On the effect of inheritance of microbes in commensal microbiomes

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Background. Our current view of nature depicts a world where macroorganisms dwell in a landscape full of microbes. Some of these microbes not only transit but establish themselves in or on hosts. Although hosts might be occupied by microbes for most of their lives, a microbe-free stage during their prenatal development seems to be the rule for many hosts. The questions of who the first colonizers of a newborn host are and to what extent these are obtained from the parents follow naturally.

Results. We have developed a mathematical model to study the effect of the transfer of microbes from parents to offspring. Even without selection, we observe that microbial inheritance is particularly effective in modifying the microbiome of hosts with a short lifespan or limited colonization from the environment, for example by favouring the acquisition of rare microbes.

Conclusion. By modelling the inheritance of commensal microbes to newborns, our results suggest that, in an eco-evolutionary context, the impact of microbial inheritance is of particular importance for some specific life histories.

Keywords: microbiome, host, colonization, microbial inheritance, mathematical model.

22 1. Background

23 Microbial life is ubiquitous in the biosphere [1]. The human body is no exception, as first described
 24 by van Leeuwenhoek in the 17th century. We are among the many macroorganisms where diverse
 25 microbiomes – microbial communities living in or on hosts – have been observed [2, 3]. As part
 26 of their life cycle, members of the microbiome may migrate between hosts and the environment.
 27 The migration process has been studied using experimental [4] and theoretical approaches [5, 6].
 28 However, some microbes have been found exclusively in hosts [4, 7]. How do such microbes persist
 29 in the population?

30 One possibility is the vertical transfer of microbes from parents to offspring [8]. Although there is
 31 ample literature about transmission of endosymbionts (e.g. *Buchnera* and *Wolbachia* in insects [9]),
 32 less is known about extracellular – possibly transient – microbes. Quantifying the low microbial loads
 33 in newborns [10] and deciphering the true origin of microbes [11] remains experimentally challenging
 34 [12, 13]. A few experimental studies have explored the vertical transfer of the microbiome in specific
 35 species across the tree of life – including sponges [14], mice [15], cockroach eggs [16], and wheat
 36 seedlings [17]. For many others, including humans, there is an ongoing debate on when and how
 37 inherited microbes are obtained [11]. Together, these studies suggest there is no universal reliance
 38 on microbial inheritance across host species, raising the possibility that even if such associations
 39 matter to the host, certain life-history traits may limit their inheritance [13, 18]. Relevant traits
 40 may include, among others, the extent of environmentally acquired microbes and host lifespan.

41 Previous theoretical work has studied microbial inheritance in the context of symbiosis – where
 42 microbes affect the host fitness. In these models, depending on whether the interaction is positive
 43 (mutualism) or negative (parasitism) the presence of symbionts is promoted or impeded, respec-
 44 tively. Using multilevel selection arguments, Van Vliet and Doebeli have shown that a symbiosis
 45 that is costly for microbes can be sustained only when the host generation time is short and the
 46 contribution of inheritance exceeds that of environmental immigration [19]. Following up, in addition
 47 to individual inheritance (single contributing parent), Roughgarden analyzed scenarios of collective
 48 inheritance (multiple contributing parents) [20]; while Leftwich et al. found a weak influence of the
 49 host reproductive mode (sexual or asexual) and mate choice (based on symbiont presence) on the

50 symbiont occurrence [21]. If these host-symbiont interactions persist over evolutionary timescales,
51 they are said to lead to phyllosymbiosis – where microbiomes recapitulate the phylogeny of their
52 hosts [22].

53 Not all co-occurrences between hosts and microbes reflect a fitness impact, however. As suggested
54 by Bruijning et al., the selection on the host-microbiome pair and the microbial inheritance might
55 change with the environment [18]. Moreover, despite taxonomic differences, functional equivalence
56 of microbes in localized host populations could prevail [16]. Microbes might not always influence
57 host fitness [18] nor benefit from influencing it [21]. In this context where there is no active selection
58 of the microbes by the host, the role of microbial inheritance remains largely unexplored [23].

59 Using a stochastic model, we study the effect of microbial inheritance on the commensal micro-
60 biome – microbes living in hosts but not affecting their fitness. First, we introduce different models
61 of inheritance representative of diverse host species. Then we discuss their effect on microbes present
62 in both hosts and environment, or only present in hosts. We see that inheritance might influence
63 the within-host occurrence and abundance in some cases. However, within the same microbiome,
64 microbial types could be affected differently – while inheritance causes some microbes to increase
65 in frequency, others decrease from it. Moreover, the effects may be transient, rendering life history
66 parameters crucial. Altogether, we highlight the potential and limits of microbial inheritance to
67 modify the composition of commensal microbiomes under different life-history scenarios.

68 2. Model and methods

69 Consider the host-microbiome system depicted in Fig. 1A. A population of hosts is colonized by
70 a set of microbes, and each microbial taxon i has a constant frequency p_i in the environment.
71 The total number of microbes a host can contain is finite and given by N . Each newborn empty
72 host inherits a set of microbes from its parent, chosen at random within the host population. The
73 inherited sample, taken off the parental microbiome, is drawn according to a probability distribution
74 (Fig. 1B). After this initial seeding, only the death, immigration and replication of microbes can
75 modify the host microbiome. Through these processes, the microbial populations within the host

Figure 1: **Host-microbiome dynamics and microbial inheritance in our model.** (A) Dark blobs indicate hosts, coloured- and empty-circles indicate microbes and empty-space, respectively. Within the hosts, microbes go through a death and immigration-birth process, with new residents migrating from the pool of colonizing microbes with probability m or replicating within a host with probability $1 - m$. For microbes, each host is an identical habitat. The host population is at a dynamic equilibrium, every timestep there is a probability τ that a host death occurs, immediately followed by the birth of a new one. The newborn obtains a sample of its parent microbiome according to a probability distribution. (B) The probability distribution of the fraction of the parental microbiome inherited vary across host taxa – among others, influenced by development, reproduction and delivery mode. Certain hosts might not transfer microbes (eg. *C. elegans* [24] or *D. melanogaster* [25]). Others might provide minimal (eg. humans [11]) or large fractions of their microbes (eg. fragmentation of some sponges, corals, fungi and plants [26, 27]), while others might be centred around a fixed value (eg. seeds of plants [17]). In our model, we control this probability distribution through the parameters a_i and b_i in Eq. (4).

76 can decrease or increase by one individual each time step. After one microbe is selected to die,
 77 migration from the pool of colonizers occurs with probability m , while duplication of a resident
 78 microbe, or non-replacement, occurs with probability $1 - m$. This process ends with the host death,
 79 which occurs with probability τ at each time step. We assume that the number of hosts does not
 80 change, so that a host death is followed by the birth of a new empty host, for which the process
 81 described above is repeated.

