

1 **Substrate specialization in microbes is driven by biochemical**
2 **constraints of dynamic flux sensing**

3 Severin Josef Schink^{1,*}, Dimitris Christodoulou^{1,2,*}, Avik Mukherjee^{1,3}, Edward Athaide¹, Viktoria
4 Brunner², Tobias Fuhrer², Gary Andrew Bradshaw⁴, Uwe Sauer^{2,#} and Markus Basan^{1,#}

5
6 * Equal contribution

7 ¹ Systems Biology Department, Harvard Medical School, 200 Longwood Ave, Boston, MA 02115, USA

8 ² Institute of Molecular Systems Biology, ETH Zurich, Zurich 8093, Switzerland

9 ³ Applied Mathematics Department, Harvard College, Cambridge, MA 02138, USA

10 ⁴ Laboratory of Systems Pharmacology, Harvard Program in Therapeutic Science, Harvard Medical School,
11 200 Longwood Ave, Boston, MA 02115, USA

12 # Correspondence: sauer@imsb.biol.ethz.ch, markus@hms.harvard.edu

13

14 **Central carbon metabolism is highly conserved across microbial species, but operates**
15 **in very different ways depending on the organism and their ecological niche. Here,**
16 **we study the dynamic re-organization of central metabolism after switches between**
17 **the two major opposing pathway configurations of central carbon metabolism,**
18 **glycolysis and gluconeogenesis in different bacteria. We combined growth**
19 **dynamics and dynamic changes of intracellular metabolite levels with a coarse-**
20 **grained model that integrates fluxes, regulation, protein synthesis and growth and**
21 **uncovered fundamental limitations of the regulatory network: after nutrient shifts,**
22 **metabolite concentrations collapse to their equilibrium, turning the cell ‘blind’ to**
23 **which direction the flux is supposed to flow through the metabolic network. The cell**
24 **can partially alleviate this ‘blindness’ by picking a preferred direction of regulation,**
25 **at the expense of increasing lag times in the opposite direction. Moreover, decreasing**
26 **both lag times simultaneously comes at the cost of reduced growth rate or higher futile**
27 **cycling between metabolic enzymes. These three trade-offs can explain why**
28 **microorganisms specialize for either glycolytic or gluconeogenic substrates and can**
29 **help elucidate the complex growth patterns exhibited by different microbial species.**

30 **Introduction**

31 Fast growth and quick physiological adaptation to changing environments are key
32 determinants of fitness in frequently changing environments that microorganisms
33 encounter in the wild. But in comparison with steady state exponential growth,
34 understanding of the physiology of growth transitions has remained largely elusive. For
35 steady state exponential growth, metabolic models have made substantial progress over the
36 last two decades, elucidating the flux and regulatory networks that govern the coordination
37 of microbial metabolism (Bennett et al., 2009; Bordbar et al., 2014; Chubukov et al., 2014;
38 Gerosa et al., 2015a; Link et al., 2013; Noor et al., 2010, 2014; Vasilakou et al., 2016).
39 Such metabolic model were successfully expanded to dynamic environments (Zampar et
40 al., 2013; Chassagnole et al., 2002; Chakrabarti et al., 2013; Saa and Nielsen, 2015;
41 Andreozzi et al., 2016; Yang et al., 2019) and used to gather vital information about
42 metabolism, using perturbations (Link et al., 2013), stimulus response experiments
43 (Chassagnole et al., 2002) or sequential nutrient depletion (Yang et al., 2019) to validate
44 and improve metabolic models. But, dynamic changes of metabolism like shifts in growth
45 conditions continue to pose a considerable challenge. Changes in enzyme abundance alone
46 cannot explain the variation of phenotypes exhibited by individual microbial species, nor
47 between different species, and it is still unclear what determines how long bacteria need to
48 adapt upon a change of the environment.

49

50 One example of such a switch happens when microbes deplete their primary nutrient.
51 *Escherichia coli* preferentially utilizes hexose sugars like glucose that are metabolized via
52 glycolysis (Gerosa et al., 2015b). To maximize growth on sugars, *E. coli* excretes
53 substantial ‘overflow’ production of acetate, even in the presence of oxygen (Basan et al.,
54 2015a, 2017). This naturally leads to bi-phasic growth, where initial utilization of glucose
55 is followed by a switch to acetate. Similar growth transitions from preferred glycolytic
56 substrates to alcohols and organic acids ubiquitously occur for microbes in natural
57 environments (Buescher et al., 2012; Otterstedt et al., 2004; Zampar et al., 2013). Since
58 these fermentation products are all gluconeogenic, they require a reversal of the flux
59 direction in the glycolysis pathway, which results in multi-hour lag phases caused by the
60 depletion of metabolite pools throughout the gluconeogenesis pathway (Basan et al., 2020).

61 Similar long lag times in glycolytic to gluconeogenic shifts were observed for *Bacillus*
62 *subtilis* and the yeast *Saccharomyces cerevisiae* (Basan et al., 2020). Shifts in the opposite
63 direction, however, from gluconeogenic substrates to glycolytic ones, occur much more
64 quickly in *E. coli* and other preferentially hexose fermenting microbes, in some cases even
65 without detectable lag phases (Basan et al., 2020).

66

67 In our previous work (Basan et al., 2020), we showed how the growth rate dependence of
68 enzyme expression leads to a universal relation between lag times and preshift growth rates
69 and found evidence that futile cycling at irreversible metabolic reactions plays an important
70 role for causing lag times. However, we were unable to answer the most fundamental
71 questions raised by these observations: Why are microorganisms like *E. coli* or *S.*
72 *cerevisiae* unable to overcome lag phases by expressing more metabolic enzymes or
73 allosteric regulations that turn off futile cycling after metabolic shifts? Given the small
74 number of enzymes involved in these irreversible reactions, their cost in terms of proteome
75 allocation is likely minimal. Instead, microbes like *E. coli* appear to be intentionally
76 limiting enzyme expression and decreasing their growth rates on many glycolytic
77 substrates (Basan et al., 2017). Moreover, why do shifts from glycolytic to gluconeogenic
78 conditions result in lag times of many hours, while shifts from gluconeogenic to glycolytic
79 conditions only take minutes? Given the symmetry of central metabolism, one would
80 expect similar lag phases in the opposite direction. Is this preference for glycolysis a
81 fundamental property of central metabolism or rather an evolutionary choice of individual
82 species? At the core of these questions is a gap in understanding of how central carbon
83 metabolism adjusts itself to nutritional changes.

84

85 Here, we study growth and metabolite dynamics of *E. coli*, *Pseudomonas aeruginosa* and
86 *Pseudomonas putida* using a kinetic model of central carbon metabolism to overcome this
87 challenge. Our model coarse-grains central metabolism to a low number of irreversible and
88 reversible reactions, which allows us to focus on the dynamics of key metabolites and their
89 regulatory action. The model couples metabolism to enzyme abundance via allosteric
90 regulation and enzyme expression to the concentration of regulatory metabolites via
91 transcriptional regulation and flux dependent protein synthesis. Our formulation of

92 metabolism and growth bridges fast metabolic time scales with slow protein synthesis. As
93 we demonstrate, our model can explain a major reorganization of metabolism in response
94 to nutrients shifts: the switching of the directionality of metabolic flux between glycolysis
95 and gluconeogenesis. Dependent on the required directionality of flux in central
96 metabolism, enzymes catalyzing the required flux direction are expressed and catalytically
97 active, while enzymes catalyzing the opposite flux are expressed at low levels and their
98 activities are repressed by allosteric regulation. This self-organization is key for enabling
99 fast growth and preventing costly futile cycling between metabolic reactions in opposing
100 directions, which can inhibit flux and deplete ATP in the process.

101

102 Reestablishing this self-organization after growth shifts is limited by biochemical
103 constraints to sense fluxes and to regulate accordingly. When metabolite levels transiently
104 collapse, allosteric and transcriptional regulation cannot distinguish between glycolysis
105 and gluconeogenesis, turning the cell ‘blind’ to the direction of flux. By choosing the
106 activity of metabolic enzymes at these low metabolite levels to favor one direction, the cell
107 can enable fast switching at the expense of the other direction. This choice of direction in
108 the absence of information becomes the ‘default state’ of central metabolism and
109 determines the substrate preference.

110

111 According to the model, the preferred direction does not need to be glycolysis, and in
112 principle gluconeogenic specialists with a gluconeogenic ‘default’ state could have evolved,
113 too. Indeed, we showed that *P. aeruginosa* shows reversed lag time and growth phenotypes
114 compared to those of *E. coli*, which verified that long lag times to glycolytic substrates are
115 caused by the same inability to sense flux after nutrient shifts.

