surrounding the L3 - L4 larval transition (red horizontal line at 36 hours corresponds to the molt). Each distribution was divided into five quantiles. The percentage of quiescent animals present within each quantile was calculated (see Methods), and each quantile was colored to reflect this percentage. In all shape variables, quantiles that contain the largest animals displayed an increase in quiescence earlier than quantiles that contain the smallest animals. These dynamics were consistent across all larval-stage transitions (S7 Fig).

246 Measurements of body shape suggest that cuticle stretch determines the timing of

247 larval-stage transitions

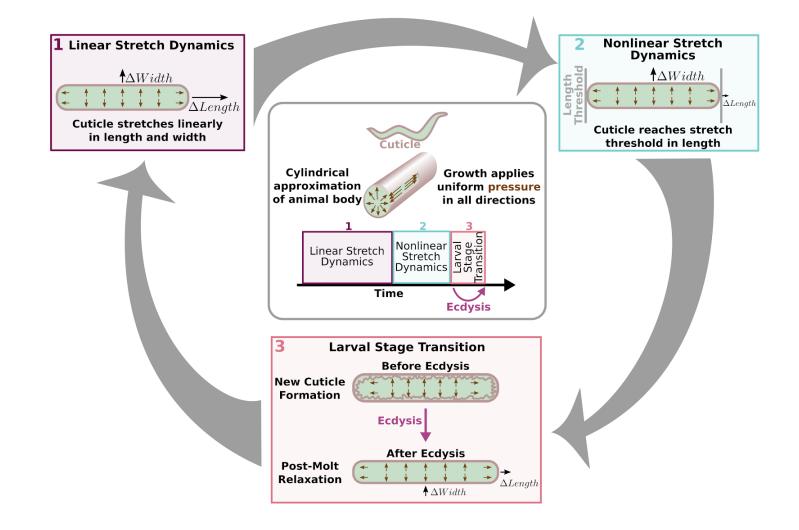
248 Previous studies theorized that the internal mechanism for sensing body size and triggering molts in *C.* 249 *elegans* is driven, in part, by the properties of the collagen-rich cuticle (Towbin and Grosshans, 2021; Uppaluri

250 and Brangwynne, 2015). Many cuticle collagen mutations cause morphological defects in nematode shape some of which cause animals to be shorter but do not impact animal width, implying that the cuticle affects 251 length and width independently (Brenner, 1974). The C. elegans cuticle does not grow through the addition of 252 new material, but rather stretches to accommodate increases in animal body size. Cuticle stretch is likely 253 mited by the material properties of the cuticle. The C. elegans cuticle is primarily made of cross-linked 254 collagens organized into lateral ridges and circumferential bands (Page and Johnstone, 2007b). Commonly 255 found in many biological systems, collagen-based materials are fairly flexible under low stress conditions. 256 However, as stress increases, collagen fibrils may become elongated and orient in the load bearing direction 257 leading to a decrease in elasticity (Holzapfel, 2017). Previous work using atomic force microscopy revealed a 258 high level of biomechanical stiffness at the circumferential bands (Essmann et al., 2017), leading others to 259 speculate that mechanical strain on these structures is likely adjusted as internal body pressure changes 260 (Dodd et al., 2018). Additionally, in nekl-3(sv3) molting mutants, the cuticle is not properly removed from the 261 middle part of their body, leaving the free head and tail to grow normally while the encased middle is 262 constricted by the old cuticle to pre-molt dimensions (Yochem et al., 2015). Given this body restriction, we 263 264 speculate that the old cuticle stretches beyond its tolerance, becomes stiff, and constricts the center of the nematode relative to the growing head and tail size. We hypothesize that C. elegans sense when the cuticle 265 becomes restrictive and use a threshold in the reduction of elasticity or "stretchiness" of the cuticle to 266 determine when to initiate a molt. 267

To explain the initialization of molt behavior, we developed a "Stretcher" model for a cuticle-stretch-based threshold that triggers *C. elegans* larval-stage transitions. We propose that the nematode passes through three distinct regimes related to cuticle stretch: linear stretch dynamics, non-linear stretch dynamics, and larval stage transition (Fig 5). The cuticle structure is anisotropic, possibly leading to distinct properties in the length and width directions (Cox et al., 1981; Petzold et al., 2011). We approximated the cuticle as a hollow cylinder of negligible thickness filled by the body of the nematode. Growth was modelled as internal pressure evenly

16

- 274 applied to the cuticle in all directions. We hypothesized that the cuticle responds differently during linear
- 275 stretch, nonlinear stretch, and post-molt relaxation.



276 Fig 5. Cuticle stretch determines larval-stage transitions

The "Stretcher" model describes each larval stage as a cycle. Nematodes are modeled as a cylindrical object with a thin cuticle epidermis. (Box 1) Linear Stretch Dynamics: uniform growth pressure stretches the cuticle linearly in both length and width. (Box 2) Nonlinear Stretch Dynamics: the cuticle has reached a stretch threshold in length, and under uniform growth pressure the length stretches less (sub-linear) and width stretches linearly. (Box 3) Larval Stage Transition: a new cuticle is formed and the old cuticle is shed (ecdysis), removing constraints in length. The nematode body "relaxes" in length, causing an increase in length, a decrease in width, and constant volume.

284 In the linear stretch regime (Fig 5), the cuticle would be linearly elastic in both the length and width directions,

285 stretching proportionally to the pressure exerted on the cuticle. Previous work found evidence for a linearly

elastic cuticle (Gilpin et al., 2015; Park et al., 2007) in animals expanded in a negative external pressure environment or after positive force was applied to the cuticle. Gilpin *et al.* have found evidence of linear elasticity in the nematode body. We conjecture that this linear elasticity is caused by the constraints applied by the cuticle ((Gilpin et al., 2015; Park et al., 2007). A linearly elastic cuticle will have ΔL stretch in the length direction and ΔW stretch in the width direction. each related to growth-applied pressure Δp by

$$\Delta L = a_L \Delta p \tag{1}$$

291

$$\Delta W = a_W \Delta p \,. \tag{2}$$

The "stretch coefficients" in length, a_L , and width, a_W , measure the stiffness of the cuticle (S5 File, Eq. S14-S23). Smaller values correspond to a stiffer material, which is less able to stretch in response to pressure. The stretch coefficients are constant in the linearly elastic regime and are determined by geometric constants and material properties. The ratio of the change in length (Eq. 1) and width (Eq. 2) produces a pressure-independent relationship that depends only on the ratio of the geometric and material properties, which can be verified using measurements of length and width (Fig. 3). During the linearly elastic regime, the ratio of growth in width to growth in length is constant throughout a larval stage where the cuticle properties are fixed as in

$$\frac{\Delta W}{\Delta L} = \frac{a_W}{a_L} = constant.$$
(3)

In the non-linear stretch regime (Fig 5), growth continues to apply pressure to the cuticle uniformly in all directions. As observed in *nekl-3(sv3)* mutants, the cuticle can restrict body growth (Yochem et al., 2015). Once outside of the linearly elastic regime, the cuticle would hardly stretch, even under large forces. We hypothesized that this shift from linear to nonlinear regimes provides a mechanism for size-sensing and cues the larval-stage transition (Fig 5). In principle, this transition could occur in either the width or length directions.

308 maintains linear stretch in the width direction. In the nonlinear regime, the stretch in the length direction in 309 response to pressure becomes

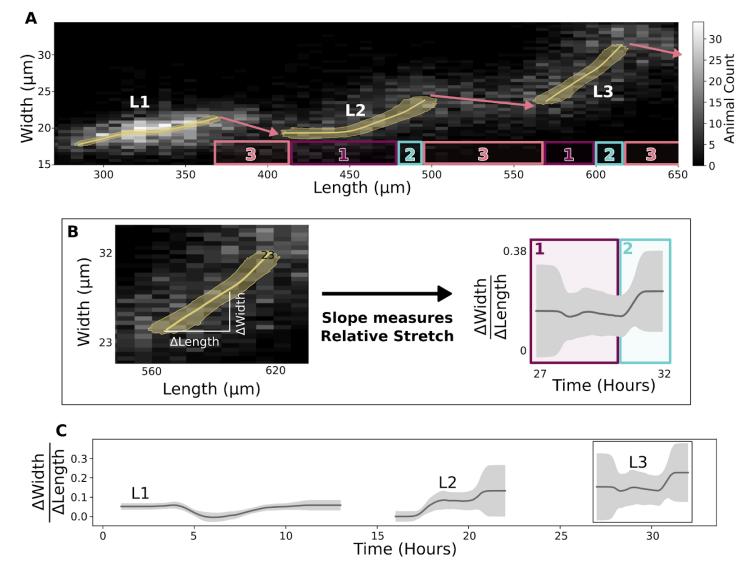
$$\Delta L \approx \tilde{a}_L(p) \,\Delta p. \tag{4}$$

The nonlinear "stretch coefficient," $\tilde{a}_L(p)$, is no longer constant and decreases with increasing pressure. It is smaller than a_L because the cuticle has become less elastic than in the linear regime. If the length-direction enters the nonlinear regime and has reduced stretch response, while width has the same constant stretch response then, we expect the $\frac{\Delta W}{\Delta L}$ ratio to increase

315
$$\frac{\Delta W}{\Delta L}|_{non-linear} = \frac{a_W}{\tilde{a}_L(p)} > \frac{a_W}{a_L} = \frac{\Delta W}{\Delta L}|_{linear}.$$
 (5)

During the larval-stage transition (Fig 5), a new, larger cuticle is formed beneath the old cuticle that is shed during ecdysis. Because the old cuticle constrained growth in length, we predict a rapid increase in the length direction when the constraint is removed. Nematode volume is conserved as growth does not occur during this process. Therefore, the relaxation in length is accompanied by a corresponding decrease in width.

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320 Fig 6. Stretcher model analysis of replicate 2 COPAS BIOSORT data consistent with a length trigger for 321 molting

(A) A grayscale histogram of the width (y-axis) vs length (x-axis) of all sampled animals in replicate 2. The range of all bootstrap regressions is in gold. (B) Demonstration of calculating the ratio of width-to-length stretch as the local slope using L3. Left panel is a repetition of L3 data from Fig 6A. Right panel is a repetition of results from Fig 6C. (C) Within a larval stage, the ratio of width to length stretch varies over time. The standard deviation captures population variation (grey) (S5 File, Eq. S26, S28).