82 2.1. Transition probabilities

83 Our aim is to describe the dynamics of the microbiome load and composition, focusing in particular
 84 on how a certain microbial taxon experiences it. Within a specific host, the frequency of the i -th
 85 taxon is denoted by x_i (for $i \geq 1$), and of the remaining other microbes by $o_i = \sum_{j \neq i} x_j$. The
 86 frequency of available space is then given by $x_0 = 1 - x_i - o_i$. The transition probabilities from state
 87 $\{x_i, o_i\}$ that are due to the microbial dynamics are given by the product of the probability of host

88 survival, $1 - \tau$, by the probability of death of a certain microbial type followed by an immigration
89 or birth event. These events produce changes in the frequencies of magnitude $\frac{1}{N}$. First, microbial
90 taxa can replace each other when a microbe dies and is replaced by another one,

$$T_{x_i-}^{o_i+} = (1 - \tau) x_i \left(m(1 - p_i) + (1 - m) \frac{o_i}{\alpha_0 x_0 + x_i + o_i} \right) \quad (1a)$$

$$T_{x_i+}^{o_i-} = (1 - \tau) o_i \left(mp_i + (1 - m) \frac{x_i}{\alpha_0 x_0 + x_i + o_i} \right). \quad (1b)$$

91 In Eq. (1a), a microbe of type i dies and is replaced by another microbe, either by immigration from
92 the environmental pool or by replication within the same host. Similarly, in Eq. (1b), a microbe of
93 another type dies and is replaced by a microbe of type i .

94 Alternatively, microbes may occupy previously available space, such that the microbial abundance
95 increases,

$$T_{x_i-}^{o_i+} = (1 - \tau) x_0 \left(m(1 - p_i) + (1 - m) \frac{o_i}{\alpha_0 x_0 + x_i + o_i} \right) \quad (1c)$$

$$T_{x_i+}^{o_i-} = (1 - \tau) x_0 \left(mp_i + (1 - m) \frac{x_i}{\alpha_0 x_0 + x_i + o_i} \right). \quad (1d)$$

96 Finally, microbes may decrease in abundance, when a microbe selected for death is not replaced,

$$T_{x_i-}^{o_i-} = (1 - \tau) x_i \left((1 - m) \frac{\alpha_0 x_0}{\alpha_0 x_0 + x_i + o_i} \right) \quad (1e)$$

$$T_{x_i+}^{o_i+} = (1 - \tau) o_i \left((1 - m) \frac{\alpha_0 x_0}{\alpha_0 x_0 + x_i + o_i} \right). \quad (1f)$$

97 In these equations, α_0 controls the establishment of microbes in hosts – the ability to occupy
98 available space – going from fast for $\alpha_0 = 0$, to slow if α_0 is positive. For $\alpha_0 > 1$ and without
99 migration, microbes cannot be maintained in hosts.

100 The transition probabilities due to the hosts dynamics are given by the product of the probability
101 of host death and birth of an empty host (τ), by the probability to inherit certain microbes,

$$T_{\Delta x_i}^{\Delta o_i} = \tau \sum_p \frac{1}{H - 1} \omega_i[\Delta x_i, x_i^{(p)}] \omega_i[\Delta o_i, o_i^{(p)}], \quad (2)$$

where $1/(H - 1)$ is the probability of choosing a parent p in the population of $H - 1$ potential parents, and $\omega_i[\Delta x_i, x_i^{(p)}]$ and $\omega_i[\Delta o_i, o_i^{(p)}]$ are the probabilities of transfer of Δx_i and Δo_i microbes from the parent to the offspring, respectively. Because the frequencies within the parent are $x_i^{(p)}$ and $o_i^{(p)}$, the probability to transfer more microbes than the parent can provide is zero. Finally, for completeness, the probability of staying in state $\{x_i, o_i\}$ without host death is

$$T_{x_i}^{o_i} = 1 - T_{x_i-}^{o_i+} - T_{x_i+}^{o_i-} - T_{x_i-}^{o_i+} - T_{x_i+}^{o_i-} - T_{x_i-}^{o_i-} - T_{x_i+}^{o_i+} - \tau, \quad (3)$$

where the last term includes all possible transitions due to parental transfer of microbes, $\int \int T_{\Delta \tilde{x}_i}^{\Delta \tilde{o}_i} d\Delta \tilde{x}_i d\Delta \tilde{o}_i = \tau$.

2.2. Distribution of inherited microbes

In our model, parents can seed the microbiome of their offspring. A sample of the parental microbiome is vertically transmitted according to a probability distribution function, Eq. (2). In addition to the case without inheritance, which we have previously analyzed elsewhere [28], at least three qualitatively distinct cases may be observed (Fig. 1B), depending on host development, reproduction, and mode of delivery.

Firstly, inheritance could be low. For example in animals, newborns get microbes attached to epithelia or fluids during delivery [11, 8]. These represent a small fraction of the parental microbiome, leading to distributions centred at frequency zero decaying towards one. Secondly, certain hosts, including some sponges, corals, fungi and plants [26, 27], are able to reproduce by fragmentation, where a breaking body part generates a new individual. Such fragments could carry a faithful microbiome composition, leading to distributions centered at frequency one decaying towards zero. Finally, hosts that produce embryos that can disperse, eg. seeds, might transfer a microbiome sample contained within these physical structures [17].

We modelled such diverse parental microbiome samplings (Δx_i) using the beta distribution for the probability $\omega_i[\Delta x_i, x_i^{(p)}]$ to inherit Δx_i microbes from parent p . This probability distribution can

125 take arguments in the range from zero to the current frequency of a microbe in the parent p , $x_i^{(p)}$,

$$\omega_i[\Delta x_i, x_i^{(p)}] = \frac{1}{B[a_i + 1, b_i + 1]} \left(\frac{\Delta x_i}{x_i^{(p)}} \right)^{a_i} \left(1 - \frac{\Delta x_i}{x_i^{(p)}} \right)^{b_i}, \quad (4)$$

126 where B is the beta function [29], $1/B$ a normalization constant, and a_i and b_i are shape parameters.
 127 The expected value of our beta distribution is $\frac{a_i+1}{a_i+b_i+2}$. The special case of $a_i, b_i = 0$ leads to a
 128 uniform distribution, where the parental microbes are distributed randomly between parent and
 129 offspring. Other combinations of $a_i, b_i \geq 0$ produce different unimodal distributions (Fig. 1B). The
 130 case of $a_i > b_i$ skews the distribution towards full inheritance of the parental microbes, $\Delta x_i = x_i^{(p)}$ –
 131 all the i -th microbes from the parent could be transferred to the offspring. The case of $a_i < b_i$ skews
 132 the distribution towards non-inheritance of microbes of type i to offspring, $\Delta x_i = 0$. Finally for
 133 $a_i = b_i$, the distribution is symmetric and the parental microbes are likely to be equally distributed
 134 between parent and offspring. In most of our analyses a_i and b_i are the same for all microbial taxa.
 135 Only for non-neutral, asymmetric inheritance, we will set different a_i and b_i for the focal taxon (x_i)
 136 and the set of others (o_i). To illustrate the effect of a_i and b_i , on average, an offspring inherits
 137 $\approx 9\%$ of the parental microbes of taxon 1 for $a_1 = 0$ and $b_1 = 9$, while only $\approx 1\%$ is inherited for
 138 $a_1 = 0$ and $b_1 = 99$.