116

117 **Results**

118 *An integrated, self-consistent kinetic model of glycolysis / gluconeogenesis*

119 In a shift between glycolysis and gluconeogenesis, flux in central metabolism needs to be
120 reversed. To understand what limits the speed of adaptation between those two modes of
121 flux, we turn to a theoretical model of central metabolism. But because the complexity of
122 central metabolism with intertwined regulation at different levels prevents tracing

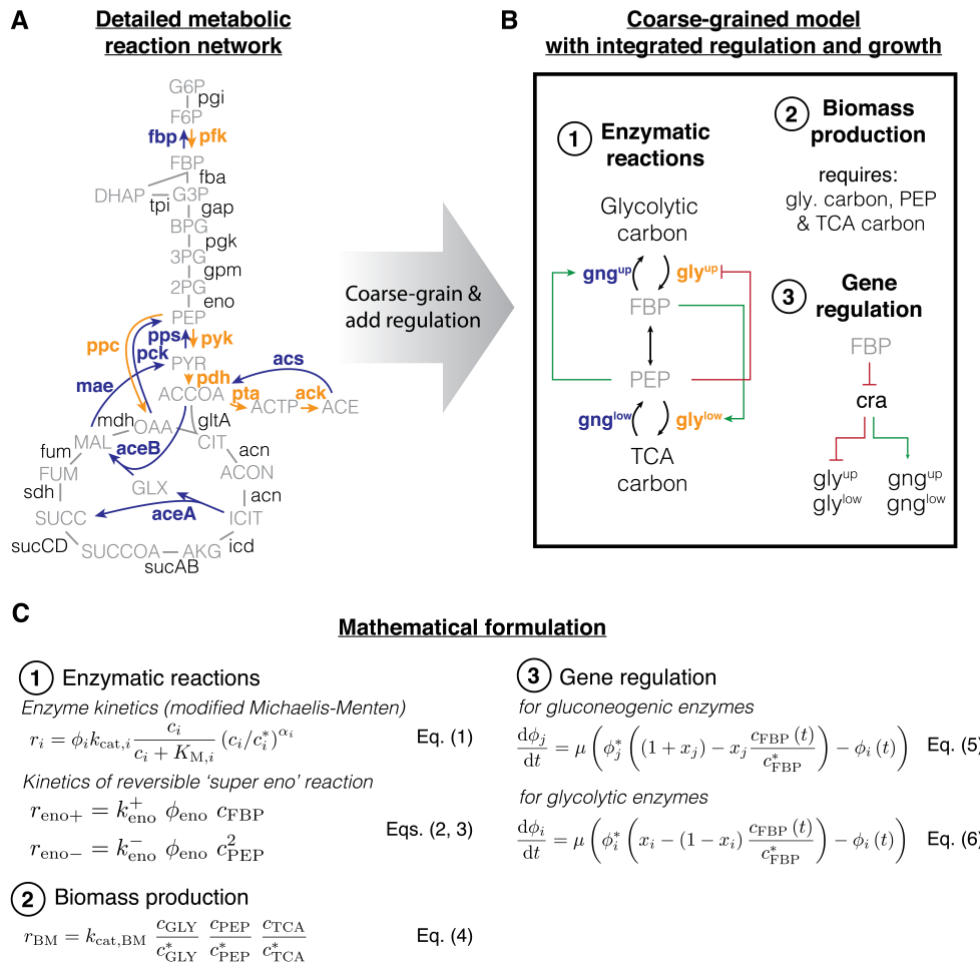
123 quantitative phenotypes to their molecular origins, we sought to focus on the biochemical
124 pathway topology with its key regulations that differentiate glycolysis and gluconeogenesis
125 and constructed a minimal model of central metabolism. The model is illustrated in Box 1
126 and described in detail in the SI. It is based on topology of the biochemical network, the
127 allosteric and the transcriptional regulation of the key the metabolic proteins of *E. coli*, all
128 of which have been well characterized (Berger and Evans, 1991; Ramseier et al., 1995;
129 Johnson and Reinhart, 1997; Pham and Reinhart, 2001; Kelley-Loughnane et al., 2002;
130 Hines et al., 2006; Fenton and Reinhart, 2009).

131

132 The defining feature of the model is a coarse-graining of the irreversible reactions (one-
133 directional arrows in ‘orange’ and ‘blue’, Box 1A) in the upper and lower part of central
134 metabolism into single irreversible reactions (one-directional ‘black’ arrows in Box 1B).
135 While not irreversible in an absolute sense, so-called irreversible reactions are
136 thermodynamically favored so much in one direction that they can be effectively
137 considered as irreversible (Noor et al., 2014). As a result, these irreversible reactions in
138 central metabolism need to be catalyzed by distinct enzymes that perform distinct reactions
139 For example, Fructose 6-phosphate (F6P) is converted to Fructose 1-6-bisphosphate (FBP)
140 by enzyme PfkA using ATP. The opposite direction, FBP to F6P, is performed by a
141 different enzyme, Fbp, which splits off a phosphate by hydrolysis. Each of the two
142 reactions follows a free energy gradient and are irreversible. If both enzymes are present
143 and active then the metabolites will be continuously interconverted between F6P and FBP
144 and in each interconversion one ATP is hydrolyzed to ADP and phosphate. This is a ‘futile
145 cycle’. It drains the cell’s ATP resource and prevents flux going through the biochemical
146 network. Because of this importance of irreversible reactions and futile cycling, we
147 implement irreversible enzymes (‘bold font, blue/orange’ in Box 1A&B) and their
148 allosteric regulation (‘green’ and ‘red’ arrows in Box 1B) in the model. To successfully
149 switch flux directions, the cell needs to express irreversible enzymes in the new direction,
150 up-regulate their activity and repress enzyme activity in the opposing direction.

151

152



Box 1 Integrated kinetic model of central carbon metabolism. (A) Detailed metabolic reaction network and (B) minimal network of central carbon metabolism. Coarse-graining was done by combining irreversible glycolytic (orange) and gluconeogenic reactions (blue), as well as metabolites. Influx can either occur from glycolytic carbon sources (e.g. glucose) or tricarboxylic acid (TCA) cycle carbon sources (e.g. acetate). (1) Gatekeepers to the central section of glycolysis and gluconeogenesis are the two irreversible reactions (gly^{up}, gng^{up} and gly^{low}, gng^{low}) that feed and drain FBP and PEP. The irreversible reactions are allosterically regulated by FBP (Fructose 1-6-bisphosphate) and PEP (phosphoenolpyruvate), where 'outward' facing reactions are activated (green arrows) and 'inward' facing reactions are repressed (red arrow). (2) Biomass production requires precursors from glycolytic carbons, PEP and TCA cycle carbon. (3) Glycolytic and gluconeogenic enzymes are regulated by Cra, which is in turn modulated by FBP. (C) Mathematical formulation of the model. Numbers correspond to features in panel B. (1) Fluxes r_i of enzymes i depend on enzyme abundances ϕ_i , catalytic rates $k_{cat,i}$ and allosteric regulations, modeled as a Hill function below its maximal saturation $(c_j/c_j^)^{\alpha_i}$, where c_j is the concentration of the regulatory metabolite and c_j^* is a reference concentration. Reversible fluxes are modeled with simple mass action kinetics. (2) Biomass production is implemented in the model as single reaction that drains all three metabolites simultaneously at catalytic rate $k_{cat,BM}$. (3) Enzyme expression depend linearly on FBP concentration c_{FBP} . Growth rate: μ , steady state abundance: ϕ_i^* , steady state concentration c_{FBP}^* and x_i & x_j modulate the sensitivity of regulation to FBP. Glycolytic and gluconeogenic enzymes are produced as part of protein synthesis. Thus in the model, flux through metabolism automatically leads to synthesis of metabolic enzymes and biomass production, resulting in dilution of existing enzymes.*

153 The metabolites ‘sandwiched’ between the irreversible reactions are coarse-grained into
154 the first and last metabolites of the series of reversible reactions connecting the irreversible
155 reactions, FBP and PEP (phosphoenolpyruvate). These metabolites regulate the activity
156 and expression of the irreversible enzymes (Box 1B and SI Sec. 2).

157

158 In total, the model encompasses four irreversible reactions, each regulated allosterically by
159 either FBP or PEP, and transcriptionally by FBP via Cra, and one reversible reaction that
160 connects FBP and PEP. We used measured metabolite concentrations for growth on
161 glucose (Kochanowski et al., 2013a) and Michaelis constants (Berman and Cohn, 1970;
162 Zheng and Kemp, 1995; Donahue et al., 2000) to constrain enzymatic parameters and
163 biomass yield (Link et al., 2008) and density (Basan et al., 2015b) on glucose to constrain
164 fluxes (SI Sec. 4). We used the level of futile cycling in the upper and lower reactions in
165 exponential glucose growth, which summarize the effect of enzyme abundance and
166 allosteric regulation, as fitting parameters such that the model reproduces the observed lag
167 times in this paper; see SI Sec. 4.2 for details.

168

169 While the model in Box 1 was formulated to coarse-grain glycolysis via the Embden-
170 Meyerhof-Parnas (EMP) pathway, other glycolytic pathways, such as the Entner-
171 Doudoroff (ED) pathway, have a similar topology. In ED glycolysis, phosphogluconate
172 dehydratase (Edd) and KDPG aldolase (Eda) are irreversible reactions that feed into the
173 chain of reversible reactions, analogous to 6-phosphofructokinase (pfk) in the EMP
174 pathway. The coarse-grained model thus should capture these alternative pathways too.

175

176 *Central carbon metabolism self-organizes in response to substrate availability*

177 To test whether this simple model could recapitulate steady state glycolytic and
178 gluconeogenic growth conditions, we compared it to published metabolite and proteomics
179 data of *E. coli*, which is well-characterized in steady state exponential growth on glucose
180 and acetate as sole carbon substrates (Basan et al., 2020). Indeed, the model reached distinct
181 steady states for glycolytic and gluconeogenic conditions, which we summarized
182 graphically with font size indicating enzyme and metabolite abundance and line widths
183 indicating the magnitude of fluxes (Fig. 1A&B). Active regulation is shown in colored