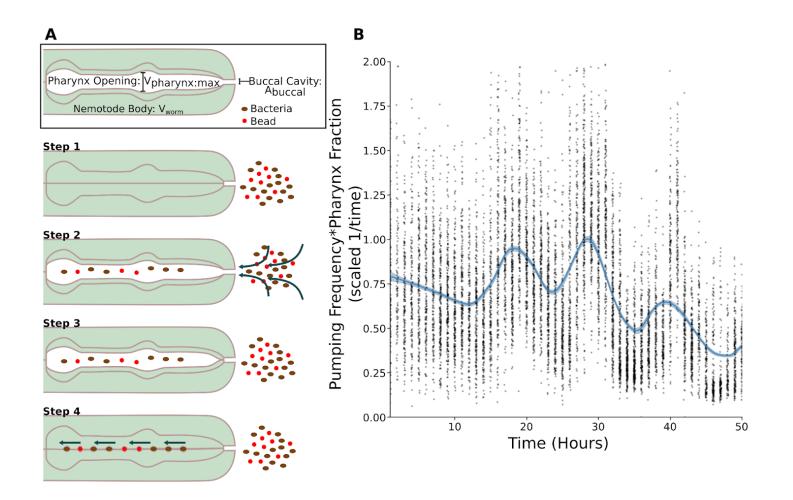
To verify the shape dynamics predicted by the Stretcher model, we analyzed the relationship between nematode length and width over developmental time. All three regimes, linear stretch, non-linear stretch, and relaxation, predicted by the Stretcher model are detectable in the COPAS BIOSORT data (Fig 6). In all larval stages, the instantaneous ratio $\frac{\Delta W}{\Delta L}$ was approximately constant for the majority of the time, consistent with a linear stretch regime (Fig 6C). We observed a large slope decrease during the L1 stage, which could

332 correspond in time to the metabolic decision for entry into the dauer stage (Golden and Riddle, 1984) or divisions of the seam cells (Sulston and Horvitz, 1977). Near the end of L2 and L3 stages, we observed a 333 sharp slope increase, supporting our predictions of a non-linear stretch regime in length prior to lethargus. 334 Slope transitions are difficult to detect at all larval stages due to noise amplification present in slope 335 calculations and population effects, making the larval stage boundaries difficult to define in a consistent 336 manner. We note that the transitions between larval stages contain the expected increase in length and a 337 decrease in width (Fig 6A and S8 Fig) consistent with a length threshold in the Stretcher model. Though the 338 shape relaxation for an individual animal is expected to happen at a much shorter time scale than data 339 collection (seconds to minutes), the measured shape change within the population occurs on a larger time 340 scale of several hours. As different individuals reach the transition points at different times, the shape change 341 is smoothed out and difficult to observe in the time-course data (Fig 3). However, we were able to more readily 342 observe the sudden shape change at transitions by looking at the width and length because animals of similar 343 shape are grouped together, regardless of the time they were observed (Fig 6A). These results suggest that 344 the material properties of the cuticle could generate a mechanical signal for the start of larval transition. 345 Additionally, sensing when the cuticle reaches a critical stiffness would allow the animal to detect when a 346 certain fold change occurs. 347

348 Mechanical control of feeding and allocation of food energy likely constrain growth dynamics

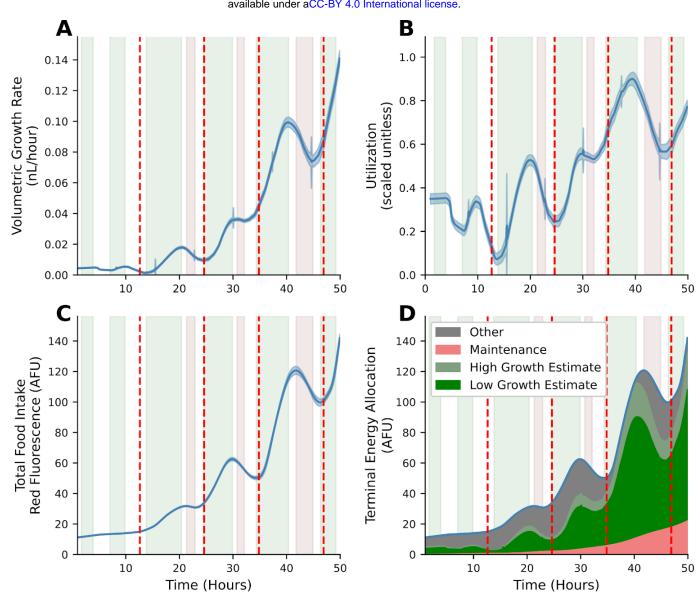
We have shown that changes in physical properties of the *C. elegans* cuticle precede the decision to initiate molt and might serve as a cue for developmental timing. *C. elegans* must have mechanisms to control growth throughout development, particularly in response to these cues. Like most species, *C. elegans* do not increase their growth rate indefinitely in response to increased food availability (Uppaluri and Brangwynne, 2015). The animals could control growth entirely using feeding rate, as they actively control the feeding rate (Fang-Yen et al., 2009) and stop feeding at the initiation of a molt (Singh and Sulston, 1978). In addition to this mechanical control, they could use metabolic control to preemptively divert ingested resources toward or away from growth. Metabolic processing of stored resources could be especially useful if animals complete their molt and

357 enter a food-limited environment. For these reasons, we investigated the possible mechanical control of 358 feeding (Fig 7) and the metabolic control of the allocation of ingested food toward organismal growth and 359 development (Fig 8). Using a quantitative feeding model, we calculated the rate of mechanical feeding 360 behavior from animal volume and food intake data. Additionally, we calculated an estimate for allocation of 361 ingested food toward volumetric growth.



362 Fig 7. Visualization and analysis of Feeding Model

363 Schematics for food intake and utilization models are shown. (A) The buccal cavity is the opening through 364 which food enters. The pharyngeal lumen is the cavity opened and closed by pharyngeal muscles that drives 365 food intake. (B) Product of pumping frequency and pharyngeal lumen fraction, f(t)g(t).



366 Fig 8. Visualization and analysis of Food Utilization model.

(A) Dynamics of volume growth rate. (B) Dynamics of the estimated food utilization towards growth ($\alpha(t)$). (C) 367 Dynamics of red fluorescence. (D) Dynamics of food allocation breakdown. Food allocated toward 368 maintenance is proportional to animal size (pink). Food allocated toward growth is calculated from food intake 369 (B) and utilization (C) to produce low (dark green) and high (combined green) estimates (S5 File). Food 370 allocated to other metabolic processes consists of remaining food resources (grey). In panels A-C, the solid 371 blue line represents the mean bootstrap regression. Standard deviation on the regression is marked by the 372 shaded blue region. In panels A-D, Vertical red lines mark molt times. Green regions correspond to times 373 during which volumetric growth rate and red fluorescence are both increasing, red regions correspond to times 374 375 during which volumetric growth rate and red fluorescence are both decreasing, and white regions correspond 376 to times during which volumetric growth rate and red fluorescence do not vary together. Errors on shaded regions are ± 0.7 hours. These data are from replicate 2 and are representative of all replicates (S11 Fig). 377

378 Variation in pumping rate controls food uptake

C. elegans is a filter feeder that pumps its food through a cycle of pharyngeal muscle contractions and relaxations that alternatively open and close the pharyngeal cavity. *C. elegans* are capable of actively modulating the length of time used to contract or open a subset of the pharyngeal muscles (Fang-Yen et al., 2009). Our feeding model describes how control of this time length and thus the control of the overall pumping period, defined as the length of time of one full pumping cycle, translates to changes in the rate of food uptake.

384 A single cycle in which animals take up and transport food to the gut consists of four general steps (Fig 7A). The cycle begins with relaxed pharyngeal muscles and a closed pharyngeal lumen (step 1). The animal opens 385 the pharyngeal lumen so that fluid and food flow through the buccal cavity and into the pharyngeal lumen (step 386 2). The animal cannot create a vacuum, so the volume of the cavity produced must be filled entirely by media 387 and bacteria at the same concentration as the external environment. The animal relaxes the muscles that 388 control the opening, stopping the flow of fluid through the buccal cavity and trapping a volume of media 389 approximately equal to the maximum volume of the pharyngeal lumen (step 3). Finally, the pharynx closes, 390 extruding excess media and trapping bacteria and beads that are then 'swallowed' (step 4). The period of a 391 single cycle varies throughout the life cycle of *C. elegans* (Fang-Yen et al., 2009). 392

We find a relationship between eating rate and animal volume. It has previously been suggested that the cross-sectional area of the buccal cavity is a limiting factor in the rate of food intake (Knight et al., 2002). However, the volume of the pharyngeal lumen is filled with media each cycle, so the volume of the pharyngeal lumen, not the cross-sectional area, sets food uptake rate. We express the volume of the pharyngeal lumen as a fraction, g(t), of nematode volume, $V_{lumen:max}(t) = g(t) \cdot V_{worm}(t)$. As the pumping period is much faster (roughly 200 ms in adults) (Fang-Yen et al., 2009) than the rate of measured growth (hours), we averaged the food intake rate, $\frac{dV_{food}}{dt}$, over a single pumping period (S5 File, Eq. S1-S6) to obtain

400
$$\frac{dV_{food}}{dt} = Cf(t)g(t)V_{worm}.$$
 (6)

24

Here, *C* is the concentration of bacteria in the culture where animals are grown and f(t) is the pumping frequency and the inverse of the period of a single pump. Both pumping frequency, f(t), and the fractional pharyngeal lumen size, g(t), vary over the animal's life cycle. Though any individual bacterium may take multiple pumps to travel down to the gut, we assume that, once food has entered the pharyngeal lumen, it will eventually be metabolized. With this assumption, we are only interested in the rate at which food enters so we do not model the dynamics of food traveling through the gut.

We verify that red fluorescence (denoted as "*Red*") can be treated as a proxy measurement for food intake rate given defecation rates (S9 Fig, S5 File). We use red fluorescence and calculated volume as the product of pumping rate and pharyngeal lumen fraction, $f(t)g(t) \propto \frac{Red}{V_{worm}}$, over time. The product oscillated within a larval stage and decreased across larval stages (Fig 7B). The minima of the product of pumping frequency and pharyngeal lumen fraction occurred during molt times, consistent with prior knowledge (Byerly et al., 1976; Singh and Sulston, 1978). The relative length of the pharynx to animal length has been shown to decrease over development (Avery, 2003) and a similar trend in the volume of the pharyngeal lumen could explain the slow decrease in the product of pumping frequency and pharynx fraction.

415 Changes in food utilization coincide with molts

To understand whether animals control growth rate primarily using the mechanical feeding process or metabolic regulation, we describe how food is utilized once it is ingested by *C. elegans*. We assumed three general categories of food utilization: maintenance, observed volumetric growth, and all other processes. We assume that resources required for maintenance are proportional to the volume of the animal. Other processes may include the development of tissues and structures, such as reproductive components, within the worm which are resource intensive, but are not detected during the measurements of the width, length, or volume. The rate of food conversion to growth can be described by:

(7)

423
$$\frac{dV_{worm}}{dt}(t) = \eta(t)\alpha(t)\frac{dV_{food}}{dt}(t).$$

424 Here, $\frac{dV_{food}}{dt}$ is the instantaneous rate of food intake (averaged over a single pump), $\eta(t)$ is the metabolic 425 efficiency of converting food to growth, and $\alpha(t)$ is food utilization, meaning the fraction of food used for volumetric growth as opposed to maintenance or other metabolic processes. If both n(t) and $\alpha(t)$ are constant. 426 then Eq. (4) predicts the rate of volumetric growth is directly proportional to the rate of food consumption, which 427 would be equivalent to controlling growth through feeding with no changes in metabolic regulation (through 428 enzyme expression or other direction of flux between pathways). Efficiency captures the maximum efficiency of 429 metabolism, and we assume it does not vary significantly when the food source is constant, $\eta(t) = \eta$. 430 Therefore, utilization captures the dynamics of metabolic regulation. If the fraction of food utilized for growth is 431 not constant, then volumetric growth rate is no longer proportional to food consumption rate and metabolic 432 control must play a role in driving the growth rate. 433

434 We calculate the value of the product of metabolic efficiency and food utilization, $\alpha(t) \eta$, from the data by 435 manipulating Eq. (7):

$$\alpha(t) \eta = \left(\frac{dV_{worm}}{dt}(t)\right) / \left(\frac{dV_{food}}{dt}(t)\right).$$
(8)

