Blood flow modeling under LVAD physiology. From global circulation to local hemodynamics[☆]

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Abstract

This document presents the modeling strategy to address the in-silico study of different LVAD pathophysiological scenarios. The proposed approach employs a closed-loop lumped-parameter compartmental representation of the global circulation in the cardiovascular system (CVS). The CVS is coupled to a HeartMate 3 LVAD, and different cardiovascular conditions are proposed by modification of model parameters. Once the simulation for these conditions are performed, the cardiac function is analyzed in detail, and the global circulation model delivers flow rate waveforms which are employed as boundary conditions in a 3D hemodynamic simulation. This local circulation model is built using a patient-specific geometry of the aortic arch, containing 7 inlet/outlet boundaries, namely: LVAD cannula, aortic root, left and right subclavian arteries, left and right common carotid arteries and thoracic aorta. This model is exploited to investigate the impact of global cardiovascular conditions in the local hemodynamic features, particularly the wall shear stress (WSS) in different spatial regions.

Keywords: cardiovascular system, closed-loop model, Navier-Stokes equations, aortic insufficiency, cardiac function

1. Introduction

The methodology is split into two phases. First, we built a closed-loop model of the cardiovascular system to analyze global circulatory phenomena, with emphasis in the cardiac performance and its interaction with the LVAD. Second, we retrieved the hemodynamic conditions, specifically blood flow rates through the LVAD cannula and aortic root, and used them as boundary conditions to perform 3D simulations using a patient-specific geometric model of the aortic arch.

The cardiovascular model developed in the present study has been specifically tailored for the present application of cardiovascular physiology coupled to LVAD function. Nevertheless, such a model shares many components with models available in the literature. Table 1 presents the supporting bibliographic works that have been employed in the instantiation of both the global and local circulation models. These bibliographic references share similar modeling ingredients, and they served to guide the parameter selection in the present investigation.

2. Global circulation model

2.1. Closed-loop representation and notation

The global circulation model consists of a set of inter-connected compartments whose dynamics is characterized by a set of ordinary differential equations. Figure 1 schematically illustrates the compartments that form the closed-loop representation of the CVS.

Global circulation model		
Ingredient	Section	References
Closed loop representation	2.1	[1, 2]
Cardiac chamber equations and parameters	2.2	[1, 2, 3]
Valve equations and parameters	2.3	[1, 4, 5]
Arterial blood flow equations	2.4	[1, 2]
Venous blood flow equations	2.5	[1, 2]
Pulmonary blood flow equations	2.6	[1, 2]
Post-processing	2.9	[6]
Local circulation model		
3D Model geometry	3.1	[7]
3D Model equations	3.2	[8, 9]
Post-processing	3.4	[8]

Table 1: Supporting bibliographic references for chosen techniques and parameter selection in the different components of the present model.

Figure 1: Closed-loop model of the CVS. Red: arterial compartments. Blue: venous compartments. Light blue: valve compartments. Orange: cardiac compartments. Lime: septal compartments. Yellow: LVAD compartment.

The main common variables across the closed-loop system are the blood pressure, denoted by P , and the flow rate, denoted by Q . In the cardiac chambers, and in the cardiac valves, chamber volume, denoted by V , and valvel opening angle, denoted by θ , are also described by the system of equations

In the system illustrated in Figure 1, the following notational convention is used concerning indexes

- RA, LA, RV, LV: right/left atria, right/left ventricles
- AS, VS: atrial septum, ventricular septum
- TrV, PuV, MiV, AoV: tricuspid, pulmonary, mitral, aortic valves
- pa, pv: pulmonary arteries/veins
- LVAD: left ventricular assist device
- lccsi, rccsi, lccs, rccs, lccp, rccp: left/right common carotid systemic inlet, left/right common carotid systemic, left/right common carotid peripheral
- lssi, rssi, lss, rss, lsp, rsp: left/right subclavian systemic inlet, left/right subclavian systemic, left/right subclavian peripheral
- dasi, das, dap: descending aorta systemic inlet, descending aorta systemic, descending aorta peripheral
- ubve, lbve, ubv, lbv, svc, ivc: upper/lower body venules, upper/lower body veins, superior/inferior vena cava
- u, d: upstream and downstream (circulation-wise), respectively; these indexes are used to characterize connectivity with upstream and downstream components

The model descriptive capabilities in terms of hemodynamic variables are described in Table 2, including pressure, flow rate quantities, chamber volume and valve opening angle unknowns. Table 3 describes the connectivities across the entire closed-loop system, which allow to write the equations to be presented below in a more compact way. In turn, the list of parameters, including their specific physical significance, is presented in Section 4.