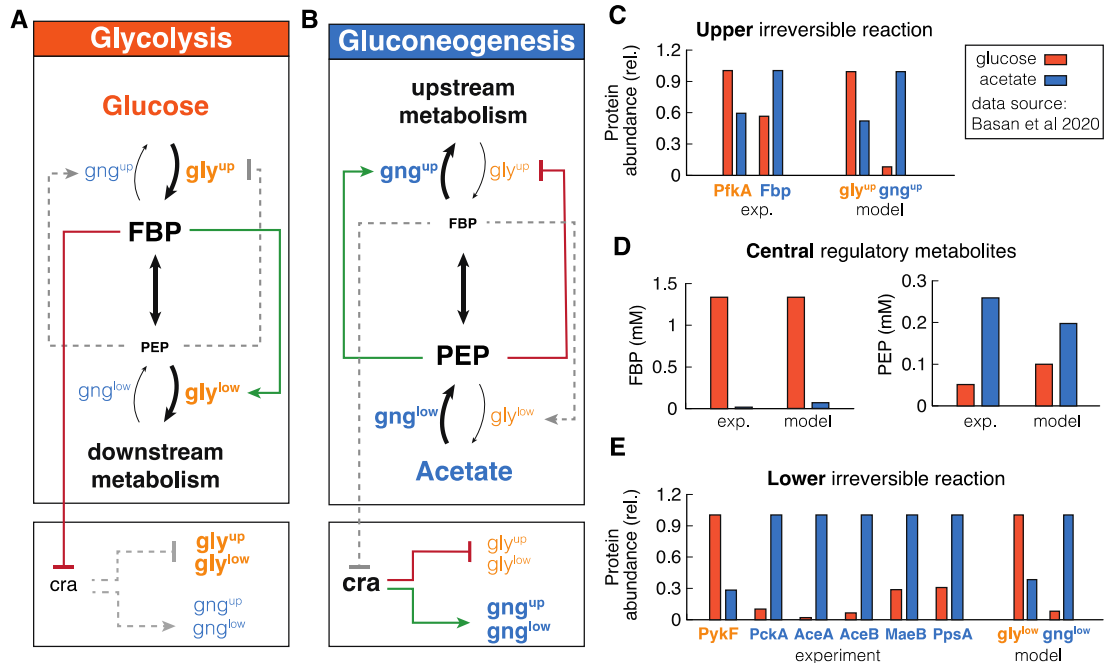


Figure 1 Self-organization of metabolism in glycolysis and gluconeogenesis. (A&B) Graphic summary of the reorganization in glycolysis and gluconeogenesis. Linewidth of reactions arrows indicate magnitude of flux. Font size of metabolites and enzymes indicate metabolite concentrations and enzyme abundances, respectively. Active regulation is indicated by red/green color, inactive regulation is grey and dashed. (C, D&E) Comparison of theoretical and experimental (from (Basan et al., 2020)) metabolite concentrations and enzyme abundances. Note the striking, differential regulation of FBP and PEP, high in one condition and low in the other.

184 lines, while inactive regulation are grey, dashed lines. We quantitatively compare enzyme
 185 and metabolite abundances to experimental measurements in Fig. 1C-E and find that the
 186 coarse-grained model can describe the reorganization of metabolism well, despite the
 187 simplifications of the metabolic and regulatory networks.

188

189 The simulation helps to understand how central metabolism self-organizes in glycolytic
 190 and gluconeogenic conditions and how allosteric and transcriptional regulation optimize
 191 fluxes and minimize futile cycling during exponential growth. As shown in Fig. 1C, in
 192 ‘orange’, during glycolytic conditions, the simulation reached a steady state with high FBP
 193 levels and low PEP levels. As illustrated in Fig. 1A, the high FBP pool activates lower
 194 glycolysis, while the low PEP pool derepresses upper glycolysis and deactivates upper
 195 gluconeogenesis. This suppression of gluconeogenic fluxes in glycolysis reduces futile
 196 cycling, i.e., circular fluxes at the irreversible reactions, thereby streamlining metabolism.

197 On a transcriptional level, the high FBP pool represses Cra, which in turn derepresses the
198 expression of glycolytic enzymes and inhibits the expression of gluconeogenic enzymes.
199 This results in high levels of glycolytic enzymes and low levels of gluconeogenic enzymes
200 in the simulation (Fig. 1D&E, right panels).

201

202 In gluconeogenic conditions ('blue' in Fig. 1), we find precisely the complementary
203 configuration of central carbon metabolism. Simulation and experiments show low FBP
204 and high PEP pools (Fig. 1C). As illustrated in Fig. 1B, high PEP represses upper glycolysis
205 and activates upper gluconeogenesis, while low FBP deactivates lower glycolysis. Low
206 FBP also derepresses Cra, which leads to high expression of gluconeogenic enzymes and
207 low expression of glycolytic enzymes (Fig. 1D, right panels).

208

209 Next we tested if the model could recapitulate how varying growth rates on glycolytic and
210 gluconeogenic nutrients affects metabolite levels and protein expression in *E. coli* (Gerosa
211 et al., 2015b; Hui et al., 2015). In particular, it has been shown experimentally that FBP
212 acts like a flux sensor and FBP concentration linearly increases with glycolytic flux (Fig.
213 S1A) (Kochanowski et al., 2013b), which is recapitulated by our simulation (Fig. S1D),
214 under the condition that the speed of the reversible reaction is slow compared to the
215 irreversible reactions. The linear increase of FBP concentration with growth rate results in
216 a linear growth rate dependence of gluconeogenic and glycolytic enzyme abundances in
217 the simulation, in good agreement with experimental measurements of enzyme abundances
218 from proteomics (Fig. S1 compare B&C with E&F) (Hui et al., 2015). Together, these
219 results show that integrating the transcriptional and allosteric regulation of FBP and PEP
220 in the coarse-grained model suffices to describe the major re-configuration of central
221 metabolism in glycolysis and gluconeogenesis.

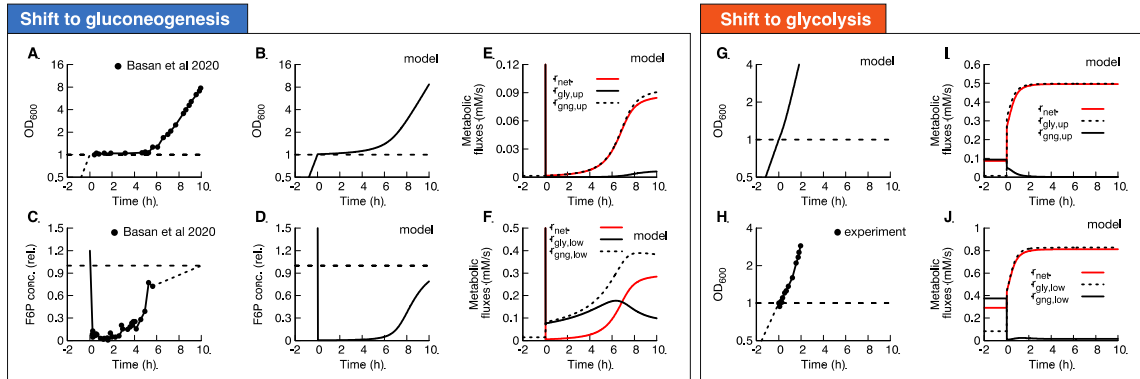


Figure 2 Shifts between glycolysis and gluconeogenesis. (A) Experimental and (B) model of optical density after shift of *E. coli* from glucose to acetate. Growth shows a substantial lag before it recovers. (C) Experimental and (D) model of F6P (normalized to the final state) collapses after shift to acetate, and continues to stay low throughout lag phase. Because F6P is an essential precursor for biomass production, this limitation effectively stops biomass growth. (E&F) Fluxes of all irreversible reactions in units of intracellular concentration per time. Especially fluxes in lower glycolysis/gluconeogenesis are of equal magnitude, leading to a futile cycle, where no net flux (red line) through central carbon metabolism can be established. (G-J) Optical density and metabolic fluxes for the reversed shift from acetate to glucose shows immediate growth and no intermittent futile cycling. The dynamics of all enzyme abundances, regulation and fluxes for both shifts are shown in Fig. S2-6 in detail. The model also correctly predicts that enzyme abundances only adapt late in the lag phase (Fig. S7).

222

223 Central carbon metabolism of *E. coli* is primed for switches to glycolysis

224 Equipped with this model, we next address the mechanistic basis for the extended lag
 225 phases of *E. coli* upon nutrient shifts from glycolytic to gluconeogenic conditions. When
 226 shifted from glucose to acetate *E. coli* shows a lag time with almost no growth for around
 227 5h (Fig. 2A, data: (Basan et al., 2020)). We can reproduce this lag with our model (Fig. 2B,
 228 Fig. S2-5) when we fit pre-shift futile cycling, which is a measure for enzyme abundances
 229 and allosteric regulations; see SI Sec. 4.2 for details. All model solutions for *E. coli* shown
 230 in this paper are generated with the parameters generated from this fit. The model captures
 231 the slow adaptation of glycolytic and gluconeogenic enzymes, the major change of which
 232 occurs only towards the end of the lag phase (Fig. S7). Investigating the origin of the
 233 growth arrest in the simulation, we found that during lag phase, the concentrations of upper
 234 glycolytic precursors (which includes Fructose 6-phosphate (F6P) and Glucose 6-
 235 phosphate (G6P)) remained very low compared to their steady state values, which matches
 236 published experimental evidence of F6P measurements (Basan et al., 2020) (Fig.

237 simulation: 2C, data 2D). This indicates that essential precursors are limited, and thereby,
238 according to Eq. (4) growth rate during lag phase stalls.

239

240 In the simulation, the F6P limitation is caused by low net fluxes in upper and lower
241 gluconeogenesis (Fig. 2E&F, red lines). Previously, it was suggested that futile cycling
242 between gluconeogenic and glycolytic enzymes could contribute to this flux limitation
243 (Basan et al., 2020), supported by the observation that overexpression of glycolytic
244 enzymes in upper or lower glycolysis strongly impaired switching and resulted in much
245 longer lag times (Basan et al., 2020). The simulation allows us to probe the effect of futile
246 cycling *in silico*, which cannot be directly measured experimentally. Indeed, we found for
247 our default *E. coli* parameters that residual lower glycolytic flux almost completely
248 canceled the flux from gluconeogenesis, i.e., $r_{\text{gly}}^{\text{low}} \approx r_{\text{gng}}^{\text{low}}$ (solid and dashed black lines in
249 Fig. 3F), such that net gluconeogenic flux remained close to zero (red line, Fig. 2E&F).
250 Thus, this futile cycling appears to be the main reason for limiting net flux throughout the
251 lag phase.

252

253 The biochemical network and regulation are almost completely symmetric with respect to
254 the direction of flux, so one might naively expect a shift from gluconeogenesis to glycolysis
255 to also result in a long lag. However, experimentally the shift in the opposite direction from
256 gluconeogenesis to glycolysis occurs very quickly in *E. coli* (Fig. 2G) (Basan et al., 2020).
257 Our simulations with the standard *E. coli* parameters can recapitulate that central
258 metabolism adjusted very quickly and growth resumed without a substantial lag phase (Fig.
259 2H). In striking contrast to the shift to gluconeogenesis, futile cycling played no role in the
260 shift to glycolysis, because both upper and lower glycolytic fluxes got repressed
261 immediately after the shift (Fig. 2I-J, solid black line), such that net flux could build up
262 (Fig. 2I-J, red line). The absence of transient futile cycling, despite the symmetry of
263 regulation and metabolic reactions, means that it must be the allosteric and transcriptional
264 regulations that ‘prime’ central metabolism of *E. coli* for the glycolytic direction.