436

437 By using the red fluorescence as a proxy for food intake rate in Eq. (8), we can estimate the dynamical 438 behavior up to scaling factors for the metabolic efficiency times food utilization, $\alpha(t) \eta \propto \left(\frac{dV_{warm}}{dt}(t)\right) / Red$ (Fig 439 8B). Because only utilization varies in time, it captures the dynamics of metabolic regulation:

440
$$\alpha(t) \propto \left(\frac{dV_{worm}}{dt}(t)\right) / Red.$$
 (9)

Feeding rate (using red fluorescence as a proxy) and volume growth rate (numerically differentiated from the volume regression) follow similar dynamics throughout much of *C. elegans* development (Fig 8A, Fig 8C). The regressions for volume growth rate and food intake rate (as measured through red fluorescence) demonstrate a greater than 90% correlation when using synchronized populations (through the end of L4). Each larval stage

445 consists of three types of dynamics: steady growth during which food intake and growth rate are both increasing (green), preparation for molt during which food intake and growth rate are both decreasing (red), 446 and transition regions where food intake and growth rate do not vary together (white). To illustrate how the 447 dynamics of food intake rate and growth rate (Fig. 8A, 8C) correspond to the progression within a larval stage, 448 consider the L3 larvae in replicate 2. At hour 24.5, both growth rate and food intake rate increased 449 corresponding to the start of the third larval stage for the population average. Until hour 29.8, the population 450 grew steadily, and food intake and growth rate both increased (green). Between hour 29.8 and 30.8 (white). 451 food intake decreased and growth rate increased, marking a transition from the steady growth (green) to the 452 molt preparation regime (red). Between hours 30.8 and 32.1, the animals prepared to initiate molts, and both 453 the growth rate and food intake rate decreased (red). Between hours 32.1 and 34.4 (white), the animals' 454 growth rate increased once again while the food intake rate continued to decrease corresponding to the end of 455 the molt and start of the L4 larval stage. Similar dynamics occurred in the L2 and L3 larval stages. The L1 456 larval stage followed different dynamics, likely due to the dauer decision or divisions of the seam cells. 457

During steady growth (green) and molt initiation (red), mechanical food intake rate and allocation of food 458 resources towards observable growth have similar dynamics. At transition points (white) the allocation of food 459 resources towards growth, $\alpha(t)$, reaches a local minimum or maximum (Fig 8B). These local extrema in $\alpha(t)$) 460 at transition points likely indicate large changes in metabolic regulation. One might expect growth rate to lag 461 462 food intake, but time-lag analysis showed no consistent lag across L1 to L4. During the L1 and L2 stages, volume growth rate lagged behind food intake rate (with correlation ~86%); during the L3 and L4 stages, food 463 intake rate lagged behind growth rate (with correlation ~94%) (S14 Fig). The switch to food intake lagging 464 growth rate at later larval stages might be indicative of increased regulation of resource allocation. 465

466 One might assume that the high correlation (S15 Fig) between dynamics of growth (Fig. 8A) and food intake 467 (Fig. 8C) imply that animals control their growth rate entirely through the control of mechanical food intake rate 468 with no variation in how food resources are allocated. Instead we saw variation in food allocated toward

growth, $\alpha(t)$, both between larval stages and within individual larval stages. We examined the dynamic range 469 470 of total food intake (Fig. 8C) and the dynamic range of food allocated toward growth (combined green Fig. 8D) to quantify whether control through food intake or control through metabolic regulation play a larger role in 471 growth regulation. Across a larval stage, both methods of regulation had dynamic ranges of the same order of 472 magnitude. We also calculated the dynamic range within each period of steady growth (green), molt initiation 473 (red), and transition (white) (Fig. 8). Within each region, the dynamic range of food intake and food allocated 474 toward growth differed by a factor of 0.5 to 5, but we found no noticeable trends by region (S3 Table). It is 475 possible that the interpolation and smoothing required to calculate derivatives necessary to this analysis are 476 masking some sharper transitions, which could be resolved with higher resolution temporal experiments. 477 These results suggested that both the total intake rate (governed by mechanical feeding behavior) and 478 metabolic regulation of food resources are crucial for growth control in all regions of development. Additionally, 479 we compared the food allocated toward other metabolic processes with food allocated toward growth over the 480 four larval stages. Using the low growth utilization estimate, food allocated toward growth increases with an 481 approximately 86-fold increase while the other resource allocation increases with an approximately six-fold 482 increase. Resource requirements for other metabolic processes such as development of new tissues and 483 animal mobility might vary much less during development than the resource requirements for volumetric 484 growth. 485

Feeding rate and volumetric growth rate share a complex relationship with *C. elegans* development; food intake and growth rate vary together, except at larval stage transitions and possible key developmental transitions. Notably, the changes in metabolic resource allocation at the transition from increasing to decreasing growth and food intake rates (Fig 8A, 8C) occurred at approximately the same times as the increase in slope predicted as a cue for molt initiation by the Stretcher model (Fig 6). This correlation suggests that the cuticle reaches its maximum stretch in length and a metabolic decision to reallocate food resources growth occurs at the same time, supporting the hypothesis that a physical threshold in stretch triggers metabolic decisions to enter a molt (S10 Fig).

28

494 Discussion

Using an integrated image-based and flow-based phenotyping strategy to precisely evaluate feeding, growth, 495 and molt dynamics at high replication, we detected oscillations in feeding behavior consistent with larval 496 progressions and used these dynamics to define larval stages. We observed changes in body shape at each 497 larval-stage transition that are consistent with differences in physical cuticle properties along length or width 498 (anisotropy). These results suggest that animals sense their size and control molt timing by detecting the 499 physical stretch of the cuticle. To understand whether C. elegans control growth using the moderation of the 500 physical uptake of nutrients or through metabolic regulation of the allocation of consumed resources, we 501 applied mathematical models of feeding-limited growth to our data. We predicted that the volumetric growth 502 rate was controlled by both C. elegans feeding rate and other metabolic regulation and provided a modeling 503 framework to decouple the relative effects. These results demonstrate two mechanisms by which physical 504 constraints can influence developmental timing and growth rate. 505

506 Cuticle stretch controls the timing of larval-stage transitions

Measurement of both animal length and width allowed us to observe changes in body shape as well as body 507 size. We propose that a stretch threshold along the body length axis acts as a trigger to larval-stage 508 transitions. Importantly, mechanical stretch sensing could also provide organisms a way to couple the rate of 509 growth and development to maintain a constant volume fold change within a larval stage and achieve size 510 homeostasis within a population. In this way, smaller animals would reach a stretch limit at a smaller size as 511 the cuticle would only stretch a percentage of its original size before reaching a threshold. A folder mechanism 512 for C. elegans growth has been previously suggested (Towbin and Grosshans, 2021). For cuticle stretch to 513 trigger larval-stage transitions, animals must either have the ability to measure the amount the cuticle has 514 stretched or the stiffness of the cuticle. Across biological systems, cells can respond to the stiffness of their 515 environment using mechanosensitive components (Schiller and Fässler, 2013; Wolfenson et al., 2011), but few 516 examples in tissues or whole-organisms are known. In C. elegans, it has been demonstrated that 517

518 hemidesmosomes, which connect the cuticle and the epidermis, are mechanosensitive during embryogenesis (Suman et al., 2019; Zhang et al., 2011). Additionally, dense bodies, which connect the epidermis and muscles, 519 are hypothesized to be mechanosensitive as well (Broday et al., 2007; Costa et al., 1997; Moerman and 520 Williams, 2006; Zaidel-Bar et al., 2010). Changes in cuticle composition, and presumably stiffness, have been 521 shown to also affect well known growth controlling pathways such as the BMP signaling pathway (Madaan et 522 al., 2020). These possible mechanosensitive components could monitor the stiffness of the cuticle and be part 523 of the signaling pathways that regulate larval-stage transitions. Further experiments are required to explicitly 524 test whether these components control larval-stage transitions. 525

526 Our analysis of width-to-length ratio variation over larval stages provides a first approximation of the timing of larval-stage transition cues and cuticle stretch properties (Fig 8). The sudden increase we observed in the 527 width-to-length ratio suggests a length stretch threshold. Interestingly, when observing the L4 to adult 528 ansition, others have detected anisotropic constriction on the transverse (width) axis followed by gradual 529 relaxation driven by rearrangements in cortical actin networks (Katz et al., 2018). Single-worm, high frequency 530 measurements targeting hours surrounding the sudden width-to-length ratio increase, are needed to better 531 resolve cuticle shape dynamics. Higher time resolution would also minimize edge effects (S12 Fig), which likely 532 caused the unpredicted width-to-length ratio increase observed at the start of larval stage L2 (Fig 8C). 533 Measurements of animal length and width provide a total stiffness estimate but do not allow us to distinguish 534 the contributions of cuticle stiffness from other tissues. To investigate cuticle properties, independent of other 535 nematode tissues and organs, experiments must probe the stiffness of free cuticles. 536

537 Physical constraints on feeding influence growth dynamics

538 Our mechanical feeding model defines a relationship between food availability, food intake rate, food utilization, 539 and growth rate. We distinguished between food intake rate and pumping rates by modeling the physical 540 process of feeding. The results of our analysis are consistent with both an oscillation in pumping rates (Singh 541 and Sulston, 1978) and a slow change in pharyngeal lumen size throughout development (Avery, 2003).

Previous research suggested that pumping frequencies within a larval stage are constant with sudden transitions between lethargus and pumping (Nika et al., 2016). However, we were unable to resolve sudden transitions because of the continuous smoothing of the kernel regression method used and population effects (Fig 7B). Previous work has shown that growth rate increases with increasing food availability up to a saturation limit (Uppaluri and Brangwynne, 2015). Varying bacterial concentration levels in future experiments would allow us to distinguish whether mechanical control of food intake or metabolic control of food utilization determine the upper bound on growth rate.

Our analysis of the relationship between growth rate and food intake rate quantified the interplay of metabolic 549 regulation and mechanical food intake. Mechanical food intake provides the upper bound of available food 550 551 resources for growth, but metabolic regulation substantially changes how much of this available food is utilized for volumetric growth across development. Local extrema in metabolic regulation dynamics coincide with the 552 start of transition times. Within the L2 and L3 stages we observed a decoupling between growth rate and food 553 intake dynamics (Fig. 8 white region) twice. The first of these time periods corresponds to the times at which 554 the width-to-length ratio drastically changes and the second corresponds to ecdysis (S10 Fig). We estimated 555 that throughout larval stages metabolic resources allocated to non-growth processes varies much less than 556 food resources required for growth and maintenance. The oscillatory behavior of food utilization motivates the 557 need for further metabolomic experiments to probe metabolic regulatory dynamics. Higher time resolution 558 experiments on single animals in future experiments may be able to better resolve the existence of sudden 559 changes in metabolic regulation. 560

In the analysis of both the Stretcher and feeding models, we found that the L1 larval stage has different dynamics than other larval stages. We observed a decrease in growth rate with no associated decrease in feeding rate, corresponding to a mid-stage resource reallocation, that does not occur in any other larval stage, possibly showing the dauer decision (Golden and Riddle, 1984) or the divisions of seam cells. Additionally, within the L1 stage, the relative stretch measured in width and length did not follow the pattern observed in

31

566 other larval stages. We observed a mid-stage dip in the width-to-length ratio that is otherwise approximately 567 constant throughout the L1 stage. As animals reallocate food resources in mid-L1, they also undergo a change 568 in shape suggesting either directed growth or structural changes to either the cuticle or animal body (Fig 3, Fig 569 6, S8 Fig). Future experiments exploring the structural properties of cuticles at all larval stages may help to 570 determine where the L1 shape changes originate.