2.2. Cardiac chamber equations

The pressure-volume relation for the cardiac chambers are the following

$$P_{SC} = P_{ex} + E_{SC}(t)(V_{SC} - V_{SC}^0) + \alpha P_{SC} \frac{dV_{SC}}{dt} + K_{sep}^{SC}(t)P_{\dot{S}C} \quad S \in \{R, L\}, C \in \{A, V\}, \quad (1)$$

where $\dot{R} = L$ and $\dot{L} = R$.

The cardiac elastances are defined by means of proper activation functions, and are coupled through the septal interaction

$$E_{SC}(t) = E_{sep}^C(t)K_{sep}^{SC}(t) \quad S \in \{R, L\}, C \in \{A, V\}, \quad (2)$$

where the septal inter-atria and inter-ventricular interactions are defined as follows

$$E_{sep}^C(t) = \kappa_{sep}^{RC}E_{RC}^0(t) + \kappa_{sep}^{LC}E_{LC}^0(t) \quad C \in \{A, V\}, \quad (3)$$

$$K_{sep}^{SC}(t) = \frac{E_{SC}^0(t)}{E_{sep}^C(t) + E_{SC}^0(t)} \quad S \in \{R, L\}, C \in \{A, V\}. \quad (4)$$

The native chamber elastances are given by

$$E_{SC}^0(t) = E_A^{SC}e_{SC}(t) + E_B^{SC} \quad S \in \{R, L\}, C \in \{A, V\}, \quad (5)$$

Pressure unknowns			equation	Flow rate unknowns			equation
P_{RA}	right atrium	(1)		Q_{TrV}	tricuspid valve	(9)	
P_{RV}	right ventricle	(1)		Q_{PuV}	pulmonary valve	(9)	
P_{LA}	left atrium	(1)		Q_{MiV}	mitral valve	(9)	
P_{LV}	left ventricle	(1)		Q_{AoV}	aortic valve	(9)	
P_{sa}	systemic arterial	(14)		Q_{LVAD}	LVAD	(24)	
P_{lccs}	left common carotid systemic	(17)		Q_{lccsi}	left common carotid systemic inlet	(15)	
P_{rccs}	right common carotid systemic	(17)		Q_{lccs}	left common carotid systemic	(16)	
P_{lss}	left subclavian systemic	(17)		Q_{lccp}	left common carotid peripheral	(18)	
P_{rss}	right subclavian systemic	(17)		Q_{rccsi}	right common carotid systemic inlet	(15)	
P_{das}	descending aorta systemic	(17)		Q_{rccs}	right common carotid systemic	(16)	
P_{lccp}	left common carotid peripheral	(19)		Q_{rccp}	right common carotid peripheral	(18)	
P_{rccp}	right common carotid peripheral	(19)		Q_{lssi}	left subclavian systemic inlet	(15)	
P_{lsp}	left subclavian peripheral	(19)		Q_{lss}	left subclavian systemic	(16)	
P_{rsp}	right subclavian peripheral	(19)		Q_{lsp}	left subclavian peripheral	(18)	
P_{dap}	descending aorta peripheral	(19)		Q_{rssi}	right subclavian systemic inlet	(15)	
P_{ubve}	upper body venules	(21)		Q_{rss}	right subclavian systemic	(16)	
P_{ubv}	upper body veins	(21)		Q_{rsp}	right subclavian peripheral	(18)	
P_{svc}	superior vena cava	(21)		Q_{dasi}	descending aorta systemic inlet	(15)	
P_{lbve}	lower body venules	(21)		Q_{das}	descending aorta systemic	(16)	
P_{lbv}	lower body veins	(21)		Q_{dap}	descending aorta peripheral	(18)	
P_{ivc}	inferior vena cava	(21)		Q_{ubve}	upper body venules	(20)	
P_{pa}	pulmonary arteries	(23)		Q_{ubv}	upper body veins	(20)	
P_{pv}	pulmonary veins	(23)		Q_{svc}	superior vena cava	(20)	
				Q_{lbve}	lower body venules	(20)	
				Q_{lbv}	lower body veins	(20)	
				Q_{ivc}	inferior vena cava	(20)	
				Q_{pa}	pulmonary arteries	(22)	
				Q_{pv}	pulmonary veins	(22)	