265

266 *Molecular cause of preferential directionality*

267 To understand the molecular cause of the asymmetric response and lag phases, we
268 investigated the role of allosteric and transcriptional regulation in our simulation. During
269 steady state growth, the differential regulation during glycolysis and gluconeogenesis is
270 achieved by PEP and FBP, the metabolites that are “sandwiched” between the two
271 irreversible reactions and connected by a series of reversible enzymes, coarse-grained in
272 our model into the ‘super-eno’ enzyme. First, we focused on regulation during exponential
273 growth and wanted to investigate how the cell achieves differential regulation of glycolytic
274 and gluconeogenic enzymes using the metabolites FBP and PEP. In equilibrium, forward
275 and backward reactions would balance, i.e., $r_{\text{ENO}+} = r_{\text{ENO}-}$, and no net flux could run
276 through central metabolism, meaning that the cell could not grow. Using Eqs. (2&3), the
277 balance of forward and backward fluxes results in a fixed quadratic dependence of FBP
278 and PEP in equilibrium,

$$c_{\text{FBP}}^{\text{eq}} = k_{\text{ENO}-} / k_{\text{ENO}+} (c_{\text{PEP}}^{\text{eq}})^2. \quad (7)$$

279
280 Close to the equilibrium, FBP and PEP levels go up and down together, rather than the
281 opposing directions, as observed for glycolytic and gluconeogenic growth (Fig. 1A&B).
282 This results in low net flux and very slow growth. Hence, for steady state growth, the
283 equilibrium must be broken and $\text{FBP} \gg \text{PEP}$ or $\text{FBP} \ll \text{PEP}$, such that either glycolytic
284 flux is bigger than gluconeogenic or vice-versa ($r_{\text{ENO}+} \gg r_{\text{ENO}-}$ and $r_{\text{ENO}+} \ll r_{\text{ENO}-}$,
285 respectively). This is achieved by the irreversible reactions, which drain and supply
286 metabolites to the ‘super-eno’. Because of the positive feedback between enzyme activity
287 and non-equilibrium of the ‘super-eno’, this regulation topology achieves differential
288 regulation during glycolysis and gluconeogenesis. As we observed in the analysis of the
289 glycolytic and gluconeogenic steady states (Fig. 1), this differential regulation adjusts
290 enzyme levels via transcriptional regulation and suppresses futile cycling at the irreversible
291 reactions.
292

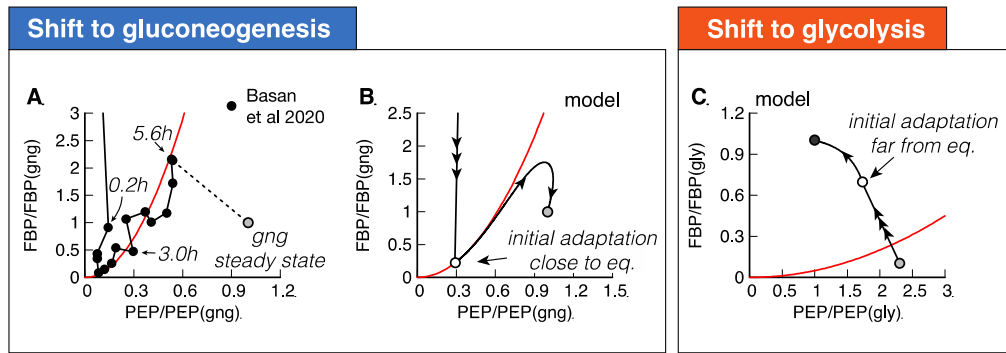


Figure 3 Molecular cause for asymmetric recovery dynamics in E. coli. (A) Recovery of FBP and PEP of after a shift from glucose to acetate, shows a distinctive joint increase, followed by an overshoot of FBP. Data from Ref. [4]. Red line is a quadratic guide to the eye. Final acetate steady state is drawn as grey symbol and used to normalize both FBP and PEP levels. (B) Model solution of FBP and PEP. After the fast collapse of metabolite levels (triple arrow to white circle), the dynamics closely follows the quadratic FBP-PEP equilibrium Eq. (7). Eventually recovery will diverge away from the equilibrium line, towards the non-equilibrium steady states of gluconeogenesis (grey circle) (C) For a shift to glycolysis, metabolite levels do not collapse, but instead land already far from equilibrium (triple arrow to white circle), such that flux is immediately established, and recovery is quick.

293 While regulation of central metabolism efficiently organizes FBP-PEP in a far from
 294 equilibrium state during exponential growth, nutrient shifts expose the limitations of this
 295 regulatory system. To understand why, we plot FBP against PEP, with both metabolites
 296 normalized to their gluconeogenic steady state (Fig. 3A). We indicated several time-points
 297 along the dynamics, and the final steady state is shown with a grey symbol. Initially, both
 298 FBP and PEP drop close to zero, followed by a very slow joint increase of FBP and PEP
 299 over the course of hours (Fig. 3A). This joint increase, rather than a differential increase,
 300 is the hallmark of a close-to-equilibrium state.

301

302 The slow recovery can be understood from the simulation, which shows that FBP and PEP
 303 proceed close to the equilibrium line of Eq. (7), where growth is slow (Fig. 3B). As a guide
 304 to the eye, we drew an equilibrium parabola in Fig. 3A along the joint increase, too.

305

306 We previously showed that throughout most of the lag phase, higher gluconeogenic flux
 307 from increasing levels of gluconeogenic enzymes is almost completely lost to a
 308 corresponding increase in futile cycling because increasing FBP activates lower glycolysis,
 309 instead of deactivating it (Fig. 2F). The overshoot of FBP in Fig. 3A (data) and Fig. 3B

310 (model) is what finally allows the cell to establish net flux because it is breaking the
311 equilibrium: PEP concentration is high enough to activate upper gluconeogenesis
312 sufficiently to drain FBP via upper gluconeogenesis (see Fig. 2E). Lower FBP then shuts
313 down futile cycling in lower glycolysis/gluconeogenesis (Fig. 2F), pushing FBP and PEP
314 concentrations to a state far from the equilibrium line (see Fig. 3B) and allowing the cell
315 to grow at a faster rate.

316

317 The fundamental difference between shifts to gluconeogenesis and glycolysis in *E. coli* is
318 that glycolytic shifts immediately land far from equilibrium (Fig. 3C, triple arrow to white
319 circle), such that cells immediately grow at faster rates, allowing them to express the new
320 enzymes needed to recover quickly. But why does one direction immediately land far from
321 equilibrium, while the other lands close to equilibrium?

322

323 *Three trade-offs constrain lag times to glycolysis and gluconeogenesis*

324 The out-of-equilibrium state is caused by net flux going through metabolism. Therefore,
325 we investigated what causes fluxes not to flow in a uniform direction after shifts to
326 glycolysis and gluconeogenesis. In principle, metabolite flux brought to the ‘super-eno’
327 can exit via two drains: upper gluconeogenesis, activated by PEP, and lower glycolysis,
328 activated by FBP (Fig. 4A). How much flux exits via either drain depends on the current
329 protein abundances and the allosteric regulation. If the allosteric regulation and protein
330 abundances favor the lower drain, then after a switch to glycolysis, FBP builds up, PEP is
331 drained and a net flux is immediately accomplished. In a shift to gluconeogenesis, however,
332 flux that enters central metabolism from the TCA cycle will immediately drain back to the
333 TCA cycle, leading to an in-and-out flux but no net flux. In this situation, FBP and PEP
334 stay in equilibrium and the recovery stalls. If on the other hand, the upper drain was favored
335 over the lower drain, then we would expect the behavior to be reversed and gluconeogenic
336 flux would be immediately accomplished, while the glycolytic recovery would stall.