571 Development comprises complex interactions of growth regulation across diverse scales

Our results demonstrate that C. elegans may use physical constraints on animal size and feeding rate to 572 control growth rate and determine developmental transitions. This type of regulation could be applicable to 573 574 organisms with stiff cuticles or other physical barriers to growth, like many species of Ecdysozoa. The control of whole-organism growth requires cells, tissues, and organs to orchestrate final size and cell number. In C. 575 elegans, cell number is precisely defined and invariant from animal to animal (Horvitz and Sulston, 1980), so 576 the final adult size of an individual must come from cell size as opposed to number. Future studies should 577 focus on how whole-organism size is determined by the integration of cell, tissue, and organ size. By 578 579 incorporating these different developmental scales, the Stretcher model can be refined to completely describe how physical constraints on parts of the organism impact the whole. C. elegans gives investigators a method to 580 investigate animal-to-animal variation in developmental trajectories across each of these scales. 581

582 Methods

583 Worm culture

The canonical laboratory strain N2 was obtained from the *C. elegans* Natural Diversity Resource (Cook et al., 2016). Animals were cultured at 20°C on 6 cm plates of modified nematode growth media (NGMA), which contained 1% agar and 0.7% agarose seeded with *E. coli* OP50 bacteria (Andersen et al., 2014).

587 Bacterial food

E. coli HB101 bacteria were prepared from cultures grown for 15 hours in Superbroth and then pelleted by centrifugation. HB101 bacteria were diluted to OD100 in K medium (51 mM NaCl, 32 mM KCl, 3 mM CaCl2, and 3 mM MgSO4 in distilled water) and stored at -80°C. Bacteria were thawed and fed to animals at a concentration sufficient to sustain population growth from hatching to adulthood (OD20).

592 Growth of the animals

Populations of animals were propagated on NGMA plates for two generations without starvation. In the third 593 generation, gravid adults were bleach-synchronized (Stiernagle, 2006). Embryos were resuspended in K 594 medium, aliguoted into a 500 mL flask at a concentration of one embryo per µL, and allowed to hatch 595 overnight. The following day, arrested L1s were fed HB101 bacteria at a final concentration of OD20 in a final 596 flask volume of 100 mL K medium and HB101 food. Animals were grown for three days at 20°C with constant 597 shaking. Following these three days, adult animals were bleach-synchronized once more and embryos were 598 aliguoted to seven replicate 500 mL flasks at a concentration of one embryo per μ L in 100 mL. The following 599 morning, six flasks were fed HB101 bacterial food at a final concentration of OD20 in a final flask volume of 600 100 mL K medium and HB101 food. Two additional flasks were included to control for L1 animal size and 601 possible clumping of bacterial food: one flask contained L1 larvae but did not have food added and one flask 602 603 contained no larvae but the same concentration of HB101 bacteria as the six flasks containing L1 larvae. All replicate flasks were kept in an incubator at 20°C with shaking for the duration of the experiment. A small 604 temperature gradient of 1.25°C was recorded in the shaking incubator with the highest temperature readings 605 on the right side and lowest temperature readings on the left side (S1 File). This slight variation in temperature 606 contributed to variation in developmental rate among replicates based on position within the incubator 607 (replicates were placed in numerical order with replicate 1 positioned on the far right side of the incubator). 608

609 High-throughput measurements of body size and fluorescence

610 Flasks were sampled each hour beginning one hour after feeding and continuing for 72 consecutive hours. At each hour, 500 µL was removed from each flask and transferred to a well of a deep 96-well plate. Each flask 611 was sampled at each time point. Fluorescent polychromatic beads (Polysciences, 19507-5) with a 0.5 µm 612 613 particle size were added to each well at a final concentration of 3.64x10⁸ beads/mL and incubated at 20°C for 10 minutes with shaking. Following the bead incubation, 30 µL from each well of the deep 96-well plate was 614 aliguoted to a 96-well microtiter plate. The process was repeated 11 times to 11 separate wells of the same 615 microtiter plate with pipetting to mix the well contents from the deep 96-well plate. Animals were then treated 616 with sodium azide at a final concentration of 50 mM to paralyze and prevent defecation of the ingested beads. 617 The 96-well plate was imaged with an ImageXpress Nano (Molecular Devices, SanJose, CA) using both 2x 618 (Nikon MRD00025) and 10x (Nikon MRH00101) objectives. The ImageXpress Nano acquires brightfield 619 images using a 4.7 megaPixel CMOS camera. Images are stored in 16-bit TIFF format. Finally, animals were 620 scored using a large-particle flow cytometer (COPAS BIOSORT, Union Biometrica, Holliston MA). The COPAS 621 BIOSORT sheath flow rate was kept at a constant 10.3 ±0.1 mL per minute to reduce variability in length 622 measurements. 623

624 Image processing

625 Manual measurements of animal size were performed using the free Java image-processing program ImageJ Abràmoff et al., 2004). Well images for the six replicate flasks, excluding controls were loaded into ImageJ 626 software. Length was measured from head to tail, and width was measured at the widest point of the animal. 627 Five animals were measured per well across thirty total wells for each hour. Measurements were repeated for 628 all 72 time points in the assay. Body length and width were used to estimate cross-sectional area 629 (length*width). This metric was used to describe animal area for the extent of the text. Volume was calculated 630 from body length and width by approximating the animal as a cylinder. Pixels were converted to µm using a 631 conversion factor of 3.2937 pixels/µm. 632

633 Data processing

The COPAS BIOSORT was used to collect measurements of animal length (TOF), optical extinction (EXT), and fluorescence for every animal in each well. These traits measure properties of nematode development and, as such, increase as animals progress to adulthood (Andersen et al., 2015). Optical extinction measurements correspond to the amount of light absorbed over the full length of an animal as it passes through the instrument. An additional measurement (norm.EXT) can be calculated by normalizing optical extinction by length. The raw data collected were imported and processed using the *easysorter* R package (Shimko and Andersen, 2014).

641 The COPAS BIOSORT data were analyzed further using Gaussian finite mixture modeling as implemented in the mclust R package (Scrucca et al., 2016). These probabilistic models assume that data are generated from 642 a mixture of multivariate normal distributions and, therefore, can be used to classify unstructured data into 643 meaningful groups. Specifically, the mclust package fits a mixture model to data and selects the optimal 644 number of clusters using an expectation-maximization algorithm and Bayes Information Criteria. For 645 646 model-based clustering, log transformed animal length (logTOF) and log transformed optical extinction 647 (logEXT) were used as inputs for the *Mclust* function. Data from each hour of the experiment was analyzed by 648 replicate and clusters that did not appear to include majority animal objects were identified and removed as described previously (Smith et al., 2009). This processing removed non-animal objects such as bacterial 649 clumps, shed cuticles, and next generation larval animals from the time-course data. 650

We used a numpy polyfit regression of well-median data from the COPAS BIOSORT and image measurements to convert TOF and norm.EXT data to microns (S5 File, Eq. S7-S9). Only the unit-corrected BIOSORT data were used for further analysis.

654 Molt analysis

655 Fluorescence data obtained from the COPAS BIOSORT was used as a proxy for feeding behavior to 656 distinguish animals in a molt from growing animals. First, fluorescence was normalized by EXT to account for the ability of larger animals to consume more food and beads. Next, an analysis of variance statistical model 657 was fit to the fluorescence data normalized by EXT to determine the amount of variance contributed by 658 replicate and well (Table S1). A local kernel regression smoothing method was then applied to the residuals of 659 the variance analysis using the lokern R package (Hermann, 2016). Residuals were used to address only the 660 differences over time and ignore minor variation among replicates and wells. The local minima of the 661 regression function were found by solving for where the first derivative of this function equaled zero. The time 662 associated with each local minimum was used to represent the timing of each molt. Molts occurred at 14, 25, 663 36, and 48 hours. 664

To identify periods of time that contained a majority of growing animals, the inflection points of the regression function were calculated by solving for where the second derivative of the function equaled zero. Time points between inflection points that did not contain a local fluorescence minimum were considered as growth periods. These hours were 1-13, 17-22, 27-32, and 39-45 corresponding to L1, L2, L3, and L4 growth periods.

Each molt is initiated when animals enter lethargus: a behavioral state where animals cease active feeding. To classify individual animals as in a molt or growing, we set a quiescence threshold using fluorescence measurements at each local minimum. The fluorescence measurement at each local minimum was as follows: 0.07, 0.06, 0.06, 0.06. The average of these measurements (0.06) was used as the fluorescence threshold signifying quiescent behavior. Any individual animals that fell below this threshold fluorescence value were designated as in a molt and animals above this threshold value were classified as growing.

36

675 Comparison of model fits

676 To determine the volume growth model, we fit linear, exponential, and cubic functions to data designated as 677 growth periods for each larval stage. Both linear and nonlinear functions were fitted using least-squares regression. Akaike's information criterion (AIC) (Sakamoto et al., 1986) and Bayesian information criterion 678 (BIC) (Schwarz, 1978) were goodness of fit criteria used to evaluate candidate models. To assess the strength 679 of evidence for each candidate model, we identified the model with the smallest AIC/BIC value and assessed 680 the difference between this value and the AIC/BIC of the other two models. The magnitude of the difference 681 was used to determine the level of support for each candidate model as previously described (Burnham and 682 Anderson, 2007; Kass and Raftery, 1995). All model fits and analysis were performed using the stats R 683 package. 684

685 Stretcher and feeding model analysis

To analyze shape dynamics, length and width data from growth time periods were extracted from the full 686 COPAS BIOSORT population data and analyzed from each replicate separately to avoid issues with replicate 687 variability. For replicate 2, the hours defining growth periods were 1-13, 16.37-22.39, and 26.93-32.96; 688 corresponding to L1, L2, and L3. Hours defining larval stages were rounded as data was collected at exact 689 hour increments. The L4 stage was excluded from the analysis because of the high variability within the 690 691 population. We applied a local kernel regression, lokern R package ("Lokern: Kernel regression smoothing with local or global plug-in bandwidth," n.d.), to smooth the population dynamics of length and width. To calculate 692 mean and standard deviation, the smoothed population measurements were bootstrapped using 2.000 693 samples with replacement (S5 File, Algorithm S1). To determine cuticle properties throughout larval stages, we 694 calculated the mean ratio of derivatives of regression width and length. Error for this ratio was calculated using 695 error propagation to pass the bootstrap variation through the ratio (S5 File, Eq. S24-28). 696

697 To analyze volumetric growth dynamics and feeding dynamics, volume regression was calculated using a 698 cylindrical approximation for animal shape (S5 File, Eq. S7-S9) and the same local kernel regression

- 699 previously described was applied to red fluorescence data. Volume growth rate was calculated using the
- 700 python numpy gradient function applied to the volume regressions. An additional moving time window average
- 701 (1.4 hours) was applied to smooth numerical errors in the derivative when determining feeding and growth
- 702 regime transition points (S13 Fig).