139 Throughout the results, we focus on distributions with a maximum at microbial frequency zero
 140 decaying towards $x_i^{(p)}$, which we call ‘low inheritance’ (Fig. 1B). In our model, the low inheritance
 141 and the ‘full inheritance’ scenarios (distributions with maximum at frequency $x_i^{(p)}$ decaying towards
 142 zero) are equivalent. This stems from the fact that the number of microbes is conserved, so that
 143 inheritance happens through the splitting of the parental microbiome between the parent and the
 144 offspring. Thus, since in our model, the probability to die of a host does not depend on its age, the
 145 splitting of microbes in the low inheritance scenario – where a small fraction is transmitted – and in
 146 the full inheritance scenario – where most of the microbiome is transmitted – are equivalent. Finally,
 147 we address under which circumstance a ‘seed-like inheritance’ leads to different results.

148 2.3. Stochastic simulations

149 In order to simulate the microbiome dynamics of individual hosts we formulated the model as a
150 stochastic differential equation. We solved this equation numerically using the Euler-Maruyama
151 method [30]. Starting from state $\mathbf{x} = \{x_i, o_i\}$ at time t the new state after an interval Δt is given
152 by

$$\mathbf{x}[t + \Delta t] = \mathbf{x}[t] + \mathbf{A}[\mathbf{x}[t]]\Delta t + B[\mathbf{x}[t]]\Delta \mathbf{W}[\Delta t], \quad (5)$$

153 where $\mathbf{A}[\mathbf{x}[t]]$ is the vector of expected changes of $\mathbf{x}$, the deterministic contribution; while $B[\mathbf{x}[t]]$ is
154 a matrix that has the property $B[\mathbf{x}[t]]^T B[\mathbf{x}[t]] = V[\mathbf{x}[t]]$, where $V[\mathbf{x}[t]]$ is the covariance matrix of
155 the change of $\mathbf{x}$. Further, $\Delta \mathbf{W}$ is a vector of uncorrelated random variables sampled from a normal
156 distribution with mean 0 and variance Δt , the stochastic contribution. That $\Delta \mathbf{W}$ is normally
157 distributed arises from the time independence and identical distribution of the noise. A detailed
158 description connecting Eq. (1) and Eq. (5) is provided in Appendix A1.

159 For most of their life, hosts are independent of each other, only newborns are influenced by
160 others when they acquire their initial microbiome. A given host lives for a duration sampled from
161 an exponential distribution $\tau e^{-\tau t}$, with mean $1/\tau$. We solve Eq. (5) for that interval. Immediately
162 after a host dies, the microbiome of a newborn is assembled according to Eq. (2). We repeat these
163 steps for all hosts until the total simulation time is reached.

164 As a result of stochasticity, each host trajectory is different. We look into the statistical description
165 of the microbiome composition across the host population.

166 3. Results

167 3.1. Inheritance can increase the occurrence of microbes in hosts with 168 low microbial loads

169 Without microbial inheritance, which will be our reference case throughout, any microbe occurring
170 inside a host has to have migrated from the environment during the host lifespan. As a result, a
171 low environmental migration or short host lifespan can be limiting [28]. The transfer of microbes

Figure 2: **Microbial occurrence in hosts under microbial inheritance.** (A) Starting from a condition where all hosts are initially empty, the microbial occurrence increases through time. At first sight, this increase is largely independent of α_0 and the inheritance of microbes. A closer look at equilibrium abundance reveals that inheritance increases the occurrence, in this case, regardless of how rapidly hosts are occupied (α_0). (B) The increase results from a distribution of microbial load across the host population where the microbe-free state is less common. A microbial load of 10^{-5} corresponds to 1 microbe per host. In (C-E), single parameters are modified from the case shown in (A-B) (with parameters $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$, indicated by the triangles in (C-E)). (C) A large migration from the pool of colonizers, $m \rightarrow 1$, hinders any effect of inheritance on occurrence as hosts are readily colonized. The change peaks and decreases for smaller m , as for $m \rightarrow 0$ hosts are less likely to be colonized. The change can even be negative for slowly occupied hosts where the few colonizing microbes are lost to stochasticity. (D) The gain from inheritance is maximal for intermediate values of host death probability, τ . Long living hosts, $\tau \rightarrow 0$, are colonized even without inheritance. Short living hosts, $\tau \rightarrow 1$, are less likely to be colonized and thus transmit microbes through inheritance. (E) The carrying capacity for microbes of a host, N , and α_0 do not alter the gain from inheritance. Points and bars in (C-E) indicate the average and standard deviation of 6 simulation pairs, with vs. without inheritance, with 10^4 hosts each. Offspring receive 9% of their parent's microbiome on average, $a_i = 0$ and $b_i = 9$ in Eq. (4). The whole distributions are shown in Fig. Sup. 2.

172 from parents to offspring during birth could increase the probability of observing any microbes in
 173 hosts, $P[x_i + o_i > 0]_{\text{inh.}}$. We quantified the change in the probability of occurrence relative to its
 174 microbe-free birth condition $P[x_i + o_i > 0]_{\text{no inh.}}$,

$$\Delta P[x_i + o_i > 0] = P[x_i + o_i > 0]_{\text{inh.}} - P[x_i + o_i > 0]_{\text{no inh.}} \quad (6)$$

175 Using this observable, we investigated the role of life history in modulating the effect that inheritance
176 has on the microbiome. We quantified this for a single microbial taxon, x_i , as well.

177 Fig. 2 shows a condition where, in the absence of inheritance, hosts are not fully occupied by
178 microbes. This results from a short host lifespan (τ) and low microbial immigration from the pool
179 of colonizers (m). We tested the effect of the ‘low inheritance’ mode (Fig. 1B) for increasing rates
180 of establishment of microbes ($\alpha_0 \rightarrow 0$) and other life-history parameters.

181 Inheritance impacts the occurrence of microbes by increasing the number of hosts with at least
182 one colonizing microbe (Fig. 2B). The effect is most prominent in scenarios where without inheri-
183 tance, most of the hosts are microbe-free. However, the maximum increase occurs at intermediate
184 immigration and host lifespans (Fig. 2C-D). For high immigration, $m \rightarrow 1$, hosts are readily occu-
185 pied by microbes, so inheritance brings no change. Similarly for a long host lifespan, $\tau \rightarrow 0$. On the
186 other hand, if immigration is limited, $m \rightarrow 0$, or host lifespan short, $\tau \rightarrow 1$, microbes never occur
187 in hosts, so parents cannot transmit microbes to their offspring.