Volume unknowns			equation	Opening angle unknowns			equation
V_{RA}	right atrium	(8)		φ_{TrV}	tricuspid valve	(11)	
V_{RV}	right ventricle	(8)		φ_{PuV}	pulmonary valve	(11)	
V_{LA}	left atrium	(8)		φ_{MiV}	mitral valve	(11)	
V_{LV}	left ventricle	(8)		φ_{AoV}	aortic valve	(11)	

Table 2: Unknowns corresponding to the blood pressure, flow rate, chamber volume and valve opening angle across the different compartments of the closed-loop CVS system.

where the atrial and ventricular activation functions are

$$e_{SA}(t) = \begin{cases} \frac{1}{2} (1 + \cos(\pi \frac{t+T-t_{ar}^{SA}}{T_{ar}^{SA}})) & \text{if } 0 \leq t \leq t_{ar}^{SA} + T_{ar}^{SA} - T, \\ 0 & \text{if } t_{ar}^{SA} + T_{ar}^{SA} - T < t \leq t_{ac}^{SA}, \\ \frac{1}{2} (1 - \cos(\pi \frac{t-t_{ac}^{SA}}{T_{ac}^{SA}})) & \text{if } t_{ac}^{SA} < t \leq t_{ac}^{SA} + T_{ac}^{SA}, \\ \frac{1}{2} (1 + \cos(\pi \frac{t-t_{ar}^{SA}}{T_{ar}^{SA}})) & \text{otherwise,} \end{cases} \quad S \in \{R, L\}, \quad (6)$$

$$e_{SV}(t) = \begin{cases} \frac{1}{2} (1 - \cos(\pi \frac{t}{T_{vc}^{SV}})) & \text{if } 0 \leq t \leq T_{vc}^{SV}, \\ \frac{1}{2} (1 + \cos(\pi \frac{t-T_{vc}^{SV}}{T_{vr}^{SV}})) & \text{if } T_{vc}^{SV} < t \leq T_{vc}^{SV} + T_{vr}^{SV}, \\ 0 & \text{otherwise,} \end{cases} \quad S \in \{R, L\}. \quad (7)$$

The mass conservation equations in the cardiac chambers read

$$\frac{dV_{SC}}{dt} = Q_{SC}^u - Q_{SC}^d \quad S \in \{R, L\}, C \in \{A, V\}, \quad (8)$$

where the upstream and downstream connectivities are given in Table 3.

2.3. Valve equations

The governing equations for the blood flow across the cardiac valves are the following (note the constraints defined in (13))

$$\begin{cases} L_V \frac{dQ_V}{dt} + R_V Q_V + B_V |Q_V| Q_V = \Theta_V (P_V^u - P_V^d) & \text{if } P_V^u > P_V^d, \\ Q_V = 0 & \text{otherwise,} \end{cases} \quad V \in \{TrV, PuV, MiV, AoV\}, \quad (9)$$