703 References

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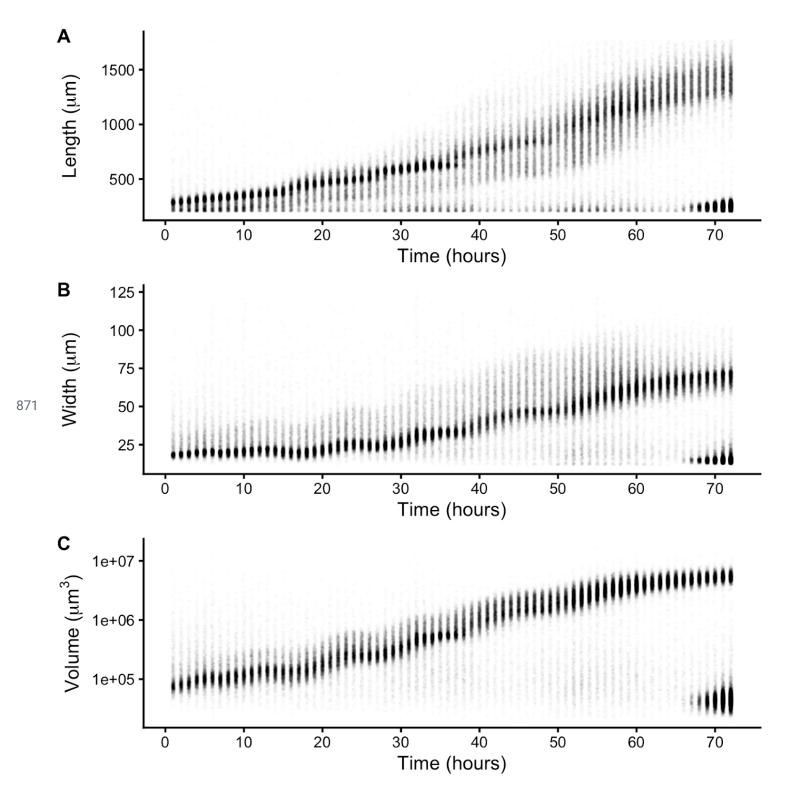
851 Data availability

The authors state that all data necessary to confirm the conclusions of this work are within the text, figures, and supporting information files. All files and code for analysis and generation of figures and tables are archived on GitHub (<u>https://github.com/AndersenLab/C.elegans-growth-manuscript</u>).

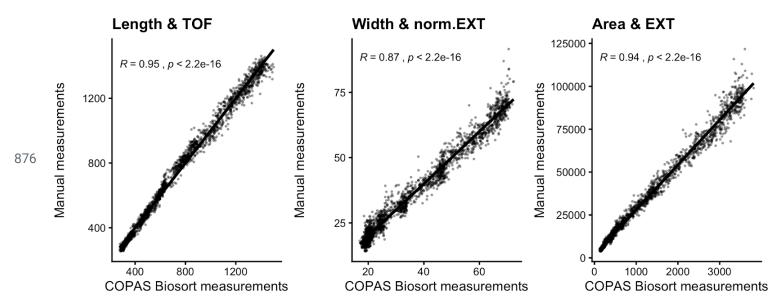
855 Acknowledgements

856 E.C.A and N.M.M conceived the project. J.N., G.Z., and E.C.A designed, optimized, and performed the experiments. J.N., H.N.A, E.J.A, I.R.M, J.K.R, I.L.S., and J.A.V. collected manual size measurements of 857 animals from images. J.N. processed the COPAS BIOSORT data to remove non-animal objects. J.N, C.G., and 858 S.S. analyzed the results. C.G. and S.S. developed the theory and tested the models. E.C.A and N.M.M 859 supervised the research and the development of the manuscript. J.N, C.G, and S.S. wrote the first draft of the 860 manuscript; J.N., C.G., G.Z, N.M.M, E.C.A., and S.S. edited the manuscript. We thank Jiping Wang and Keren 861 862 Li for helpful advice about statistical data analysis. We would like to thank members of the Andersen laboratory and the Mangan group for their helpful comments on the manuscript. For this work, J.N., C.G., G.Z., E.C.A., 863 N.M.M. and S.S. received support from the NSF-Simons Center for Quantitative Biology at Northwestern 864 865 University (awards Simons Foundation/SFARI 597491-RWC and the National Science Foundation 1764421). C.G., S.S., and N.M.M. received support from the National Science Foundation RTG: Interdisciplinary Training 866 in Quantitative Biological Modeling, award 1547394). C.G. was supported in part by the Murphy Scholars 867 Program of the Robert R. McCormick School of Engineering and Applied Science at Northwestern University. 868 869 **Competing interests:** The authors have no competing interests.

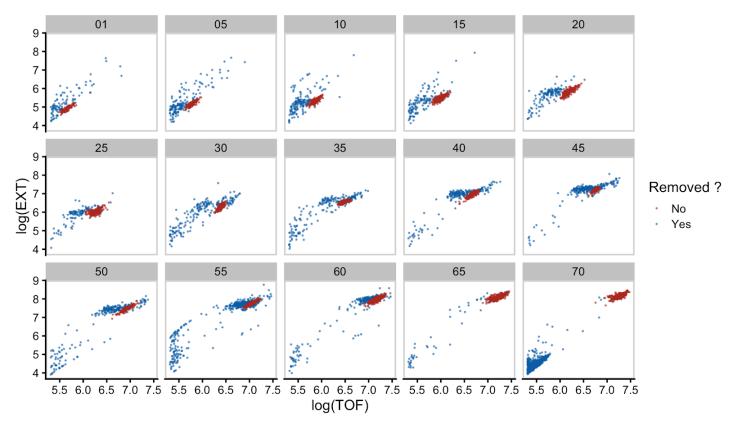
870 Supporting Information Captions



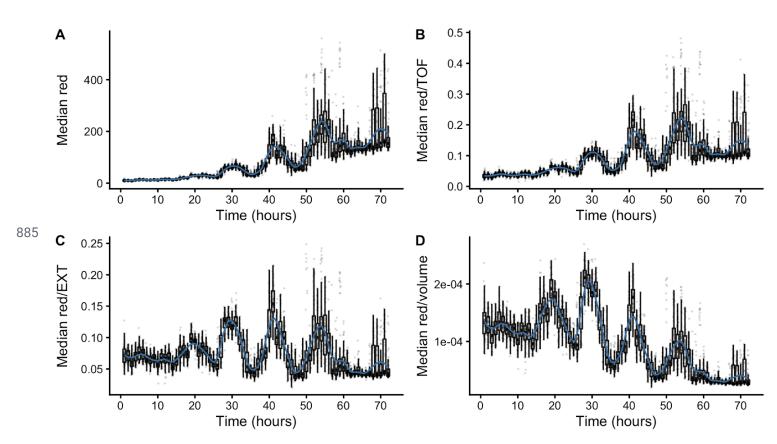
S1 Fig. Raw measurements of animal size. Raw COPAS BIOSORT data of animal length (A), width (B), and volume (C) are shown here. After 60 hours, animals have developed to the adult stage. Smaller objects observed after 65 hours were the next generation of newly hatched L1 larvae laid by the animals that developed during the time course.



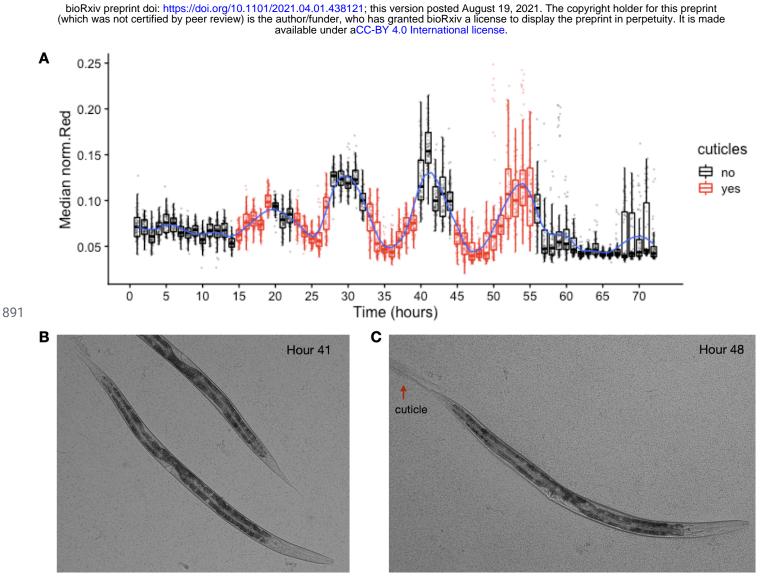
S2 Fig. Correlation analysis of body size measurements. Manual measurements of animal length, width, and estimated area were compared to COPAS BIOSORT measurements of TOF, norm.EXT, and EXT. Kendall correlation value is shown in each plot.



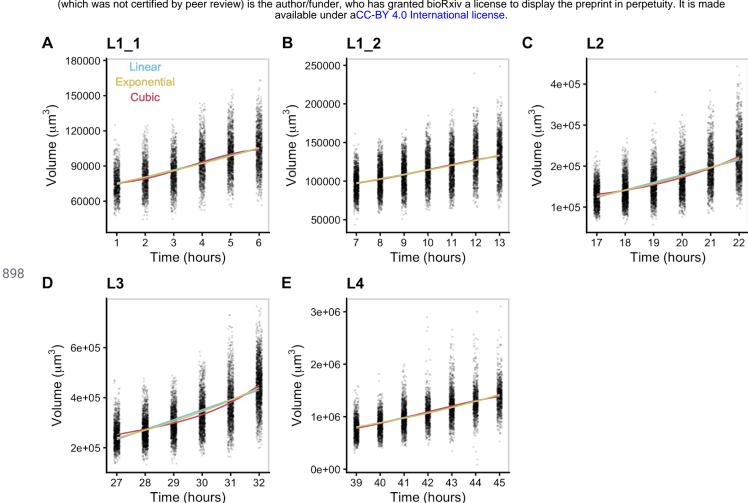
S3 Fig. Mixture modeling of COPAS BIOSORT data was used to prune data. Mixture models of Gaussian distributions were fit to log transformed animal length (x-axis) and log transformed optical extinction (y-axis). Data from each hour of the experiment was analyzed and processed to remove clusters that did not include animal objects. All replicates were pruned independently; a subset of data from replicate 2 is shown here. Panels indicate experimental hours from which data were taken.



S4 Fig. Fluorescence measurements normalized by body size. Red fluorescence beads were fed to animals during experimentation and fluorescence data was collected by the COPAS BIOSORT. Fluctuations in fluorescence indicate fluctuations in feeding behavior. Fluorescence data was normalized by body size measurements to account for increases in body size. Dividing fluorescence by area was most successful in normalizing fluorescence dynamics to account for changes in animal size over time.