188 Inheritance might decrease the occurrence if the transfer – which splits the parental microbiome
189 between parent and offspring – makes microbes more susceptible to stochastic fluctuations. This
190 occurs if the microbial frequency of the parent is already low – for example when migration is limiting
191 and microbes proliferate slowly (Fig. 2C). This phenomenon might be pronounced for individual
192 taxa. Our analyses from the perspective of a single taxon (Fig. Sup. 1) found multiple instances
193 where inheritance might decrease the occurrence (Fig. Sup. 1C-F), but also have a larger effect in
194 situations where the occurrence increases. Additionally, the effect on single taxa depends strongly
195 on the carrying capacity for microbes, N (Fig. Sup. 1F compared to Fig. 2E). Competition for space
196 favours taxa according to their frequency in the pool of colonizers, p_i (Fig. Sup. 1C). Abundant
197 taxa outcompete rare ones as space is more limited, but only until a point, after which there is no
198 benefit – they readily occur without inheritance. In other words, in microbiomes composed by many
199 taxa, the taxon-level effect of inheritance in terms of occurrence is relative to their environmental
200 abundance.

3.2. Inheritance can increase the abundance in hosts, but mostly of those abundant in the environment

Modifying the presence of taxa is not the only effect – inheritance also alters the microbiome composition considerably. Using the distribution of microbial frequencies in hosts, we quantified the change in the average frequencies as compared to its microbe-free birth condition,

$$\Delta E[x_i + o_i] = E[x_i + o_i]_{\text{inh.}} - E[x_i + o_i]_{\text{no inh.}} \quad (7)$$

Similarly to Eq. (6), we quantified this observable for a single microbial taxon, x_i , as well.

When looking at the distribution of microbial loads and frequencies in hosts, the effect of the ‘low inheritance’ mode (Fig. 1B) is two fold – while hosts with small frequencies might experience the largest increase in microbes, hosts with large frequencies can see the largest decrease of microbes (Fig. 2B and Fig. Sup. 2). Thus, at both microbial load and single taxon levels, hosts with small and large frequencies become rarer. Inheritance makes hosts resemble each other to a greater extend (see the reduced spread of the distributions in Fig. Sup. 2 and Fig. Sup. 3). This is equivalent to the effect of increased immigration, which also tends to make microbiomes similar to one another, but increased inheritance does not favour the preservation of the diversity from the pool of colonizers – in contrast to immigration.

An increase in the average load is observed for some conditions (Fig. Sup. 2). Analogously to the occurrence, such increase peaks at intermediate host death probabilities τ ; but also at intermediate carrying capacities N (Fig. 3C-D). The limited time for host colonization impedes any inheritance ($\tau \rightarrow 1$), while for $\tau \rightarrow 0$ or small N , hosts are fully occupied even without it. The relative effect of inheritance is less for large N . A faster occupation of available space ($\alpha_0 \rightarrow 0$) displaces the effect to larger host death probabilities and capacities for microbes. Finally, because the main limitation is the short host lifespan (τ), the influence of immigration (m) is minimal (see the scale in Fig. 3B and Fig. Sup. 4C).

Although higher loads might be reached with inheritance if space is limited (Fig. Sup. 2C), abundant taxa might increase at the expense of rare ones (Fig. Sup. 3D and Fig. Sup. 4D-E).

Figure 3: **Average microbial load in hosts under microbial inheritance.** (A) Starting from a condition where all hosts are initially empty, the average frequency of microbes in hosts increases through time before reaching an equilibrium. In this particular case, inheritance makes such equilibrium abundance larger only when hosts are occupied rapidly, $\alpha_0 \rightarrow 0$. This increase results from a host distribution where higher microbial loads are more common (Fig. 2B). The cases shown in (A), with parameters $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$, are indicated by the triangles in (B-D). A single parameter is varying in (B-D). (B) Changes of migration from the pool of colonizers, m , have minimal effect (notice the scale). As $m \rightarrow 1$, more microbes colonize the hosts. Still the average microbial load only increases if the loss of microbes to inheritance is less than the gain from proliferation. (C) The effect of changes to host death probability, τ , are much larger and maximal at intermediate τ . A faster occupation of hosts makes the effect of inheritance larger for shorter living hosts, $\tau \rightarrow 1$. (D) In contrast to the occurrence (Fig. 2E), changes in the carrying capacity for microbes, N , have a larger intermediate effect. Faster occupation of hosts makes the effect peak for larger N . Points and bars in (B-D) indicate the average and standard deviation of 6 simulation pairs, with vs. without inheritance, with 10^4 hosts each. Offspring receive 9% of their parent's microbiome on average, $a_i = 0$ and $b_i = 9$ in Eq. (4). The whole distributions are shown in Fig. Sup. 2.

226 Such reduction is exacerbated by the fast occupation of available space $\alpha_0 \rightarrow 0$. Interestingly, this
 227 might happen as a result of longer host lifespans as well, if hosts are rapidly occupied by inherited
 228 microbes. Such condition favours abundant taxa in the pool of colonizers. Instead, if the occupation
 229 is slower, rare taxa increase in frequency, derived from the added benefits of inheritance and a more
 230 influential immigration (m).

231 A particularly relevant question is whether the frequency of a taxon in a specific host (x_i) can be

larger than in the pool of colonizers (p_i) – i.e. a benefit is obtained from the host association. We observe this even in the absence of inheritance (Fig. Sup. 3), where stochastic colonization results in some host containing frequencies larger than in the pool (p_i). The average frequency across hosts, however, can be larger only when the space limitation increases the competition. In this context, inheritance may, in fact, decrease the chances of such outcome, by relating the hosts to each other (Fig. Sup. 3C-D).

3.3. Preferential inheritance can temporally lead to specific taxa overrepresentation

A potential mechanism to increase the average frequency of taxa beyond their frequency in the pool of colonizers (p_i), is preferential inheritance. The asymmetry in inheritance could stem from differences in microbial properties, but also a host's direct or indirect influence. We studied such possibility by manipulating the distribution of the sample inherited, Eq. (4). Focusing on a 'low inheritance' mode, we decreased the inheritance of other taxa relative to taxon i , from equal if offspring receive 9% of every taxa on average, to preferential if they receive 9% of taxon i but 1% of others.

For the same parameters as before (Fig. 4), we observe no effect if the host lifespan is limiting. In this case, regardless of the frequency in the pool of colonizers (p_i), preferential inheritance does not alter the average frequency of the i -th taxon in hosts (Fig. 4A), similarly for the probability of immigration m (Fig. 4B). This holds even for fast occupation of available space, $\alpha_0 \rightarrow 0$. Only for longer host lifespan, $\tau \rightarrow 0$, preferential inheritance leads to an increase (Fig. 4C). Besides the almost exclusive occupation of hosts by the i -th taxon ($\bar{x}_i \rightarrow 1$), the maximum effect is constrained to intermediate τ . This is because the effect of preferential inheritance is transitory for longer living hosts, after which they continue approaching their long term equilibrium, $\bar{x}_i \rightarrow p_i$. For faster occupation of available space the gain spans a wider range and shorter host lifespans ($\tau \rightarrow 1$). For hosts with short lifespan and limited immigration (in our example $\tau = 10^{-4}$ and $m = 10^{-2}$), the gain from preferential inheritance is largest for decreasing carrying capacity for microbes, N (Fig. 4D).