337

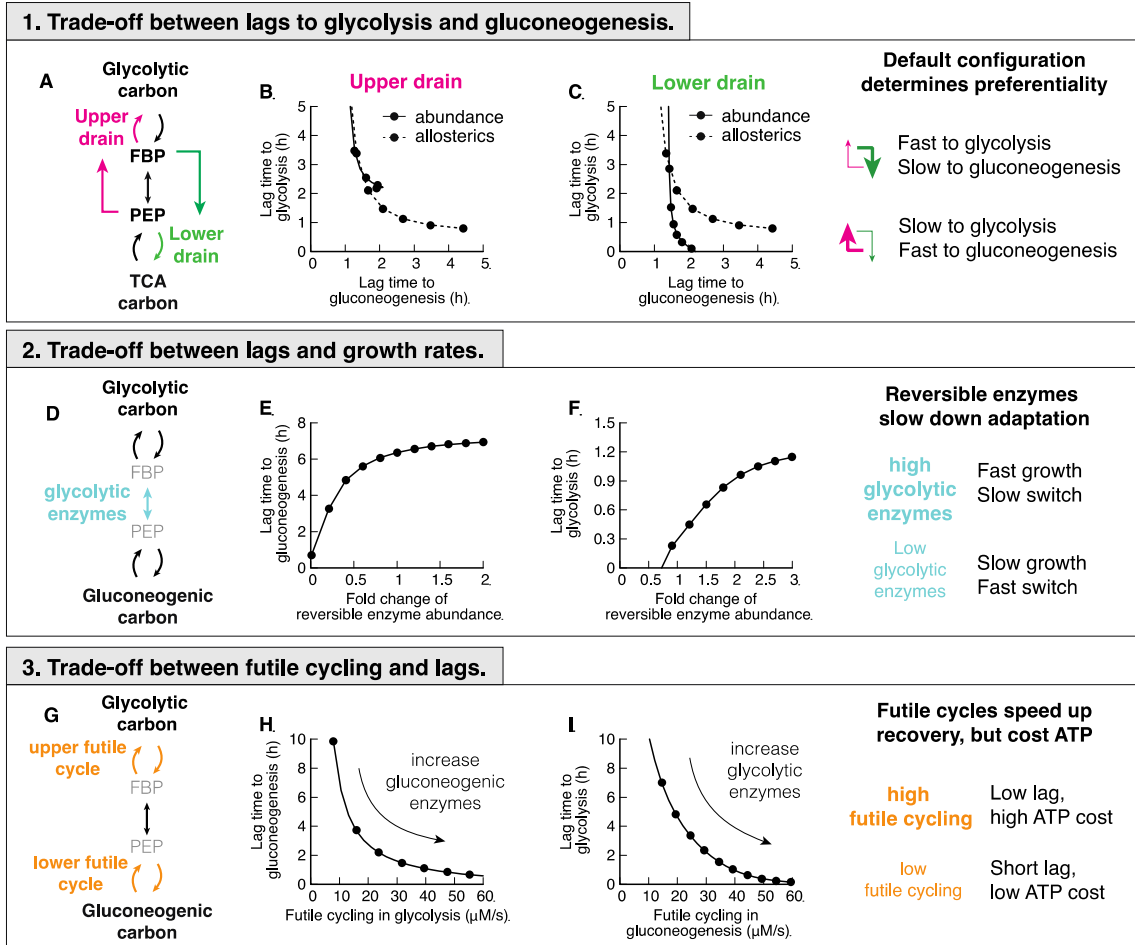


Figure 4 Trade-offs between glycolysis and gluconeogenesis. (A) Two drains in central metabolism deplete central metabolites. (B-C) Changing abundance ϕ or allosteric regulation strength α in either lower or upper drain leads to a shift of lag times, decreasing lags in one direction at the cost of the other. Choosing strength of the drains such that either top or bottom is stronger, will lead to a fast recovery in one direction, and a slow in the other. (D) Reversible enzymes in the central metabolism (coarse-grained here into ‘super-eno’). Abundance of reversible enzymes scale linearly with growth rate [16]. (E-F) Decreasing abundance of reversible enzymes decreases lag times. This effect is due to regulatory metabolites being in a far-from-equilibrium state when abundances are low, which allows differential regulation via FBP and PEP. For high abundance, regulation is weak and lag times long. (G) There are two futile cycles in central metabolism. (H-I) Increasing abundance of enzymes of the opposing direction in pre-shift, e.g. gluconeogenic enzymes in glycolytic growth, increases futile cycling and decreases lag times. Because in futile cycles free energy is dissipated, usually in the form of ATP hydrolysis, futile cycling has an energetic cost.

338 In the simulation, we are able to test the hypothesis that the upper and lower drains
 339 determines the preferential directionality of the central metabolism by varying enzyme
 340 abundances and the strength of allosteric interactions in upper and lower drains *in silico*.
 341 We let metabolism adapt to gluconeogenic and glycolytic conditions and calculate lag

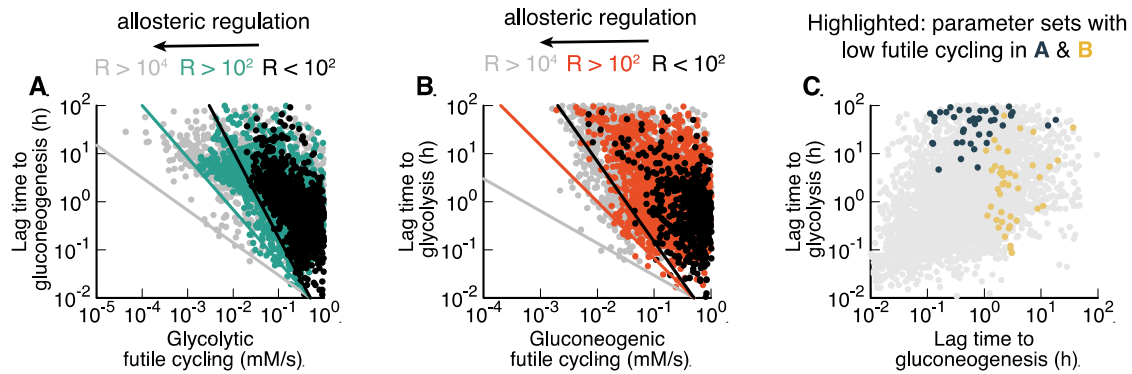


Figure 5 Large-scale parameter scan reveals Pareto optimality between lag times and futile cycling. (A-B) Model calculated for randomized sets of protein abundancies, reaction rates, Michaelis constants, allosteric interactions, transcriptional regulation, see SI. Each point corresponds to a parameter set that allows exponential growth on both glycolytic and gluconeogenic carbons, as well switching between both conditions. Data is colored according to the total regulation R , i.e., the sum of fold-changes of enzyme activities between glycolysis and gluconeogenesis, $(c_i^{gly}/c_i^{gnb})^{\alpha_i}$, where c_i^{gly} and c_i^{gnb} are protein abundancies in glycolysis and gluconeogenesis of protein i and α_i the strength of the allosteric regulation. For standard *E. coli* parameters $R = 23$. $R > 10^4$ are likely unphysiological. Lines indicate Pareto front and are drawn by hand. (C) Parameter sets from panels A&B with low futile cycling highlighted over the background of all parameter sets (grey).

342 times (Fig. 4B&C). Indeed, we found that a decrease of lag time in one direction led to an
 343 increase of lag time in the opposite direction.

344

345 Varying the outflow from metabolism is not the only determinant of lag times. The set of
 346 reversible enzymes, coarse-grained in our model into the ‘super-eno’, plays another key
 347 role because it interconverts the regulatory metabolites FBP and PEP (Fig. 4D). If this
 348 conversion is fast, the concentrations of FBP and PEP will be close to their equilibrium
 349 relation in Eq. (7), and differential regulation will be impossible. As a result, lag times in
 350 both directions increase if we increase the abundance of reversible reactions (Fig. 4E-F).
 351 This is a counter-intuitive result, as one would have naïvely expected more enzymes to
 352 speed up reactions. But instead, in metabolism more enzymes will collapse the differential
 353 regulation and slow down adaptation rates. This trade-off is unavoidable for fast growing
 354 cells because the cell needs a sufficient amount of reversible glycolytic enzymes to catalyze
 355 metabolic flux.

356

357 Finally, lag times depend on the amount of futile cycling, i.e., the circular conversion of
358 metabolites in the upper and lower irreversible reactions (Fig. 4G). Increasing the
359 abundance of gluconeogenic enzymes in glycolytic growth or glycolytic enzymes in
360 gluconeogenic growth increases futile cycling but decreases lag times (Fig. 4I&H).
361 Because futile cycling dissipates ATP, which is not explicitly built into our model, this
362 third trade-off means that organisms can decrease their switching times by sacrificing
363 energetic efficiency.

364

365 Are these three trade-offs a fundamental consequence of the regulatory structure or are
366 there parameter combinations that avoid the trade-offs by simultaneously enabling rapid
367 growth and rapid switching without costly futile cycling? To answer this question we
368 performed an extensive scan of model parameters by randomly choosing sets of
369 biochemical parameters and simulating the resulting model. Of those parameter sets we
370 chose those that allowed steady state growth in both glycolytic and gluconeogenic
371 conditions and were able to switch between both states. We plotted the sum of futile cycling
372 in the upper and lower irreversible reactions in the pre-shift conditions against the
373 subsequent lag times for shifts to gluconeogenesis (Fig. 6A) and to glycolysis (Fig. 6B). In
374 addition, we colored individual parameter sets according to the total allosteric regulation,
375 defined as the sum of fold-changes of enzyme activities between glycolysis and
376 gluconeogenesis (black: $R < 10^2$, red/green: $10^4 > R > 10^2$, grey: $R > 10^4$). These fold
377 changes are the result of both allosteric and transcriptional variations. We found that
378 metabolism in the majority of randomly generated models is inefficient and dominated by
379 futile cycling; only a minority of models were able to reduce futile cycling in glycolysis
380 and gluconeogenesis. Remarkably, despite probing variations of all possible model
381 parameters, including Michaelis Menten parameters of enzymes and the strengths of
382 allosteric and transcriptional regulation, lag times could not be reduced at-will by the cell.
383 Instead, individual parameter sets with similar allosteric regulation (colors) are bound by a
384 ‘Pareto frontier’ (solid lines) between futile cycling in preshift conditions and lag times.
385 Points close to the ‘Pareto frontier’ are Pareto-optimal, meaning that any further decrease
386 of either parameter must come at the expense of the other. Overall, stronger allosteric
387 regulation shifted the Pareto frontier but was not able to overcome it. Parameter

388 combinations that led to low futile cycling in either glycolysis or gluconeogenesis showed
389 long lag times in at least one condition (Fig. 5C, ‘black’ and ‘yellow’) compared to the
390 background of all simulated parameter sets (‘grey’). Thus, from this analysis, it seems that
391 organisms with the regulatory architecture of Box 1 cannot overcome long lag times
392 without paying a futile cycling cost during steady state growth.

393

394 *Gluconeogenesis specialists are constrained by the same trade-offs*

395 Taken together, the results of Fig. 4&5 suggest that microbial cells cannot achieve fast
396 growth, low futile cycling and fast adaptation simultaneously in both glycolysis and
397 gluconeogenesis. Instead, trade-offs between these six extremes constrain the evolutionary
398 optimization of microbial metabolism, such that any optimal solution is on a surface of a
399 multidimensional Pareto frontier, where any improvement in one phenotype will come at
400 the expense of others. To test this hypothesis, we next asked whether a gluconeogenic
401 specialist would indeed be constrained by the same trade-offs as *E. coli* and other glycolytic
402 specialists. For this purpose we chose *P. aeruginosa*, a well-studied gluconeogenesis
403 specialist that has a similar maximal growth rate in minimal medium as *E. coli* (*E. coli*
404 0.9/h on glucose, *P.aeruginosa* 1.0/h on malate) and grows on a wide variety of substrates.