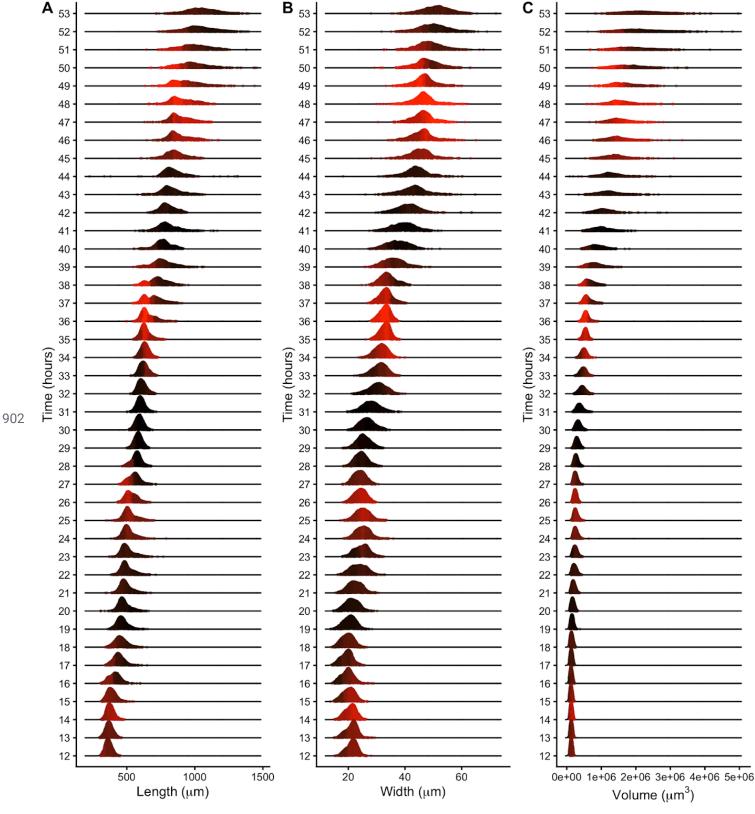


S5 Fig. Cuticles identified during periods of decreased feeding. Images of wells collected during the experiment were examined for evidence of shed cuticles. (A) Experimental hours where cuticles were identified from images overlap with hours where population feeding behavior is low. Cuticles shed from the L4-Adult molt persisted longer than previous larval stage cuticle debri. (B) Example image of animal without visible cuticle during a period of elevated feeding. (C) Example image of an animal with visible cuticle indicating completion of molt during a period of decreased feeding.



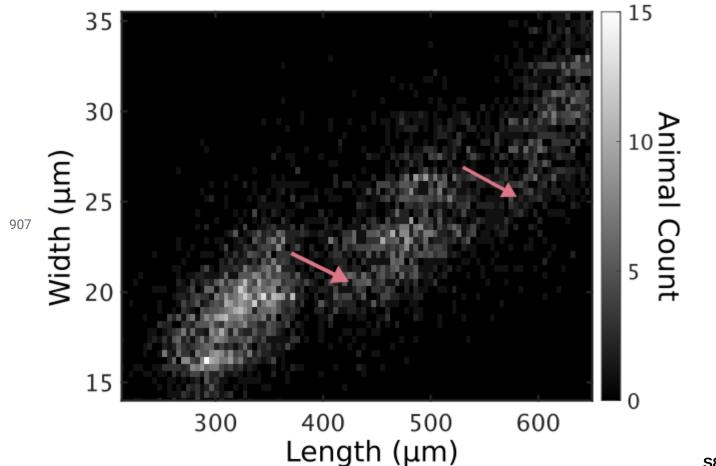
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899 S6 Fig. Volume growth data fit with linear, exponential, and cubic models. Volume data of individuals in 900 time points defined as growth periods are analyzed for each stage. L1 stage was further separated into two 901 periods to account for the volume dip that occurs mid-stage.



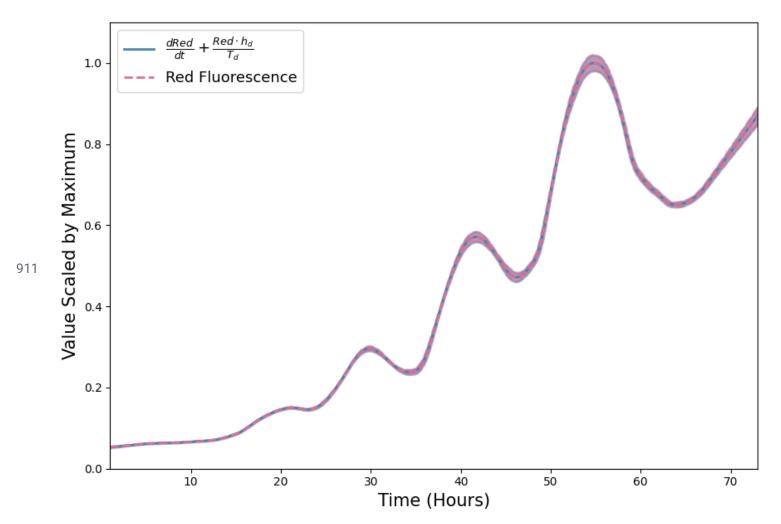
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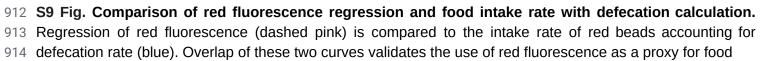
903 **S7 Fig. Density plots of population size dynamics across all larval transitions.** Density curves of length 904 (A), width (B) and volume (C). Curves are divided into five quantiles and colored by the percentage of 905 quiescent animals present within that quantile. Molts are estimated to occur at experimental hours 14, 25, 36, 906 and 48 (see Methods).

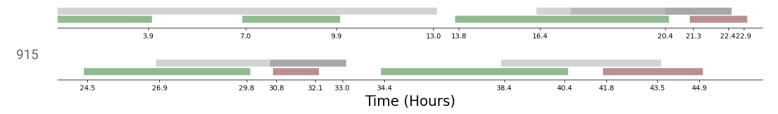


S8 Fig.

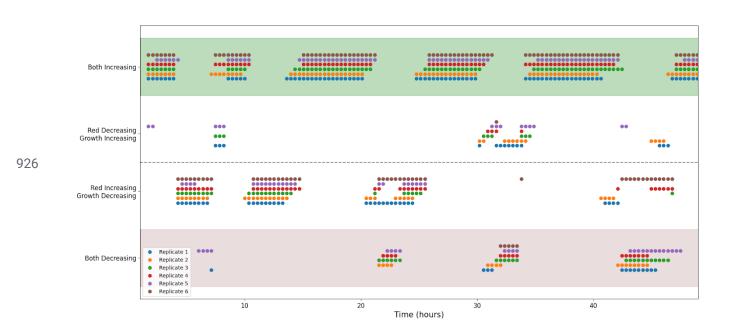
Animals in all replicates, measured from images. Animal length and width over *C. elegans* development captured from image data. Higher noise levels in these measurements preclude accurate regressions to individual larval stages. Length jumps and width dips are still apparent. Compare with Fig 6.



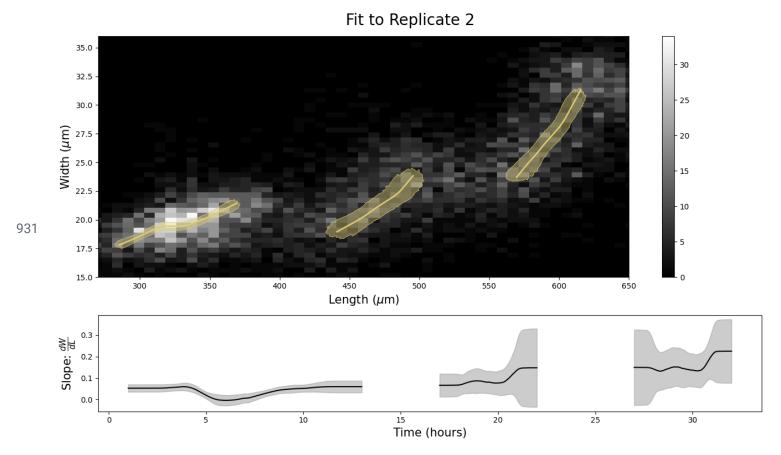




S10 Fig. Timeline of Food Utilization and Stretcher events. In the first row (grey and white), we mark the slopes determined in the Stretcher model. Transition from lighter to darker grey indicates a step increase in slope corresponding to a stiffening cuticle in the length direction. White regions denote time between larval stages. L2 and L3 are the only stages at which we have useful slope information due to the change in slope observed during L1 making transitions difficult to determine and the high level of population desynchronization in L4. In the second row (green, red, and white), we mark the food and growth correlations found in Fig 5B. Green corresponds to times at which both growth rate and food rate are increasing. Red corresponds to times at which both growth rate and food rate are decreasing. White corresponds to times at which growth rate and food rate are uncorrelated. Transitions from green to red regions occur at roughly the same times as the transition to a stiffer cuticle in the length direction.

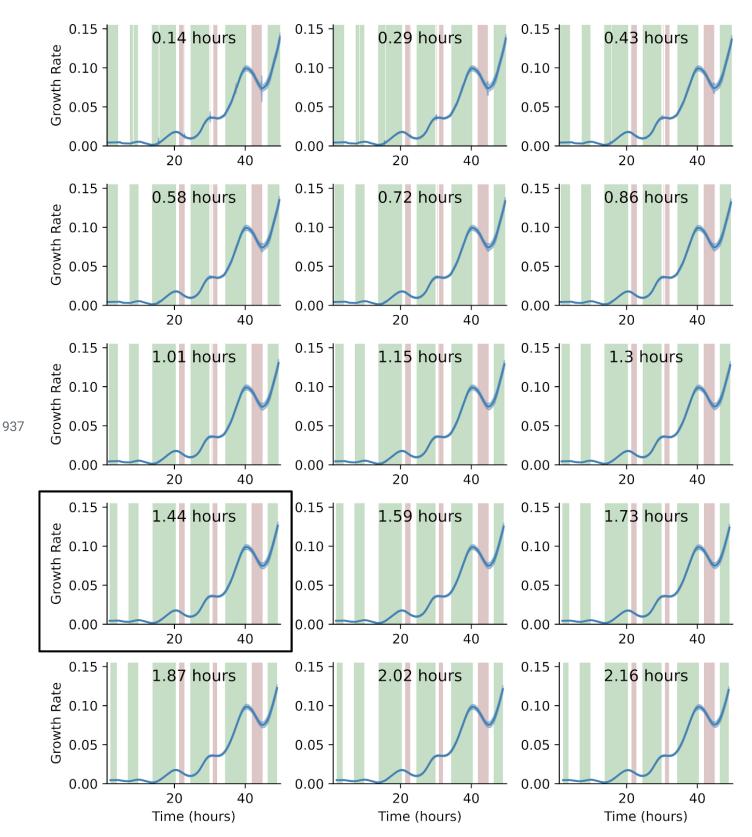


927 S11 Fig. Analysis of Food intake and growth rate correlation for all replicates. Summary of analysis in
928 Fig. 8 for all replicates. Until larval stage L4, most replicates followed the same pattern of transitions from one
929 growth regime to the next. The time delay at transitions in later replicates can be explained by the temperature
930 gradient and differences in growth between replicates.



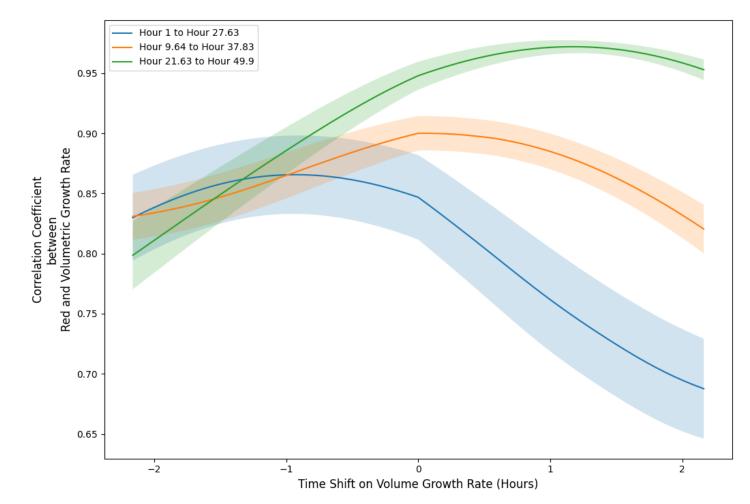
932 S12 Fig. Stretcher model analysis of replicate 2 COPAS BIOSORT data for different stage thresholding.933 Compare to Fig 5. Larval hours were defined by taking the ceiling of the lower boundary and the floor of the934 upper boundary. This rounding method for larval stage definition demonstrates the sensitivity of the analysis to935 edge effects. The unexpected step in the L2 larval stage (Fig 5) was significantly reduced with this rounding936 method.