As shown in Fig. 4D, inheritance itself might not benefit all microbial taxa. For some taxa, only

Figure 4: **Effect of asymmetric inheritance on the average frequency of a taxon in hosts.** Cases without inheritance and inheritance are compared. Inheritance is symmetric if offspring receive 9% of their parent's microbiome on average ($a_i = 0$ and $b_i = 9$). Inheritance is asymmetric if offspring receive 9% of taxon 1 and 1% of other taxa ($a_i = 0$ and $b_1 = 9$, $b_{i \neq 1} = 99$ in Eq. (4)). Available space within hosts is occupied more easily for $\alpha_0 \rightarrow 0$. Single parameters are modified from the condition $p_1 = 10^{-2}$, $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$. **(A-B)** The average frequency increases for larger abundances in the pool of colonizers (p_1), immigration (m), and $\alpha_0 \rightarrow 0$. An asymmetric inheritance has no effect, as hosts are not fully occupied within their lifetime (Fig. Sup. 2 and Fig. Sup. 3). **(C)** Longer host lifespans, $\tau \rightarrow 0$, increase the average frequency and effect of asymmetric inheritance. The gain is maximal at intermediate τ . Inheritance has more influence before hosts are fully occupied. After this, hosts resemble the colonizers pool. **(D)** The average frequency increases with competition for space (smaller N). While the symmetry of inheritance decreases the average frequency as a result of the reduced initial microbiome variability, asymmetry increases it. Each simulation included 10^4 hosts.

259 preferential inheritance can lead to larger frequencies than without inheritance.

260 3.4. Persistence of lineage taxa in hosts

261 An extreme case of reliance on microbial inheritance are microbes present in hosts but absent from
 262 the environment ($p_i = 0$) [1, 7]. We refer to these as lineage taxa. We investigated the conditions
 263 allowing their persistence under different life-history scenarios (Fig. 5).

264 Within a host, lineage taxa go through the stages sketched in Fig. 5A. Depending on the context,
 265 after host birth, their frequency might either decrease or increase. If decrease occurs, in a neutral
 266 context this trend will not change during the host life. In fact, events of microbiome inheritance
 267 will further decrease the frequency in the parent. We found that on average, lineage taxa increase

Figure 5: **Persistence of lineage taxa in hosts.** A microbial taxon is initially present in hosts $x_1(0) > 0$, but not in the pool of colonizers, $p_1 = 0$. (A) The frequency within a host decreases through time. For some conditions, Eq. (8), there is a period of increase. If the taxon is transmitted to offspring before the gain is lost, this might persist in the host population (although extinction within the parent occurs sooner). (C) Low immigration ($m \rightarrow 0$) and fast occupation of available space ($\alpha_0 \rightarrow 0$) allow increase and prolong the time before extinction, Eq. (8). Large initial available space ($x_i + o_i \rightarrow 0$) and lineage taxon fractions ($x_1/(x_1 + o_1) \rightarrow 1$) also prolong this time. (B) After the increase stops (x_1^*), the average time to extinction is shorter for large immigration ($m \rightarrow 1$) and a smaller fraction of the taxon. (D) At the host population level, lines indicate the death probability after which most hosts lose the lineage taxon ($\tau_{0.5}$), Eq. (9). The early increase shown in (A) only occurs within the darkened area. The distribution of microbes inherited, Fig. 1B and Eq. (4), affects the initial load and fraction of lineage taxa in offspring. Asymmetric inheritance in low microbial loads might preserve lineage taxa as well as symmetric inheritance in high loads. We set $N = 10^5$. Each point corresponds to 10^4 simulated hosts.

268 while the inequality

$$x_i + o_i < 1 - \frac{m}{1 - \alpha_0} \quad (8)$$

269 holds (Fig. 5C and Appendix A). Therefore, lineage taxa increase before reaching carrying capacity,
 270 favoured by their fast proliferation ($\alpha_0 \rightarrow 1$), but restricted by migration (m). Because the microbial
 271 load increases through time ($x_i + o_i \rightarrow 1$), alongside the initial state, Eq. (8) limits the time of

272 increase. Note that on average, the maximum frequency of lineage taxa is $1 - m/(1 - \alpha_0)$. From
273 this point on, a decrease driven by the immigration of environmentally present microbes (m) and
274 stochasticity follows. For sufficiently long time, such decrease may lead to their extinction (Fig. 5B).

275 There is a trade-off between the duration of the increase and the maximum frequency of lineage
276 taxa. While small initial microbial loads lead to long durations but small frequencies (as a result of
277 immigration, Eq. 8), the opposite is true for high initial loads abundant in lineage taxa. Once increase
278 stops, the time to extinction is proportional to the lineage taxa frequency, Fig. 5B. Putting these two
279 times together, the extra time from the increase is behind the subtle effect of the initial microbial
280 load on the total extinction time, Fig. 5D. A reduced migration ($m \rightarrow 0$) and fast occupation of
281 available space ($\alpha_0 \rightarrow 0$) simultaneously increase the frequency and time before extinction.

282 Looking at the population level, a condition for persistence emerges – namely, an increase of
283 frequency in each host followed by transfer to offspring of a frequency at least equal to that received
284 at birth. This is possible only while the frequency in the parent is larger than initially, Fig. 5A. The
285 largest frequencies are expected at intermediate time. In this context, host lifespan, and thereafter
286 the probability of host death (τ) become fundamental. From the distribution of host death events,
287 $\tau e^{-\tau t}$, we see most hosts die early on, potentially while lineage taxa are still abundant; $\tau \rightarrow 0$ results
288 in longer living hosts – those more likely to lose lineage taxa. We estimated the probability of host
289 death at which a fraction z of hosts loses the taxa,

$$\tau_z = -\frac{1}{t_z} \ln(1 - z) \quad (9)$$

290 where t_z , the time at which lineage taxa remain present in a fraction z of the host population, is
291 obtained from the distribution of extinction times. Based on the former observations (Fig. 5D),
292 our model predicts that regardless of the distribution of inherited microbes (Fig. 1B), preferential
293 inheritance of lineage taxa in small microbial loads might favour their persistence as effectively as
294 large but non-preferential microbial loads.

3.5. When the distribution of inherited microbes matters

We proposed that a finite set of shapes captures most of the possible microbial inheritance distributions (Fig. 1B) – low, high, and seed-like inheritance – all characterized by the most likely microbiome fraction transferred to the offspring. So far, we have focused on the impact of low inheritance on the microbiome (Fig. 2-5). As mentioned before, because we enforce the conservation of microbes in our model, i.e. the microbes are transferred from the parent host to the offspring, the outcome of low and high inheritance is equivalent: although the parental microbiome is distributed differently, the outcome is indistinguishable at the host population level, because hosts are indistinguishable.

When referring to certain life-histories, other distribution shapes may alter the impact of inheritance. To find out differences between the effect seed-like inheritance and our former results (where we assumed low inheritance) we compared the occurrence and average microbial frequencies.