405

406 Strikingly, *P. aeruginosa* grows fast on gluconeogenic substrates that are considered ‘poor’
407 substrates for *E. coli*, but slow on glycolytic substrates that are considered ‘good’ (Fig. 6A).
408 From our model, we would expect that such a specialization for gluconeogenic substrates
409 would go along with a reversal in lag phases, too. Indeed, switching between glycolytic
410 and gluconeogenic substrates, *P. aeruginosa* exhibits a mirrored pattern of lag phases
411 compared to *E. coli* (compare Fig. 6B to 6C), with a long multi-hour lag phase when
412 switched to glycolysis.

413

414 To investigate if both *E. coli* and *P. aeruginosa* are constrained by the same trade-offs, we
415 investigated the effect of pre-shift growth rate, which according to Fig. 4 should have a
416 negative effect on growth rates. For *E. coli* it is known that shifts from glycolysis to
417 gluconeogenesis depend on the pre-shift growth rate (Fig. 6D, data: (Basan et al., 2020)),
418 which we can capture in our model if we take FBP-dependent transcriptional regulation

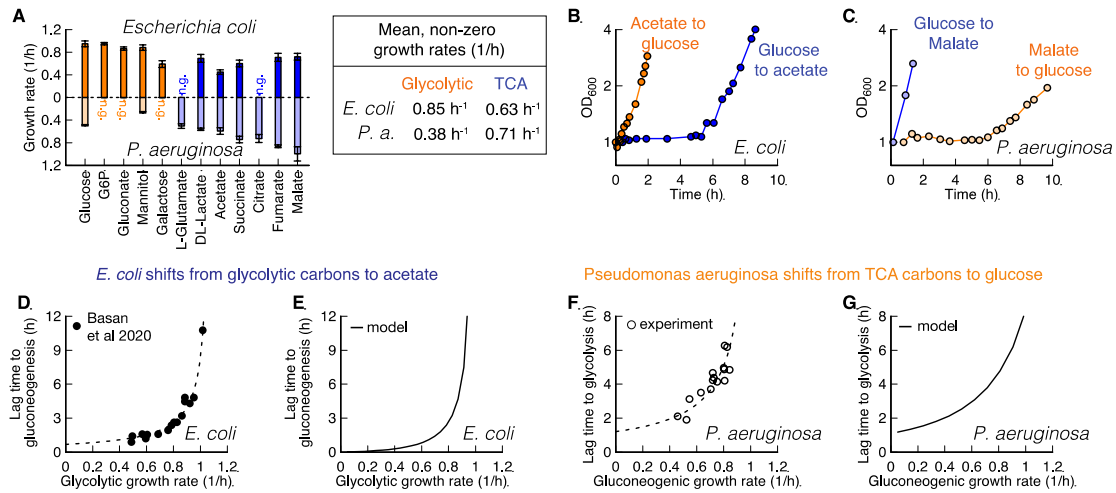


Figure 6 Comparison of *E. coli* and *P. aeruginosa* during growth and shifts. (A) Growth rates on glycolytic carbons (orange) are faster for *E. coli* than on gluconeogenic carbons (blue). For *Pseudomonas*, this dependence is reversed. No growth indicated with “n.g.”. (B-C) Shifts for *E. coli* and *P. aeruginosa* between glycolytic and gluconeogenic carbon substrates. The preferential order of *P. aeruginosa* is reversed in comparison to *E. coli* (D) *E. coli* shows an increase of lag times to gluconeogenesis with increasing pre-shift growth rate. Lag times diverge around growth rate 1.1/h. (E) The model predicts diverging growth rates without further fitting, based on the growth rate dependent expression levels of glycolytic and gluconeogenic enzymes (Fig. 2E-F). (F) *P. aeruginosa* shows a strikingly similar growth rate to lag time dependence as *E. coli*, when switched to glycolysis, with lag times diverging around 1.0/h. (G) The model can recapitulate observed *P. aeruginosa* lag times if pre-shift glycolytic enzymes are decreased as a function of pre-shift growth rate.

419 into account (Fig. 6E). We tested the corresponding lag times for *P. aeruginosa* by varying
 420 gluconeogenic substrates and found a similar dependency in shifts to glycolytic substrates
 421 (Fig. 6F&G). Hence as expected from the model, these findings show that *P. aeruginosa*
 422 is constrained by the same trade-offs as *E. coli*.

423

424 To decipher whether *P. aeruginosa* lag times are constrained on a molecular level by the
 425 same inability to break the equilibrium after nutrient shifts, we investigated metabolite
 426 concentration dynamics in central metabolism. Because *P. aeruginosa* uses the ED
 427 pathway for hexose catabolism (Wang et al., 1959; Vicente and Cánovas, 1973), we needed
 428 to adapt our model slightly. The irreversible reactions in the ED pathway convert
 429 gluconate-6-phosphate to glyceraldehyde 3-phosphate (GAP) and pyruvate. In the
 430 reversible chain of reactions, the first metabolite in glycolysis is thus GAP rather than FBP.

Pseudomonas aeruginosa

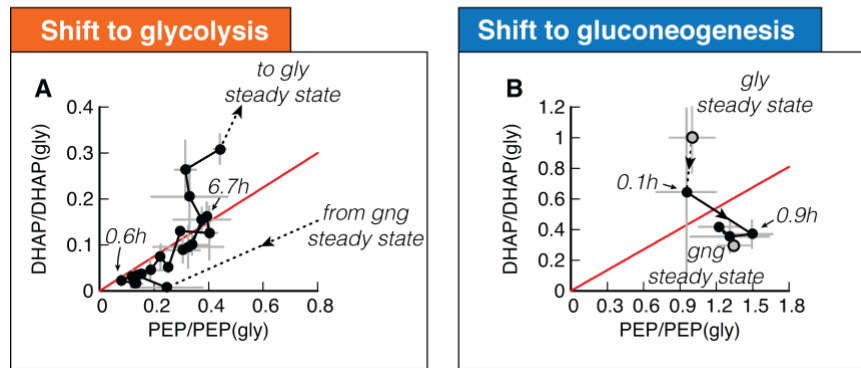


Figure 7 Metabolite dynamics of *P. aeruginosa* during shifts from malate to glucose and vice-versa. (A) DHAP and PEP during shift from malate ('gng') to glucose ('gly'), normalized to the final glycolytic steady state. Recovery follows a direct proportionality, indicating that central metabolism is close to equilibrium (red line) during the recovery. (B) DHAP and PEP reach the final steady state ('gng') without creeping along the equilibrium line.

431 Because GAP is difficult to quantify in mass spec-based metabolomics, we used the closely
 432 related compound dihydroxyacetone phosphate (DHAP) as a proxy. DHAP is in chemical
 433 equilibrium with GAP via a single fast and reversible isomerase (Nikel et al., 2015).

434

435 Analogous to Fig. 3, we plot the dynamics of DHAP versus PEP, normalized to their
 436 glycolytic steady state values, for both shifts (Fig. 7A&B). The dynamics starts and ends
 437 at their respective steady states (grey symbols and dashed lines) and follows the direction
 438 of the indicated arrow. In the chemical equilibrium, DHAP depends linearly on PEP,

439 $c_{\text{DHAP}}^{\text{eq}} = k_{\text{ENO-}}/k_{\text{ENO+}} c_{\text{PEP}}^{\text{eq}}$, analogous to Eq. (7), but without the square because of the

440 1-to-1 stoichiometry between DHAP and PEP. This equilibrium is indicated with a red line.

441 During the long lag time of *P. aeruginosa* in a shift from malate to glucose, we see that

442 initially both DHAP and PEP collapse, followed by a slow increase along the equilibrium

443 line (Fig. 7A). Thus, despite substantial amounts of metabolites being built-up, 'super-eno'

444 remains close to equilibrium. Only after 5.6 h, when the DHAP-PEP dynamics deviates

445 from the line, the equilibrium is broken and net flux can be achieved.

446

447 In the reverse shift from glucose to malate, *P. aeruginosa*, in contrast, can immediately

448 establish a non-equilibrium and grow. Thus not only is the asymmetry in lag times reversed

449 compared to *E. coli*, it is also caused by the same inability to break the equilibrium and
450 establish net flux in central metabolism.

451

452 But, microbes do not have to be optimized for either direction. One such case is *P. putida*
453 with moderate lag times of about 1 to 2 h in both directions and only a slight preference for
454 gluconeogenic substrates (Fig. S8). According to the model, such a generalist strategy can
455 also be a Pareto-optimal solution of the biochemical trade-offs of Fig. 4-5, but it must come
456 at the expense of no fast recovery (Fig. 4A-C) and reduced growth because of the trade-
457 offs with reversible enzymes (Fig. 4D-F) and futile cycling (Fig. 4G-I). This is indeed the
458 case for *P. putida*. Lag times in the fast direction are twice as long compared to *P.*
459 *aeruginosa* and the growth rate is about 20% slower (Fig. S8).

460

461 **Discussion**

462 In this work, we presented a coarse-grained kinetic model of central carbon metabolism,
463 combining key allosteric and transcriptional regulation, as well as biomass production,
464 enzyme synthesis, and growth. This model elucidates the remarkable capacity of central
465 carbon metabolism to self-organize in response to substrate availability and flux
466 requirements. During exponential growth, regulatory metabolites adjust to far-from-
467 equilibrium steady states, providing the cell with an elegant mechanism to sense the required
468 directionality of the flux. But the model reveals a key limitation of this flux sensing. Because
469 after a nutrient shift the concentration of the metabolites collapses to its equilibrium, the
470 cell becomes ‘blind’ to the direction that the flux is supposed to flow through the system.
471 By implementing a preferred direction, the cell can partially overcome lag times in one
472 direction at the cost of increasing lag times in the opposite direction. In addition, two more
473 trade-offs constrain the ability to simultaneously decrease both lag times, because it
474 impacts growth rate and the level of futile cycling during growth.

475

476 Microbial species can maximize their proliferation only up to the Pareto-frontier spanned
477 by these trade-offs, which can lead to evolution of substrate specialization. We validated
478 this key model prediction in different bacterial species. In *P. aeruginosa* we showed a
479 reversal of substrate preference as compared to *E. coli*, which coincided with a complete

480 reversal of the phenomenology of lag phases and metabolite dynamics. In *P. putida* we
481 found a generalist strategy with moderate lag times in both direction.