Quantity	connectivity x	
	u	d
P_{TrV}^x	P_{RA}	P_{RV}
P_{PuV}^x	P_{RV}	P_{pa}
P_{MiV}^x	P_{LA}	P_{LV}
P_{AoV}^x	P_{LV}	P_{sa}
P_{lccs}^x	P_{lccs}	P_{lccp}
P_{rccs}^x	P_{rccs}	P_{rccp}
P_{lss}^x	P_{lss}	P_{lsp}
P_{rss}^x	P_{rss}	P_{rsp}
P_{das}^x	P_{das}	P_{dap}
P_{lccp}^x	P_{lccp}	P_{ubve}
P_{rccp}^x	P_{rccp}	P_{ubve}
P_{lsp}^x	P_{lsp}	P_{ubve}
P_{rsp}^x	P_{rsp}	P_{ubve}
P_{dap}^x	P_{dap}	P_{lbve}
P_{ubve}^x	P_{ubve}	P_{ubv}
P_{ubv}^x	P_{ubv}	P_{svc}
P_{svc}^x	P_{svc}	P_{RA}
P_{lbve}^x	P_{lbve}	P_{lbv}
P_{lbv}^x	P_{lbv}	P_{ivc}
P_{ivc}^x	P_{ivc}	P_{RA}
P_{pa}^x	P_{pa}	P_{pv}
P_{pv}^x	P_{pv}	P_{LA}

Quantity	connectivity x	
	u	d
Q_{RA}^x	$Q_{svc} + Q_{ivc}$	Q_{TrV}
Q_{RV}^x	Q_{TrV}	Q_{PuV}
Q_{LA}^x	Q_{pv}	Q_{MiV}
Q_{LV}^x	Q_{MiV}	Q_{AoV}
Q_{lccs}^x	Q_{lccsi}	Q_{lccs}
Q_{rccs}^x	Q_{rccsi}	Q_{rccs}
Q_{lss}^x	Q_{lssi}	Q_{lss}
Q_{rss}^x	Q_{rssi}	Q_{rss}
Q_{das}^x	Q_{dasi}	Q_{das}
Q_{lccp}^x	Q_{lccs}	Q_{lccp}
Q_{rccp}^x	Q_{rccs}	Q_{rccp}
Q_{lsp}^x	Q_{lss}	Q_{lsp}
Q_{rsp}^x	Q_{rss}	Q_{rsp}
Q_{dap}^x	Q_{das}	Q_{dap}
Q_{ubve}^x	$Q_{lccp} + Q_{rccp} + Q_{lsp} + Q_{rsp}$	Q_{ubve}
Q_{ubv}^x	Q_{ubve}	Q_{ubv}
Q_{svc}^x	Q_{ubv}	Q_{svc}
Q_{lbve}^x	Q_{dap}	Q_{lbve}
Q_{lbv}^x	Q_{lbve}	Q_{lbv}
Q_{ivc}^x	Q_{lbv}	Q_{ivc}
Q_{pa}^x	Q_{PuV}	Q_{pa}
Q_{pv}^x	Q_{pa}	Q_{pv}

Table 3: Upstream and downstream connectivities for pressure and flow rate variables in the closed-loop system from Figure 1.

where the orifice coefficients are defined through the opening angles as follows

$$\Theta_V = \left(\frac{1 - \cos \varphi_V}{1 - \cos \varphi_V^{\max}} \right)^2 \quad V \in \{TrV, PuV, MiV, AoV\}. \quad (10)$$

In turn, the governing equations for the valve opening angles are the following

$$I^V \frac{d^2 \varphi_V}{dt^2} + k_F^V \frac{d \varphi_V}{dt} = k_P^V (P_V^u - P_V^d) \cos \varphi_V + k_Q^V Q_V \cos \varphi_V - F_V, \quad V \in \{TrV, PuV, MiV, AoV\}, \quad (11)$$

where

$$F_V = \begin{cases} k_V^V Q_V \sin(2\varphi_V) & \text{if } Q_V > 0, \\ 0 & \text{otherwise,} \end{cases} \quad V \in \{TrV, PuV, MiV, AoV\}. \quad (12)$$

Finally, the valve opening angle is constrained to be in a certain range, as follows

$$\varphi_V = \begin{cases} \varphi_V^{\min} & \text{if } \varphi_V < \varphi_V^{\min}, \\ \varphi_V^{\max} & \text{if } \varphi_V > \varphi_V^{\max}, \end{cases} \quad V \in \{TrV, PuV, MiV, AoV\}. \quad (13)$$