We found most changes are minimal, however, differences appear for extreme parameters. A seed-like inheritance might better guarantee the occurrence of microbes in extremely adverse life-histories – e.g. rare environmental migration ($m \rightarrow 0$) and short host lifespan ($\tau \rightarrow 1$) simultaneously (vertical axis on Fig. Sup. 5A-B). Exceptions could arise for a slower occupation of available space (α_0). For individual microbial taxa, changes are greater in occurrence as well (Fig. Sup. 6); however, derived from the competition for limited space (N), the effect of a seed-like inheritance is case-specific. Moreover, both maximum increase and maximum decrease occur at intermediate m (Fig. Sup. 6B) and τ (Fig. Sup. 6C). In microbiomes composed of taxa with different environmental frequencies (p_i), while some taxa gain, others lose from inheritance (Fig. Sup. 6A).

Under less adverse conditions, seed-like inheritance might allow larger microbial loads. That is the case when either host lifespan (horizontal axis on Fig. Sup. 5A) or migration (Fig. Sup. 5B) is limiting. The gain from a seed-like inheritance can be large, especially for a small carrying capacity for microbes N (Fig. Sup. 5C). The consistent microbial transfer and reduced variation are beneficial. Nonetheless, at the single taxon level, gains are minimal (Fig. Sup. 6). At this level, a limiting carrying capacity for microbes, where competition increases, might even lead to a decrease (Fig. Sup. 6D). In this case, the variation provided by the low inheritance mode is more beneficial.

In summary, regardless of the distribution of microbes inherited (Fig. 1B), life-history seems

intrinsically linked to the effect of microbial inheritance on the microbiome composition.

4. Discussion

The impact of microbial inheritance on host-associated microbial communities is largely unknown. In this work, we explored its potential effects under diverse life-history scenarios, including multiple distributions of microbes inherited (Fig. 1). Using a model free of selection – i.e. without microbial fitness differences or effect on host fitness – we shed light on the conditions where microbial inheritance may influence the microbiome composition, showing its impact but also its limits.

Our work emphasizes the role of life-history over host-microbe associations (Fig. 2-3). Even without symbiotic benefits, the inheritance process itself might alter the microbiome composition [21]. Using a discrete generation model, Zeng et al. considered microbial inheritance in neutral associations over evolutionary timescales – specifically, its effect on the microbial diversity and the distribution of frequencies [23]. Our results, however, highlight the relevance of within-generation probabilistic events – environmental colonization, host lifespan, or carrying capacity for microbes – as ecological drivers to constrain inheritance.

A crucial constraint is the host lifespan. Similarly to Van Vliet and Doebeli, but without any impact on the host fitness, we observe that the environmental acquisition of microbes makes the effects of inheritance transient (Fig. 2D, 3C and 4C) [19]. Short-living hosts (relative to the microbial timescale) could influence their commensal microbiome over their whole lives, while long-living hosts only during the first stages of development. The rapid proliferation of inherited microbes or isolation from the environment might prolong the period of influence. This is in contrast to Van Vliet and Doebeli, where selection within isolated hosts acts against costly symbiosis, reducing the period of mutualists presence.

We observed that the effect of inheritance may differ between taxa. Microbiomes assembled entirely from the environment are prone to variation when migration between hosts is rare [28, 18]. Inheritance might increase the presence of certain microbes, but in contrast to environmental migration, inheritance reduces the variation between hosts and potentially their microbial diversity.

349 This reduction, which especially affects rare taxa, is more pronounced if the carrying capacity is
350 limited (Fig. Sup. 1 and Sup. 4), where competition is larger. Bruijning et al. have observed
351 that under selection, such decreased variation and diversity could be detrimental for adaptation to
352 changing environments [18].

353 Initially, we assumed no distinction between microbial taxa – only their frequency determined
354 the population dynamics (Eq. 1). This could be modified in at least two ways. First, fitness
355 differences could influence the birth and death rates of microbes. Although this is certainly relevant,
356 it diverts from our focus on inheritance. Instead, we addressed a possibility crucial for inheritance
357 – the asymmetric transfer of microbes (Fig. 4). Such asymmetry could emerge from differences in
358 microbial capabilities at play during the transfer process, including oxygen tolerance [15] (obligate
359 anaerobes tend to be transmitted vertically) and sporulation [31] (spores might allow the transfer
360 of oxygen-sensitive bacteria). Alternatively, hosts could selectively transfer certain microbes to their
361 offspring [9]. Interestingly, we observe that inheritance alone is not always beneficial; some taxa
362 might only benefit when transferred asymmetrically (Fig. 4).

363 We have emphasized the importance of looking at rare taxa. Such is the case of lineage taxa
364 (Fig. 5), microbes absent from the environment that only propagate by inheritance. Our results
365 indicate the importance of modelling the stochasticity and conservation of microbes – only in this
366 way did we appreciate that inheritance can lead to stochastic loss (Fig. 2-3) and that persistence of
367 lineage taxa may be prolonged by asymmetric inheritance (Fig. 5D). Because microbial frequencies
368 are often small, the omission of stochastic effects from models could lead to misestimate the impact
369 of inheritance.

370 Vertical transfer of microbes might occur in the most diverse host species [12, 18], with only a
371 few exceptions [3]. A great diversity of reproduction and delivery modes might, in turn, determine
372 the distribution of their inheritance – namely the number of microbes transferred and its probability.
373 A comparison of two qualitatively distinct distributions (low and seed-like inheritance in Fig. 1B),
374 indicates they might influence the presence and frequency of microbes differently (Fig. Sup. 5).
375 A consistent cargo in seeds might guarantee the presence of certain microbes in plants [17], who
376 might sometimes benefit from being the first colonizers [28]. In contrast, greater variation might

377 be expected for mammals, where changing amounts of microbes are obtained from epithelia during
378 delivery [11, 12]. Overall, these intrinsic differences might affect the ecological and evolutionary
379 dynamics of hosts and microbes.

380 We found that microbial inheritance is effective only for some life-histories. While it has been
381 shown that symbiosis [19] and fidelity of inheritance [18] can evolve driven by selection, our results
382 suggest the evolution of life-history traits itself, independent of symbiosis, can impact the relevance
383 of microbial inheritance. Interestingly, the emergence of symbiosis could lead to selection acting on
384 the more evolvable and impactful traits – not only the fidelity of inheritance [18].

385 Investigating microbial inheritance experimentally poses technical challenges [11]. However, de-
386 velopments using diverse host species [15, 14, 16, 17], suggest that our predictions could be tested
387 experimentally. Firstly, that inheritance is more influential at intermediate host lifespan, environ-
388 mental migration, or carrying capacity (Fig. 2-3). Related host species with diverse life histories
389 could be compared [32]; alternatively, control could be increased using model organisms amenable
390 to manipulate such traits [33]. Secondly, that the maximum lineage taxa frequency changes with
391 life-history (Eq. 8), could be tested using germ-free or gnotobiotic hosts [17]. Finally, the effect of
392 distinct distributions of microbes inherited (Fig. 1) could be surveyed.