482

483 One of the results from our model is that lag times could be substantially reduced by
484 allowing futile cycling, e.g., by expressing irreversible enzymes for both directions at all
485 times. The energetic cost of such a wasteful strategy would be relatively low. Because
486 energy production pathways only constitute a relatively small fraction (around 20%) of the
487 total cellular proteome, the cell could compensate ATP dissipated in futile cycling by
488 increasing ATP production at a relatively low proteome cost. However, experimentally it
489 appears that *E. coli* chooses to keep futile cycling in check by transcriptionally regulating
490 irreversible enzymes. We thus hypothesize that the cost of futile cycling must be
491 considered in conditions where the energy budget is much more limited, such as growth
492 shifts and during starvation. In fact, it has been recently shown that the energy budget of
493 the cell is around 100-fold smaller during carbon starvation and that energy dissipation can
494 increase death rates several-fold (Schink et al., 2019). Therefore, even levels of futile
495 cycling that are modest during steady state growth should severely affect survival of cells
496 in these conditions

497

498 Our findings indicate that the identified trade-offs are inherent properties of central carbon
499 metabolism, at least given the existing allosteric and transcriptional regulation. But could
500 different regulation overcome this limitation? In principle, the cell could use a direct input
501 signal from the carbon substrate to allosterically inhibit or even degrade undesired
502 metabolic enzymes. This would uncouple enzyme abundances and activities in pre- and post-
503 shift growth and circumvent the trade-offs. But with dozens of glycolytic and
504 gluconeogenic substrates, this would result in a much higher degree of regulatory
505 complexity, quickly exceeding the regulatory signal capacity that microbes with their small
506 genomes could sense and integrate. In addition, any wrong decision to degrade or inhibit
507 metabolic enzymes, for example when combinations of nutrients are present or when
508 supply is only briefly inhibited, would drastically impair growth. Thus the regulatory
509 network that microbes use might not be maximizing growth, but at least it is robust and
510 prevents misregulation.

511

512 Another reason why no such regulation has evolved could be related to the observation that
513 the regulation of upper and lower glycolysis/gluconeogenesis and directionality of flux are
514 performed by the metabolite concentrations of FBP and PEP, which are cut off from the
515 rest of metabolism by irreversible reactions. We propose that the logic for this regulatory
516 architecture is product inhibition, which ensures that this essential part of central carbon
517 metabolism is adequately supplied with metabolites, but also ensures that uncontrolled and
518 potentially toxic accumulation of metabolites does not occur. In fact, because the reactions
519 of upper and lower glycolysis are effectively irreversible, even a slight misbalance in flux
520 between these enzymes and biomass demand would result in uncontrolled accumulation of
521 metabolites and, in the absence of a cellular overflow mechanism, these metabolites would
522 quickly reach toxic concentrations, e.g., via their osmotic activities. As demonstrated by
523 the simulation, the existing regulation of central metabolism successfully resolves this
524 problem.

525

526 The regulatory architecture of central metabolism accomplishes efficient regulation of
527 fluxes and metabolite pools in response to diverse external conditions while avoiding toxic
528 accumulation of internal metabolites and integrating multiple conflicting signals with only
529 two regulatory nodes. Central metabolism is a remarkable example of self-organization of
530 regulatory networks in biology. It provides an elegant solution to the complex, obligatory
531 problem, posed by the biochemistry of central carbon metabolism. All organisms that need
532 to switch between glycolytic and gluconeogenic flux modes face this problem, and we
533 argue that this explains the striking degree of conservation of the phenomenology of shifts
534 between glycolytic and gluconeogenic conditions that we found in different microbial
535 species, ranging from *E. coli*, *B. subtilis*, and even wild-type strains of the lower eukaryote
536 *S. cerevisiae* to the reversed phenotypes in *P. aeruginosa*. Conversely, we argue that the
537 quantitative phenotypes exhibited by microbes in such idealized growth shift experiments
538 in the lab can reveal much about their natural environments, ecology and evolutionary
539 origin.

540

541 **Acknowledgments**

542 We thank Terence Hwa for many helpful discussions and always pointing out unresolved
543 questions in microbial physiology. We thank Mark Polk for proofreading the manuscript.
544 This project was financed by MIRA grant (5R35GM137895) via MB and HFSP Long-
545 term fellowship (LT000597/2018) via SJS.

546

547 **Author contributions**

548 SJS, DC, AM, TF, US and MB contributed to the design of the project and writing the
549 manuscript. SJS, DC and MB performed modelling. AM and MB performed growth
550 experiments. VB, TF and GAB performed metabolomics measurements.

551 **Methods**

552 *Bacterial cultures*

553 Strains used in this paper are wild-type *Escherichia coli* K-12 NCM3722 (Soupene et
554 al., 2003), *Pseudomonas aeruginosa* PAO1 (Stover et al., 2000) and *Pseudomonas*
555 *putida* NIST0129. The culture medium used in this study is N⁻C⁻ minimal medium
556 (Csonka et al., 1994), containing K₂SO₄ (1 g), K₂HPO₄·3H₂O (17.7 g), KH₂PO₄ (4.7
557 g), MgSO₄·7H₂O (0.1 g) and NaCl (2.5 g) per liter. The medium was supplemented
558 with 20 mM NH₄Cl, as the nitrogen source, and either of the following carbon sources:
559 20 mM Glucose-6-phosphate, 20 mM gluconate, 0.2 % glucose, 20 mM succinate, 20
560 mM acetate, 20 mM citrate, 20 mM malate or 20 mM fumarate.

561

562 Growth was then carried out at 37 °C in a water bath shaker at 200 rpm, in silicate
563 glass tubes (Fisher Scientific) closed with plastic caps (Kim Kap). Cultures spent at
564 least 10 doublings in exponential growth in pre-shift medium. For growth shifts,
565 cultured were transferred to a filter paper and washed twice with pre-warmed post-
566 shift medium. Cells were resuspended from the filter paper in post-shift medium and
567 subsequently diluted to an OD of about 0.05.

568

569 *Preparation of metabolite samples*

570 Each metabolite sample was filtered, and the filter was immediately plunged in 4 ml
571 ice cold Methanol (40 %)+Acetonitrile (40 %)+water (20 %) and kept in 50 ml tube.
572 Bacteria were washed off from the filter by pipetting, and the solution was
573 transferred to 15 ml tube. Original 50 ml tube was further washed with 4 ml of ice

574 cold Methanol+Acetonitrile+Water mix and added to respective 15 ml tube (total 8
575 ml). Each sample was dried by speed vac, and dried extracts were sent for Mass spec
576 analysis.

577

578 *Quantification of intracellular metabolite levels*

579 The dried metabolite extracts were resuspended in 150 μ L MilliQ water, centrifuged
580 at 4 °C, 10,000 rpm for 10 min, and 100 μ L precipitate-free supernatant was
581 transferred to a master 96-well plate. 25 μ L of the master plate were transferred to a
582 96-well plate for acquisition, of which 10 μ L were injected into a Waters Acquity
583 ultraperformance liquid chromatography (UPLC) system (Waters) with a Waters
584 Acquity T3 column coupled to a Thermo TSQ Quantum Ultra triple quadrupole
585 instrument (Thermo Fisher Scientific) as described previously (Buescher et al., 2010).
586 Compound separation was achieved using a gradient of two mobile phases: A, 10 mM
587 tributylamine (ion-pairing agent), 15 mM acetate and 5% (v/v) methanol in water;
588 and B, 2-propanol. Data was acquired in negative ionization mode using previously
589 published MRM settings (Buescher et al., 2010). Peak integration was performed
590 using an in-house software based on MatLab. A dilution series of standards was used
591 to calculate the concentrations of metabolites in the samples. The final intracellular
592 concentration was calculated from the sample concentration and the extracted
593 intracellular volume.

594

595 *Theoretical modelling*

596 The integrated minimal model of metabolism and growth was implemented in
597 MATLAB using the SimBiology toolbox and is described in detail in the Supporting
598 Information.
599

600 **References**

- 601 Andreozzi, S., Miskovic, L., and Hatzimanikatis, V. (2016). iSCHRUNK – In Silico
602 Approach to Characterization and Reduction of Uncertainty in the Kinetic Models of
603 Genome-scale Metabolic Networks. *Metabolic Engineering* 33, 158–168.
- 604 Basan, M., Hui, S., Okano, H., Zhang, Z., Shen, Y., Williamson, J.R., and Hwa, T.
605 (2015a). Overflow metabolism in *Escherichia coli* results from efficient proteome
606 allocation. *Nature* 528.
- 607 Basan, M., Zhu, M., Dai, X., Warren, M., Sévin, D., Wang, Y.-P., and Hwa, T. (2015b).
608 Inflating bacterial cells by increased protein synthesis. *Mol Syst Biol* 11.
- 609 Basan, M., Hui, S., and Williamson, J.R. (2017). ArcA overexpression induces
610 fermentation and results in enhanced growth rates of *E. coli*. *Scientific Reports* 7.
- 611 Basan, M., Honda, T., Christodoulou, D., Hörl, M., Chang, Y.-F., Leoncini, E.,
612 Mukherjee, A., Okano, H., Taylor, B.R., Silverman, J.M., et al. (2020). A universal trade-
613 off between growth and lag in fluctuating environments. *Nature*.
- 614 Bennett, B.D., Kimball, E.H., Gao, M., Osterhout, R., Van Dien, S.J., and Rabinowitz,
615 J.D. (2009). Absolute metabolite concentrations and implied enzyme active site
616 occupancy in *Escherichia coli*. *Nature Chemical Biology* 5, 593–599.
- 617 Berger, S.A., and Evans, P.R. (1991). Steady state fluorescence of *Escherichia coli*
618 phosphofructokinase reveals a regulatory role for ATP. *Biochemistry* 30, 8477–8480.
- 619 Berman, K.M., and Cohn, M. (1970). Phosphoenolpyruvate Synthetase of *Escherichia*
620 *coli*. *Journal of Biological Chemistry* 245, 5309–5318.
- 621 Bordbar, A., Monk, J.M., King, Z.A., and Palsson, B.O. (2014). Constraint-based models
622 predict metabolic and associated cellular functions. *Nature Reviews Genetics* 15, 107–
623 120.
- 624 Buescher, J.M., Moco, S., Sauer, U., and Zamboni, N. (2010). Ultrahigh Performance
625 Liquid Chromatography–Tandem Mass Spectrometry Method for Fast and Robust
626 Quantification of Anionic and Aromatic Metabolites. *Anal. Chem.* 82, 4403–4412.
- 627 Buescher, J.M., Liebermeister, W., Jules, M., Uhr, M., Muntel, J., Botella, E., Hessling,
628 B., Kleijn, R.J., Chat, L.L., Lecoite, F., et al. (2012). Global Network Reorganization
629 During Dynamic Adaptations of *Bacillus subtilis* Metabolism. *Science* 335, 1099–1103.
- 630 Chakrabarti, A., Miskovic, L., Soh, K.C., and Hatzimanikatis, V. (2013). Towards kinetic
631 modeling of genome-scale metabolic networks without sacrificing stoichiometric,
632 thermodynamic and physiological constraints. *Biotechnology Journal* 8, 1043–1057.
- 633 Chassagnole, C., Noisommit-Rizzi, N., Schmid, J.W., Mauch, K., and Reuss, M. (2002).
634 Dynamic modeling of the central carbon metabolism of *Escherichia coli*. *Biotechnology*
635 *and Bioengineering* 79, 53–73.