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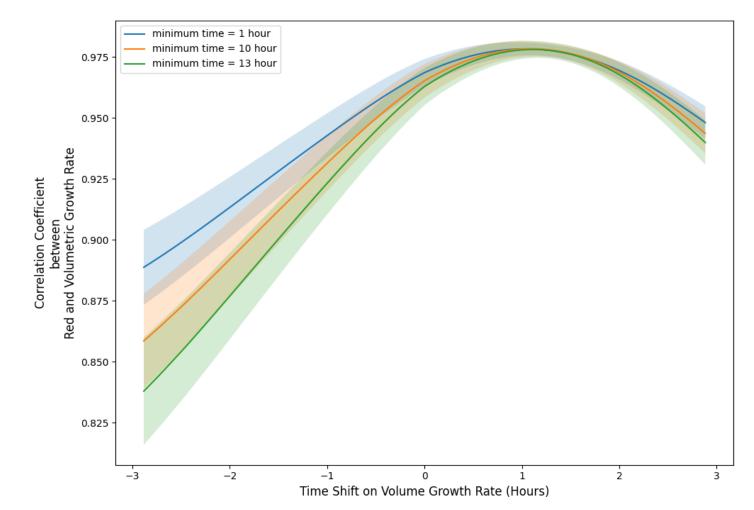


938 S13 Fig. Sensitivity analysis to moving average window size. Varying lengths of window sizes (0.14 to 939 2.16 hours) were calculated for the *lokern* growth rate regression. Window size was increased until the growth 940 rate regression was smoothed. A window size of 1.44 hours (or 0.72 hours on either side of each time point) 941 was chosen to calculate the start and end times of each regime (Fig 8). Continued increase of window size 942 past 1.44 hours did not change the pattern of regimes or their boundaries significantly.

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S14 Fig. Time Lag Analysis. Subsections of food intake rate and growth rate regressions were compared to determine the existing time lag between the two curves. The time shift is applied to the volume growth rate. A correlation coefficient was calculated for the new volume growth rate curve and the untouched red fluorescence regression curve for each bootstrap regression. The solid line corresponds to the mean of all the correlation coefficients over the bootstrapping iterations and the shaded regions correspond to the standard deviation. The blue curve corresponds to hours containing L1 and L2, the orange curve corresponds to hours containing L2 and L3, and the green curve corresponds to hours containing L3 and L4. The time lag at which the correlation between Red fluorescence and volume growth rate is at a maximum corresponds to the sparent time lag between the two curves. No single time lag captures the entirety of development.



S15 Fig. Time Lag Analysis. Dynamics over all development for food intake rate and growth rate regressions were compared to determine the existing time lag between the two curves. The time shift was applied to the volume growth rate. A correlation coefficient was calculated for the new volume growth rate curve and the untouched red fluorescence regression curve for each bootstrap regression. The solid line corresponds to the mean of all the correlation coefficients over the bootstrapping iterations and the shaded regions correspond to the standard deviation. Due to the qualitatively different dynamics in L1, we calculated correlation for L1-L4 (blue), the second half of L1 -L4 (orange), and L2-L4 (green). All curves show that there is an overall time shift of +1 hour (meaning changes in volume growth rate precede changes in food intake rate), matching the L3-L4 curve in S14 Fig but still a <90% correlation with no time lag.

Response = Norm.Red							
Terms	Df	Sum Sq	Mean Sq	F value	Pr(>F)	% Var Explained	
hour	1	439.46	439.46	217762.01	0	54.34	
replicate	6	165.82	27.64	13694.48	0	20.51	
well	10	0.32	0.03	15.62	0	0.04	
Residuals	100619	203.06	0	NA	NA	25.11	

Response = Length

Terms	Df	Sum Sq	Mean Sq	F value	Pr(>F)	% Var Explained
hour	1	86190107879	86190107879	8223506	0	98.4
replicate	6	349438944	58239824	5557	0	0.4
well	10	834970	83497	8	0	0
Residuals	100619	1054582098	10481	NA	NA	1.2

Response = Width

Terms	Df	Sum Sq	Mean Sq	F value	Pr(>F)	% Var Explained
hour	1	209090438.47	209090438.47	6950760.3	0	97.99
replicate	6	1266985.87	211164.31	7019.7	0	0.59
well	10	1495.32	149.53	4.97	0	0
Residuals	100619	3026786.99	30.08	NA	NA	1.42

Response = Volume

Terms	Df	Sum Sq	Mean Sq	F value	Pr(>F)	% Var Explained
hour	1	621712474191714688	621712474191714688	843342	0	84.08
replicate	6	43356968850687072	7226161475114512	9802	0	5.86
well	10	152458715405862	15245871540586	21	0	0.02
Residuals	100619	74176459811167296	737201321929	NA	NA	10.03

961 **S1 Table. Results of analysis of variance models fit to COPAS BIOSORT data.** Analysis of variance tests 962 were used to quantify the amount of variance in our data contributed by the sampling technique. The sampling 963 technique involved unbiased sampling of animals from six replicate populations and subsequent distribution 964 into multiple wells of a microtiter plate for analysis. We quantified the amount of variance contributed by

replicate and well. We find that the variance explained by well is nearly negligible whereas replicate contributes
minor variance in some measurements. Given this information, we deem the generated summary statistics an
appropriate representation of the population.

		ΔAIC			ΔBIC			
Stage	Linear	Exponential	Cubic	Linear	Exponential	Cubic	Best model by AIC	Best model by BIC
L1_1	17	21	0	4	9	0	Cubic	Likely Cubic
L1_2	2	4	0	0	2	12	Can't distinguish	Can't distinguish
L2	142	43	0	128	28	0	Cubic	Cubic
L3	374	145	0	360	131	0	Cubic	Cubic
L4	4	44	0	0	40	10	Likely Cubic	Linear

968 S2 Table. Model fit criteria used to assess candidate growth models. To determine the level of support for 969 each model, the candidate model with the smallest raw AIC/BIC was identified and compared to other AIC/BIC 970 values. If the delta value was greater than 6, the model with the smallest AIC/BIC value was denoted as the 971 best model. If the delta value was less than 6 but greater than 2, the model with the smallest AIC/BIC value 972 was determined to likely be the best model. If the delta value was less than 2, we are unable to distinguish the 973 model of best fit.

Green Regions

Stage	Food Intake Dynamical Range (AFU)	Food to Growth Dynamical Range - Lower Estimate (AFU)	Food to Growth Dynamical Range - Higher Estimate (AFU)
L1 (1)	1	0	0
L1 (2)	1	2	2
L2	15	12	15
L3	29	21	27
L4	65	54	69

Red Regions

Stage	Food Intake Dynamical Range (AFU)	Food to Growth Dynamical Range - Lower Estimate (AFU)	Food to Growth Dynamical Range - Higher Estimate (AFU)
L1			
L2	1	4	5
L3	6	3	4
L4	16	27	35

White Regions Preceding Molt

Stage	Food Intake Dynamical Range (AFU)	Food to Growth Dynamical Range - Lower Estimate (AFU)	Food to Growth Dynamical Range - Higher Estimate (AFU)
L1 -> L2	2	3	4
L2 - > L3	3	1	2
L3 - > L4	5	2	3
L4 - > Adult	5	2	3

Whole Larval Stage

Stage	Food Intake Dynamical Range (AFU)	Food to Growth Dynamical Range - Lower Estimate (AFU)	Food to Growth Dynamical Range - Higher Estimate (AFU)
L1	4	2	3
L2	19	12	15
L3	29	21	28
L4	70	52	67

974 **S3 Table.** Comparison of dynamical ranges between total food intake and food used for growth.

975 S1 File. Incubator temperature data. Temperature recordings of each position within the shaking incubator

- 976 used for the growth experiment. (CSV)
- 977 S2 File. COPAS BIOSORT growth data. Raw growth data collected from the COPAS BIOSORT and
- 978 processed using the easysorter R package to compile information from each well. (CSV)
- 979 S3 File. Pruned COPAS BIOSORT growth data. Processed data from the COPAS BIOSORT following
- 980 implementation of the mclust R package and removal of clusters containing non-animal objects. (CSV)
- 981 S4 File. Image growth data. Manual measurements of animal size acquired from images. (CSV)
- 982 S5 File. Model derivations.

1 Model Derivations

² Bootstrapping Algorithm

³ To calculate a robust regression of the measured COPAS BIOSORT data we bootstrap the regression using

4 case-resampling (Davison and Hinkley 1997, pages 261-266). Each iteration of the algorithm (Algorithm

- $_5$ S1) involves resampling the data of interest with replacement and maintaining the size of the sample. At
- 6 each iteration the lokern regression is calculated for Red, Length, and Width data. Additionally any desired
- 7 function (for example, volume, pumping frequency times pharynx fraction, or derivatives) of these regressions
- s is calculated at each iteration. Regressions at each iteration are saved and the mean and variance of these
- ⁹ regressions at each regression time point are used to determine the statistics of the regression.

Algorithm S1 Regression Bootstrapping with Case Resampling

Ndata = # animals in sample; iterations = # resamplings;

for i = 0 to iterations **do**

Resample Ndata points with replacement. Collect Red, Length, Width data;

Apply lokern regression to resampled Red, Length, Width;

Calculate desired functions of Red, Length, Width regressions;

Save Red, Length, Width, and combined regressions; end for

Calculate Standard deviation at each regression time point of saved regressions;

¹⁰ Derivation of eating model

¹¹ We begin by defining the instantaneous rate of food intake as a function of the flow rate of media through

¹² the buccal cavity and the cross sectional area of the buccal cavity.

$$\frac{dV_{food}}{dt} = A_{buccal} \tag{S1}$$

¹³ We then make the assumption that the uptake of media fills the pharyngeal lumen we have

$$\frac{dV_{food}}{dt} = C \frac{dV_{lumen}}{dt} \tag{S2}$$

We average both sides of the equation under the assumption that the pumping period is significantly shorter than the time scale of growth

$$\frac{1}{T} \int_0^T \frac{dV_{food}}{dt} dt = \frac{1}{T} \int_0^T CA_{buccal}$$
(S3)

 $\frac{1}{T} \int_0^T \frac{dV_{food}}{dt} dt = \frac{1}{T} \Delta V_{food}$ (S4)

We then take into account that food is not transported to the gut in the same step as its uptake. Thus 17 the total food intake during a single pump can be calculated by the amount of food that fills the fully opened 18 pharyngeal lumen 19

The integral on the right hand side is the total food intake during a single pumping period.