393 Our approach simplifies the complexity of natural microbiomes. A natural step forward would be
394 considering fitness differences among microbes. These could interact with inheritance to preserve or
395 out-compete certain microbes. Secondly, the host population structure could be included. In such
396 a scenario, subpopulations characterized by different microbiomes could emerge [21]. Moreover,
397 critical connectivity might be needed for inheritance to be effective. Finally, we did not account
398 for specific reproductive ages (or development). This might be particularly relevant because, as we
399 have shown, the effect of inheritance erodes through time.

400 5. Conclusion

401 Microbial inheritance can influence the occurrence and abundance of microbes within the host-
402 associated commensal microbiome. Even the persistence of microbes absent from the environment

could be facilitated in some cases. These findings extend to diverse scenarios of inheritance representative of different host species. However, inheritance is not a silver bullet, instead life-history in terms of environmental immigration, early microbial proliferation, and host lifespan limit its magnitude and temporal extent. Only certain naturally occurring host-microbiome pairs might meet such conditions to exploit its benefits.

Availability of data

The data generated and analysed during the current study can be simulated from the Python code available via GitHub at <https://github.com/romanzapien/microbiome-inheritance.git>

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Authors' contributions

The original model was developed in discussions between RZC, MS, and AT. RZC analysed the model, programmed the code, and wrote the initial draft. All authors interpreted the results, reviewed the manuscript, and approved the final version.

421 Competing interests

422 We declare no competing interests.

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A. Appendix

A. Supplementary methods

A.1. Deterministic and stochastic components of the model

We have introduced a model of the microbiome dynamics where we track the frequencies of a taxon i , x_i , and the set of other taxa, o_i ; together, the vector $\mathbf{x} = \{x_i, o_i\}$. In Eq. (5) we expressed the model in the form of a stochastic differential equation – that describes the microbial dynamics within

515 a host during its lifespan— where the deterministic, $\mathbf{A}[\mathbf{x}]$, and stochastic, $B[\mathbf{x}]$, contributions were
 516 introduced. Changes have magnitude $\frac{1}{N}$. The deterministic part is given by the expected change of
 517 $\mathbf{x}$ that results from the transition probabilities in Eq. (1),

$$\mathbf{A}[\mathbf{x}] = \frac{1}{N} \frac{1}{1 - \tau} \begin{bmatrix} T_{x_i+}^{o_i-} + T_{x_i+}^{o_i} - T_{x_i-}^{o_i+} - T_{x_i-}^{o_i-} \\ T_{x_i-}^{o_i+} + T_{x_i-}^{o_i} - T_{x_i+}^{o_i-} - T_{x_i+}^{o_i-} \end{bmatrix}. \quad (\text{S1})$$

518 The stochastic part is related to the matrix of covariant change of $\mathbf{x}$:

$$V[\mathbf{x}] = \frac{1}{N^2} \frac{1}{1 - \tau} \begin{bmatrix} T_{x_i+}^{o_i-} + T_{x_i+}^{o_i} + T_{x_i-}^{o_i+} + T_{x_i-}^{o_i-} & -(T_{x_i-}^{o_i+} + T_{x_i+}^{o_i-}) \\ -(T_{x_i-}^{o_i+} + T_{x_i+}^{o_i-}) & T_{x_i-}^{o_i+} + T_{x_i-}^{o_i} + T_{x_i+}^{o_i-} + T_{x_i+}^{o_i-} \end{bmatrix}. \quad (\text{S2})$$

519 $B[\mathbf{x}]$ is the matrix that satisfies $B[\mathbf{x}]^T B[\mathbf{x}] = V[\mathbf{x}]$. This is calculated analytically [34] after defining
 520 the quantities $w = \sqrt{\det(V[\mathbf{x}])}$ and $d = \sqrt{\sum_i V[i, i] + 2w}$,

$$B[\mathbf{x}] = \frac{V[\mathbf{x}] + wI}{d}, \quad (\text{S3})$$

521 where I is the identity matrix.

522 Note that Eq. (S1) and Eq. (S2) refer to the lifetime of a single host, therefore we divide by $1 - \tau$
 523 to remove it from each transition probability. We had introduced $1 - \tau$ in Eq. (1) to explain the
 524 effect of host death at the population level.

525 A.2. Condition for deterministic increase of lineage taxa

526 We start from the definition of $\mathbf{A}[1]$, Eq. (S1). This equation indicates the deterministic change of
 527 frequency of a lineage taxon (x_i) as a function of x_i , other microbes frequency (o_i), and parameters
 528 of migration (m), frequency in the pool of colonizers (p_i), and how rapidly available space is occupied
 529 (α_0). Asking under which condition $\mathbf{A}[1] > 0$, leads to

$$T_{x_i+}^{o_i-} + T_{x_i+}^{o_i} > T_{x_i-}^{o_i+} + T_{x_i-}^{o_i-}$$

530 Using the definition of the transition probabilities in Eq. (1) and simplifying, we find

$$(1 - x_i) \left((1 - m) \frac{x_i}{\alpha_0 x_0 + x_i + o_i} \right) > x_i \left(m + (1 - m) \left(1 - \frac{x_i}{\alpha_0 x_0 + x_i + o_i} \right) \right)$$

531 where we used the fact that lineage taxa are absent from the pool of colonizers, $p_i = 0$. Simplifying

532 and solving for $x_i + o_i = 1 - x_0$, we find

$$x_i + o_i < 1 - \frac{m}{1 - \alpha_0} \quad (\text{S4})$$

533 Thus, the growth of lineage taxa stops before the microbial load, $x_i + o_i$, reaches frequency 1, as

534 this is constrained by migration, m , and how rapidly available space is occupied, α_0 .

535 B. Supplementary figures

Figure Supplementary 1: Occurrence of a microbial taxon in hosts under microbial inheritance. We repeat the analysis from Fig. 2, but instead of load, $x_i + o_i$, we look into a single microbial taxon, x_i . **(A)** Starting from a condition where all hosts are initially empty, the microbial occurrence increases through time. In this particular case, inheritance increases the occurrence if hosts are colonized rapidly, $\alpha_0 \rightarrow 0$. **(B)** The hosts now contain the taxon in small frequencies. The cases shown in (A-B), with parameters $p_1 = 10^{-2}$, $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$, are indicated by the triangles in (C-F). **(C)** Changes are small for other frequencies in the pool of colonizers, p_1 , but those at intermediate values benefit the most from inheritance. **(D)** The maximum change occurs for intermediate migration from the pool of colonizers, m . For $m \rightarrow 1$ the taxon colonizes hosts even without inheritance. Instead for $m \rightarrow 0$ the taxon does not colonize the hosts. **(E)** Larger changes occur for intermediate host death probabilities, τ , and fast colonization. Long living hosts, $\tau \rightarrow 0$, contain the taxon even without inheritance. Short living hosts, $\tau \rightarrow 1$, are less likely to be colonized by the taxon within their lifetime. **(F)** In contrast to the microbial load (Fig. 2E), for a single taxon the maximum change occurs at intermediate capacities for microbes, N . The change can be negative once inheritance favours more abundant taxa competing for limited space (see C-F). Points and bars in (C-F) indicate the average and standard deviation of 6 simulation pairs, with vs. without inheritance, with 10^4 hosts each. Offspring receive 9% of their parent's microbiome on average, $a_i = 0$ and $b_i = 9$ in Eq. (4). The whole distributions are shown in Fig. Sup. 3.