- 636 Chubukov, V., Gerosa, L., Kochanowski, K., and Sauer, U. (2014). Coordination of
637 microbial metabolism. *Nature Reviews Microbiology* *12*, 327–340.
- 638 Donahue, J.L., Bownas, J.L., Niehaus, W.G., and Larson, T.J. (2000). Purification and
639 Characterization of glpX-Encoded Fructose 1,6-Bisphosphatase, a New Enzyme of the
640 Glycerol 3-Phosphate Regulon of Escherichia coli. *Journal of Bacteriology* *182*, 5624–
641 5627.
- 642 Fenton, A.W., and Reinhart, G.D. (2009). Disentangling the web of allosteric
643 communication in a homotetramer: heterotropic inhibition in phosphofructokinase from
644 Escherichia coli. *Biochemistry* *48*, 12323–12328.
- 645 Gerosa, L., Haverkorn van Rijsewijk, B.R.B., Christodoulou, D., Kochanowski, K.,
646 Schmidt, T.S.B., Noor, E., and Sauer, U. (2015a). Pseudo-transition Analysis Identifies
647 the Key Regulators of Dynamic Metabolic Adaptations from Steady state Data. *Cell*
648 *Systems* *1*, 270–282.
- 649 Gerosa, L., Haverkorn van Rijsewijk, B.R.B., Christodoulou, D., Kochanowski, K.,
650 Schmidt, T.S.B., Noor, E., and Sauer, U. (2015b). Pseudo-transition Analysis Identifies
651 the Key Regulators of Dynamic Metabolic Adaptations from Steady state Data. *Cell*
652 *Systems* *1*, 270–282.
- 653 Hines, J.K., Fromm, H.J., and Honzatko, R.B. (2006). Novel Allosteric Activation Site in
654 Escherichia coli Fructose-1,6-bisphosphatase *.
- 655 Hui, S., Silverman, J.M., Chen, S.S., Erickson, D.W., Basan, M., Hwa, T., and
656 Williamson, J.R. (2015). Quantitative proteomic analysis reveals a simple strategy of
657 global resource allocation in bacteria. *Molecular Systems Biology*.
- 658 Johnson, J.L., and Reinhart, G.D. (1997). Failure of a two-state model to describe the
659 influence of phospho(enol)pyruvate on phosphofructokinase from Escherichia coli.
660 *Biochemistry* *36*, 12814–12822.
- 661 Kelley-Loughnane, N., Biolsi, S.A., Gibson, K.M., Lu, G., Hehir, M.J., Phelan, P., and
662 Kantrowitz, E.R. (2002). Purification, kinetic studies, and homology model of
663 Escherichia coli fructose-1,6-bisphosphatase. *Biochimica et Biophysica Acta* *1594*, 6–16.
- 664 Kochanowski, K., Volkmer, B., Gerosa, L., Haverkorn van Rijsewijk, B.R., Schmidt, A.,
665 and Heinemann, M. (2013a). Functioning of a metabolic flux sensor in Escherichia coli.
666 *Proceedings of the National Academy of Sciences* *110*, 1130–1135.
- 667 Kochanowski, K., Volkmer, B., Gerosa, L., Haverkorn van Rijsewijk, B.R., Schmidt, A.,
668 and Heinemann, M. (2013b). Functioning of a metabolic flux sensor in Escherichia coli.
669 *Proceedings of the National Academy of Sciences of the United States of America* *110*,
670 1130–1135.
- 671 Link, H., Anselment, B., and Weuster-Botz, D. (2008). Leakage of adenylates during
672 cold methanol/glycerol quenching of Escherichia coli. *Metabolomics* *4*, 240–247.

- 673 Link, H., Kochanowski, K., and Sauer, U. (2013). Systematic identification of allosteric
674 protein-metabolite interactions that control enzyme activity in vivo. *Nature*
675 *Biotechnology* *31*, 357–361.
- 676 Nikel, P.I., Chavarría, M., Fuhrer, T., Sauer, U., and Lorenzo, V. de (2015).
677 *Pseudomonas putida* KT2440 Strain Metabolizes Glucose through a Cycle Formed by
678 Enzymes of the Entner-Doudoroff, Embden-Meyerhof-Parnas, and Pentose Phosphate
679 Pathways *. *Journal of Biological Chemistry* *290*, 25920–25932.
- 680 Noor, E., Eden, E., Milo, R., and Alon, U. (2010). Central Carbon Metabolism as a
681 Minimal Biochemical Walk between Precursors for Biomass and Energy. *Molecular Cell*
682 *39*, 809–820.
- 683 Noor, E., Bar-Even, A., Flamholz, A., Reznik, E., Liebermeister, W., and Milo, R.
684 (2014). Pathway Thermodynamics Highlights Kinetic Obstacles in Central Metabolism.
685 *PLOS Computational Biology* *10*, e1003483.
- 686 Otterstedt, K., Larsson, C., Bill, R.M., Ståhlberg, A., Boles, E., Hohmann, S., and
687 Gustafsson, L. (2004). Switching the mode of metabolism in the yeast *Saccharomyces*
688 *cerevisiae*. *EMBO Reports* *5*, 532–537.
- 689 Pham, A.S., and Reinhart, G.D. (2001). Pre-steady state quantification of the allosteric
690 influence of *Escherichia coli* phosphofructokinase. *J Biol Chem* *276*, 34388–34395.
- 691 Ramseier, T.M., Bledig, S., Michotey, V., Feghali, R., and Saier, M.H. (1995). The
692 global regulatory protein FruR modulates the direction of carbon flow in *Escherichia coli*.
693 *Molecular Microbiology* *16*, 1157–1169.
- 694 Saa, P., and Nielsen, L.K. (2015). A General Framework for Thermodynamically
695 Consistent Parameterization and Efficient Sampling of Enzymatic Reactions. *PLOS*
696 *Computational Biology* *11*, e1004195.
- 697 Schink, S.J., Biselli, E., Ammar, C., and Gerland, U. (2019). Death Rate of *E. coli* during
698 Starvation Is Set by Maintenance Cost and Biomass Recycling. *Cell Systems* *9*, 64-73.e3.
- 699 Soupene, E., van Heeswijk, W.C., Plumbridge, J., Stewart, V., Bertenthal, D., Lee, H.,
700 Prasad, G., Paliy, O., Charernnoppakul, P., and Kustu, S. (2003). Physiological Studies of
701 *Escherichia coli* Strain MG1655: Growth Defects and Apparent Cross-Regulation of
702 Gene Expression. *J Bacteriol* *185*, 5611–5626.
- 703 Stover, C.K., Pham, X.Q., Erwin, A.L., Mizoguchi, S.D., Warrenner, P., Hickey, M.J.,
704 Brinkman, F.S.L., Hufnagle, W.O., Kowalik, D.J., Lagrou, M., et al. (2000). Complete
705 genome sequence of *Pseudomonas aeruginosa* PAO1, an opportunistic pathogen. *Nature*
706 *406*, 959–964.
- 707 Vasilakou, E., Machado, D., Theorell, A., Rocha, I., Nöh, K., Oldiges, M., and Wahl,
708 S.A. (2016). Current state and challenges for dynamic metabolic modeling. *Current*
709 *Opinion in Microbiology* *33*, 97–104.

- 710 Vicente, M., and Cánovas, J.L. (1973). Glucolysis in *Pseudomonas putida*: physiological
711 role of alternative routes from the analysis of defective mutants. *Journal of Bacteriology*
712 *116*, 908–914.
- 713 Wang, C.H., Stern, I.J., and Gilmour, C.M. (1959). The catabolism of glucose and
714 gluconate in *Pseudomonas* species. *Archives of Biochemistry and Biophysics* *81*, 489–
715 492.
- 716 Yang, L., Ebrahim, A., Lloyd, C.J., Saunders, M.A., and Palsson, B.O. (2019).
717 DynamicME: dynamic simulation and refinement of integrated models of metabolism
718 and protein expression. *BMC Systems Biology* *13*, 2.
- 719 Zampar, G.G., Kümmel, A., Ewald, J., Jol, S., Niebel, B., Picotti, P., Aebersold, R.,
720 Sauer, U., Zamboni, N., and Heinemann, M. (2013). Temporal system-level organization
721 of the switch from glycolytic to gluconeogenic operation in yeast. *Molecular Systems*
722 *Biology* *9*, 651.
- 723 Zheng, R.L., and Kemp, R.G. (1995). Phosphofructo-1-kinase: Role of Charge
724 Neutralization in the Active Site. *Biochemical and Biophysical Research*
725 *Communications* *214*, 765–770.
- 726