16

$$\frac{1}{T} \int_0^T \frac{dV_{food}}{dt} dt = \frac{C}{T} V_{lumen:max}$$
(S5)

We then replace the average on the right hand side with the average food intake rate over the pumping 20 period. For simplicity and because we will deal entirely with the average food intake rate, we do not use a 21 different notation for this average rate. 22

$$\frac{dV_{food}}{dt} = \frac{C}{T} V_{lumen:max} = Cf(t) V_{lumen:max}$$
(S6)

Transformation of sorter measurements to volume units 23

To utilize sorter measurements and convert them to meaningful units we define a linear transformation from 24 the correlation plots (S1 Fig) 25

$$L = a_1 T O F + b_1 \tag{S7}$$

$$W = a_2 norm. EXT + b_2. \tag{S8}$$

Using Equations (S7) and (S8) we can approximate the volume of any object that passes through the 26 sorter by the expression 27

$$V = \frac{\pi}{4} (a_1 T O F + b_1) (a_2 norm. EXT + b_2)^2.$$
 (S9)

²⁸ Defecation analysis

We use the defecation results found in (Liu and Thomas 1994) to determine if red fluorescent measurements can be used as a proxy for food intake rate as opposed to the instantaneous food volume in the gut. Defecation in adults happens very regularly, with a period of $T_d = 45 \pm 3s$, with $h_d = 43 \pm 10\%$ of their intestinal volume being expelled each time. The volume expelled is well mixed. Defining V_f as the current amount of food in the nematode gut. We can use conservation of mass to state that the rate of change in the amount of food in the gut is equal to the rate of food intake through eating less the defecation rate and the rate at which food volume is metabolized into cell products:

$$\frac{dV_f}{dt} = \left. \frac{dV_f}{dt} \right|_{eating} - \left. \frac{dV_f}{dt} \right|_{defecating} - \left. \frac{dV_f}{dt} \right|_{metabolized}$$
(S10)

Using red fluorescence as a proxy for food intake we can ignore the metabolism term as the fluorescent beads are not metabolized.

$$\frac{dV_f}{dt} = \left. \frac{dV_f}{dt} \right|_{eating} - \left. \frac{dV_f}{dt} \right|_{defecating} \tag{S11}$$

Equation (S11) states that the rate of change of the volume of fluorescent beads in the gut is equal to the difference between the intake of red fluorescent beads minus the defecation rate of red fluorescent beads. Using the results of (Liu and Thomas 1994) for the second term, and defining $V_{f:max}$ as the volume of food in the gut just prior to defecation, h_d as the fraction of food expelled during a single defecation cycle, and T_d as the period of defecation. We average Equation (S11) over short time periods to remove the pumping and defecation period oscillations.

$$\frac{dV_{red:max}}{dt} = \left. \frac{dV_r e d}{dt} \right|_{eating} - \frac{V_{red:max} h_d}{T_d} \tag{S12}$$

On the left hand side, the instantaneous rate of the gut red fluorescence in Equation (S11) is replaced by the rate of change of the maximum or "full" gut fluorescence. The second term on the right hand side of Equation (S11) has been replaced by the average defecation rate over a cycle calculated by multiplying the full gut fluorescence by the fraction expelled and dividing by the defecation period. We solve Equation (S12) for the average eating rate.

$$\left. \frac{dV_{red}}{dt} \right|_{eating} = \frac{dV_{red:max}}{dt} + \frac{V_{red:max}h_d}{T_d} \tag{S13}$$

49 We take the local regression of the red fluorescence to determine $V_{red:max}(t)$. This value is plugged into

the second term on the right hand side of Equation (S13) and its derivative is used to approximate the first term on the right hand side of Equation (S13). We take the adult values of h_d and T_d (Liu and Thomas 1994) as a first approximation. Figure (S6) demonstrates a comparison of the red fluorescence and the red intake rate with defecation taken into account at the constant adult rates and quantities. We have scaled both the pink curve denoting red fluorescence and the blue curve denoting red intake rate by their maximum. This scaling allows us to see that the two curves are only a multiplicative factor apart up to error bars. This allows us to use the red measurement as a proxy for both red and food intake rates.

57 Food Allocation Breakdown Calculation

We calculate an example of resource allocation breakdown. We begin with the expression in Equation (8) of the main text relating food intake rate and animal growth rate and repeated here:

$$\frac{dV_{worm}}{dt} = \eta(t)\alpha(t)\frac{dV_{food}}{dt}$$
(S14)

Here $\eta(t)$ is metabolic efficiency and is characteristic of the nematodes and food source used. $\alpha(t)$ is the fraction of total ingested food allocated towards growth.

⁶² We make an additional assumption that food needed to maintain life is proportional to animal volume:

$$\frac{dV_{food:maint}}{dt} = \beta V_{worm}(t) \tag{S15}$$

⁶³ Here we define $\frac{dV_{food:maint}}{dt}$ as the rate of food intake required to maintain life and β is the constant of ⁶⁴ proportionality that relates animal size to required maintenance food levels. We assume that β is a constant ⁶⁵ over developmental time and depends on the food source available.

From the analysis from the previous section we can use red fluorescence as a proxy for food intake rate such that

$$\frac{dV_{food}}{dt} \propto Red \tag{S16}$$

$$\frac{dV_{worm}}{dt} \propto \eta(t)\alpha(t)Red \tag{S17}$$

$$\eta(t)\alpha(t) \propto \left(\frac{dV_{worm}}{dt}\right)/Red$$
(S18)

The constant of proportionality in Equation (S18) is unknown due to the unknown relationship between food volume and red fluorescence. We make the assumption that metabolic efficiency is constant over time

⁷⁰ and any variation in the value calculated by Equation (S18) is due to changes in $\alpha(t)$, the allocation of food ⁷¹ toward growth.

To calculate an estimate for the breakdown of food allocation, we assume a set of constants of proportionality for Equations (S15) and (S18). We assume that at the time at which the $\eta(t)\alpha(t)$ curve is at its maximum (hour 40), 10% of food resources are allocated towards maintenance, 70% (low growth estimate) or 90% (high growth estimate) are allocated towards growth, and the remainder is allocated to other metabolic processes. The resulting scaling factors are applied over developmental time to calculate an estimated food allocation breakdown and presented in Figure (8) of the main text.

78 Derivation of Stretcher Model

We model the cuticle as a thin walled pressure vessel made of orthotropic, linear materials to capture the relationship between how much the cuticle stretches and the force applied to the cuticle. The relationship between the amount of stretch and the amount of applied pressure is described by the matrix:

$$\begin{bmatrix} \varepsilon_L \\ \varepsilon_{Circ} \end{bmatrix} = \begin{bmatrix} \frac{1}{E_L} & \frac{-v_{cl}}{E_c} \\ \frac{-v_{lc}}{E_L} & \frac{1}{E_c} \end{bmatrix} \begin{bmatrix} \sigma_L \\ \sigma_{Circ} \end{bmatrix}$$
(S19)

Here E_L and E_C are the Young's modulus in the length and circumferential direction, and v_{cl} and v_{lc} are the appropriate Poisson's ratios. These material properties can be measured experimentally. Normalized stretch, ε , is defined as the change in size normalized by the initial size of a cuticle in length (L) and circumference (Circ) (Equations S20 - S21). Here σ is the normalized force applied along the length and circumferential directions of the cuticle (Equations S23 - S24).

$$\varepsilon_L = \frac{\Delta L}{L_0} \tag{S20}$$

$$\varepsilon_{Circ} = \frac{\Delta Circ}{Circ_0} \tag{S21}$$

Here L_0 and $Circ_0$ are the length and circumference of the cuticle at the onset of stretch, or in other words at the start of a larval stage. Experimentally we measure width, not circumference, but the circumference of a circle is proportional to the width of the circle, so we can replace the circumference with the measured width:

$$\frac{\Delta Circ}{Circ_0} = \frac{\pi \Delta W}{\pi W_0} = \frac{\Delta W}{W_0}$$
(S22)

By approximating C. elegans as cylindrical, and assuming the only force working on the cuticle is isotropic internal pressure, we can determine the normalized force in terms of pressure and geometric properties:

$$\sigma_L = \frac{r}{2t} \Delta p \tag{S23}$$

$$\sigma_{Circ} = \frac{r}{t} \Delta p \tag{S24}$$

Where r is the radius of the cylinder and t is the thickness of the cuticle. We can now rewrite Equation (S19) in terms of measurable quantities (length and width) by multiplying out the matrices making the appropriate substitutions.

$$\Delta L = \frac{L_0 r}{t} \left(\frac{1}{2E_L} - \frac{v_{cl}}{E_c} \right) \Delta p = a_L \Delta p \tag{S25}$$

$$\Delta W = \frac{W_0 r}{t} \left(\frac{1}{E_C} - \frac{v_{lc}}{E_L} \right) \Delta p = a_W \Delta p \tag{S26}$$

Here we compress the coefficients fixed by material and geometric properties into one constant

$$a_L = \frac{L_0 r}{t} \left(\frac{1}{2E_L} - \frac{v_{cl}}{E_c} \right) \tag{S27}$$

$$a_W = \frac{W_0 r}{t} \left(\frac{1}{E_c} - \frac{v_{lc}}{E_L} \right) \tag{S28}$$

⁹⁶ Stretcher Slope Calculations

⁹⁷ The Stretcher model predicts a constant ratio between stretch in width, ΔW , and stretch in length, ΔL . ⁹⁸ These measures of stretch are changes in the length and width measurements over some period of time. To ⁹⁹ see how the ratio of $\frac{\Delta W}{\Delta L}$ changes throughout a larval stage, we need to measure the stretch instantaneously. ¹⁰⁰ To do this we take advantage of the derivative approximation

$$\Delta W \approx \frac{dW}{dt} \Delta t \tag{S29}$$

$$\Delta L \approx \frac{dL}{dt} \Delta t \tag{S30}$$

¹⁰¹ Equations (S29, S30) are combined in the ratio found in Equation (3) to give:

$$\frac{\Delta W}{\Delta L} \approx \frac{W'(t)}{L'(t)} \tag{S31}$$

Here $W' = \frac{dW}{dt}$ and $L' = \frac{dL}{dt}$. We differentiate the time series from the local regressions of length and width data. The ratio of derivatives gives the instantaneous stretch ratio as it changes over time. Due to the numerical difficulty of calculating both derivatives and ratios with accuracy, we expect large error bars for this ratio. To estimate the size of error bars we apply a first order error propagation formula to Equation (S31).

$$\sigma_{Ratio}^2 \approx \left| \frac{\partial Ratio}{\partial (W')} \right|^2 \sigma_{(W')}^2 + \left| \frac{\partial Ratio}{\partial (L')} \right|^2 \sigma_{(L')}^2 + 2 \frac{\partial Ratio}{\partial (W')} \frac{\partial Ratio}{\partial (L')} \sigma_{(W')(L')}$$
(S32)

$$\sigma_{Ratio}^2 \approx \left| \frac{1}{L'} \right|^2 \sigma_{(W')}^2 + \left| \frac{-(W')^2}{(L')^3} \right|^2 \sigma_{(L')}^2 - 2\frac{W'}{(L')^3} \sigma_{(W')(L')}$$
(S33)

The variance in Equation (S33) is calculated for each time point in the regressions of length and width. We resample the data for each larval stage 2,000 times with replacement (see Methods for larval stage determination). For each of these resampled sets of data, we numerically differentiate the length and width regression to determine an estimate of the length and width derivatives over time. At each time point the mean regression length and width derivatives are used in place of W' and L'. The covariance matrix for the length and width derivatives is calculated at each time point using the 2,000 resampled regressions in the bootstrap analysis and used as the variance terms in Equation (S33).