Figure Supplementary 2: **Microbial load distribution across a host population, with or without microbial inheritance.** The microbial load is the set of all microbes. In contrast to the difference between distributions, Figs. 2 and 3, here the distributions are shown. The cases without and with inheritance are indicated by $\times$ and $\bullet$, respectively. Single parameters are modified from the condition $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$. The probability of occurrence and frequencies within hosts increase for (A) larger migration from the pool of colonizers, $m \rightarrow 1$, and (B) longer host lifespan, $\tau \rightarrow 0$. (C) While occurrence is constant at 1, frequencies increase for smaller capacities for microbes, N . Inheritance might increase both observables for certain parameter combinations and percentiles of the distribution (compare $\bullet$ to $\times$). The increase is evident for small percentiles. Decrease might occur for large percentiles. Only for $\tau \lesssim 2 \cdot 10^{-7}$ all hosts reach carrying capacity within their lifetime. Each simulation included 10^4 hosts and parameters $a_i = 0$ and $b_i = 9$ for inheritance, Eq. (4) – offspring receive 9% of their parent's microbiome on average – and $\alpha_0 = 0.1$ for available space occupation.

Figure Supplementary 3: **Frequency of a microbial taxon distribution across the host population, with or without inheritance.** In contrast to the difference between distributions, Figs. Sup. 1 and 4, here the distributions are shown. The cases without and with inheritance are indicated by $\times$ and $\bullet$, respectively. Single parameters are modified from the condition $p_1 = 10^{-2}$, $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$. (A) The probability of occurrence and frequency within hosts increase for higher abundances in the pool of colonizers, $p_1 \rightarrow 1$, and (B) larger migration from the environment, $m \rightarrow 1$. For $p_1 \rightarrow 0$, hosts with larger frequencies than in the pool of colonizers ($x_1 > p_1$) might occur stochastically. In contrast to microbial load (Fig. Sup. 2), inheritance might decrease the frequencies for (C) long host lifespans, $\tau \rightarrow 0$, and, (D) smaller capacities for microbes, N , where hosts are fully colonized. The reduced variability of the early microbiome, makes hosts with initially large frequencies of the microbial taxon less likely. Even if low frequencies increase, the average frequency decreases as a result. Inheritance increases the average frequency for intermediate values of τ and N , where hosts are partially colonized (Fig. Sup. 2 B-C). Each simulation included 10^4 hosts and parameters $a_i = 0$ and $b_i = 9$ for inheritance, Eq. (4) – offspring receive 9% of their parent's microbiome on average – and $\alpha_0 = 0.1$ for the available space occupation.

Figure Supplementary 4: **Average frequency of a microbial taxon in hosts under microbial inheritance.** We repeat the analysis from Fig. 3, but instead of load, $x_i + o_i$, we look into a single microbial taxon, x_i . **(A)** Starting from a condition where all hosts are initially empty, the average frequency of microbes in hosts increases through time before reaching an equilibrium. In this particular case, inheritance makes the average slightly larger if hosts are occupied more slowly, $\alpha_0 = 0.5$. Although more hosts harbour the taxon, no change occurs for $\alpha_0 = 0.1$, as inheritance reduces the variability between individuals. The cases shown in (A), with parameters $p_1 = 10^{-2}$, $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$, are indicated by the triangles in (B-E). **(B)** No changes occur for multiple frequencies in the pool of colonizers, p_1 , and **(C)** migrations from the pool of colonizers, m . **(D)** The largest changes occur for intermediate host death probabilities, τ . For long living hosts, $\tau \rightarrow 0$, the change produced by inheritance can be negative. **(E)** Similarly for small capacities for microbes, N , where inheritance causes abundant taxa to outcompete others. Points and bars in (B-E) indicate the average and standard deviation of 6 simulation pairs, with vs. without inheritance, with 10^4 hosts each. Offspring receive 9% of their parent's microbiome on average, $a_i = 0$ and $b_i = 9$ in Eq. (4). The whole distributions are shown in Fig. Sup. 3.

Figure Supplementary 5: **Difference in microbial load between 'low' and 'seed-like' inheritance.** A positive difference indicates the observable is larger for seed-like inheritance (Fig. 1B). For both, low and seed-like inheritance, offspring receive 9% of their parent's microbiome on average ($a_i = 0$ and $b_i = 9$ for low inheritance, and $a_i = 9$ and $b_i = 99$ for seed-like inheritance in Eq. (4)). Low inheritance corresponds to data shown in Fig. 2 and Fig. 3. Single parameters are modified from the condition $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$. **(A)** For low migration from the pool colonizers, $m \rightarrow 0$, seed-like inheritance increases the microbial occurrence (a exception stems from a slower occupation of available space, $\alpha_0 = 0.5$). For $m \rightarrow 1$, it mildly increases the average microbial load. **(B)** For low host death, $\tau \rightarrow 0$, this inheritance mode increases the average load importantly. For $\tau \rightarrow 1$, it only affects the occurrence, even decreasing it. **(C)** For varying carrying capacity (N), larger average loads are obtained for small N . Each point corresponds to the difference of observables calculated from simulations with 10^4 hosts. The scale of axes is logarithmic, but linear within $[-10^{-3}, 10^{-3}]$ for the average load, and $[-10^{-2}, 10^{-2}]$ for the occurrence.

Figure Supplementary 6: **Difference in the frequency of a microbial taxon between 'low' and 'seed-like' inheritance.** A positive difference indicates the observable is larger for seed-like inheritance (Fig. 1B). For both, low and seed-like inheritance, offspring receive 9% of their parent's microbiome on average ($a_i = 0$ and $b_i = 9$ for low inheritance, and $a_i = 9$ and $b_i = 99$ for seed-like inheritance in Eq. (4)). Low inheritance corresponds to data shown in Fig. Sup. 1 and Fig. Sup. 4. Single parameters are modified from the condition $p_1 = 10^{-2}$, $m = 10^{-2}$, $\tau = 10^{-4}$, and $N = 10^5$. **(A-C)** A seed-like inheritance primarily modifies the occurrence for various values of frequency in the pool of colonizers (p_i), migration (m), and host death (τ). **(D)** For varying values of the carrying capacity for microbes (N), the main change is on the occurrence, however, for small N a decrease of average frequency is observed. A decrease or increase of occurrence is not clearly attributable to the rate of host colonization (α_0). Each point corresponds to the difference of simulations with 10^4 hosts. The scale of axes is logarithmic, but linear within $[-10^{-3}, 10^{-3}]$ for the average frequency, and $[-10^{-2}, 10^{-2}]$ for the occurrence.