2.4. Arterial blood flow equations

At the entrance of the arterial system, where the LVAD and the aortic root discharge blood into the five systemic territories, the following equations hold

$$Q_{AoV} + Q_{LVAD} = \sum_{t \in \mathcal{T}} Q_{tsi} \quad \mathcal{T} = \{lcc, rcc, ls, rs, da\}, \quad (14)$$

$$P_{ts} = P_{sa} \quad t \in \{lcc, rcc, ls, rs, da\}. \quad (15)$$

Conservation of momentum in systemic arterial compartments is governed by the following equations

$$L_{ts} \frac{dQ_{ts}}{dt} + R_{ts} Q_{ts} = P_{ts}^u - P_{ts}^d \quad t \in \{lcc, rcc, ls, rs, da\}. \quad (16)$$

Mass conservation in the systemic territories is governed by the following equations

$$C_{ts} \frac{dP_{ts}}{dt} = Q_{ts}^u - Q_{ts}^d \quad t \in \{lcc, rcc, ls, rs, da\}. \quad (17)$$

The five peripheral beds, connected to the corresponding systemic compartments, are modeled using similar expressions. Thas is, for the conservation of momentum

$$L_{tp} \frac{dQ_{tp}}{dt} + R_{tp} Q_{tp} = P_{tp}^u - P_{tp}^d \quad t \in \{lcc, rcc, ls, rs, da\}, \quad (18)$$

and for the conservation of mass

$$C_{tp} \frac{dP_{tp}}{dt} = Q_{tp}^u - Q_{tp}^d \quad t \in \{lcc, rcc, ls, rs, da\}. \quad (19)$$

2.5. Venous blood flow equations

The blood flow equations for the venous compartments are analogous to those employed in the arterial side. For the upper and lower body regions, the following momentum conservation equations for each of the six compartments are employed

$$L_r \frac{dQ_r}{dt} + R_r Q_r = P_r^u - P_r^d \quad r \in \{ubve, ubv, svc, lbve, lbv, ivc\}, \quad (20)$$

and for the mass conservation it is

$$C_r \frac{dP_r}{dt} = Q_r^u - Q_r^d \quad r \in \{ubve, ubv, svc, lbve, lbv, ivc\}. \quad (21)$$

2.6. Pulmonary blood flow equations

Conservation of momentum in the pulmonary arteries and veins is governed by the following equations

$$L_q \frac{dQ_q}{dt} + R_q Q_q = P_q^u - P_q^d \quad q \in \{pa, pv\}, \quad (22)$$

and the corresponding equations for the mass conservation are

$$C_q \frac{dP_q}{dt} = Q_q^u - Q_q^d \quad q \in \{pa, pv\}. \quad (23)$$

2.7. LVAD performance

The LVAD performance is characterized through a pressure-flow rate relation corresponding to a Heart-Mate 3 device. This non-linear function is expressed as follows

$$Q_{LVAD} = \mathcal{F}(P_{sa} - P_{LV}, S_{LVAD}). \quad (24)$$

Starting from a set of pairs $\{(P_{sa}^k - P_{LV}^k, S_{LVAD}^k)\}_{0 \leq k \leq N_K}$, N_K the number of data points, a regression strategy was utilized to model the relation $\mathcal{F}$, and the resulting relations are shown in Figure 2.

2.8. Simulation

The initial condition for the model is a physiological initial guess, and a total of ten cardiac cycles is run to guarantee that the model reached a periodic regime.

The global circulation model is discretized in time using a fully implicit backward Euler scheme. Non-linearities are treated using Picard iterations. The discrete model describes the temporal dynamims of the 59 unknowns in the problem. At each time-step, the resulting linear system of algebraic equations is solved using LU factorization. The global circulation model is run in a laptop, and takes less than 2 minutes to simulate 10 cardiac cycles.

Figure 2: Pressure-flow rate relations at different LVAD speeds. These curved correspond to a HeartMate 3 device. There is a jump of 300 rpm in LVAD speed between consecutive curves.

2.9. Post-processing

Once the simulations are finished, we take the last cardiac cycle and compute several quantities of interest that help to characterize the cardiac function and the cardiovascular system as a whole. The list of quantities of interest is given in Table 4. Figure 3 illustrates some PV loops for RV and LV, with the corresponding landmarks that play a role in the processing of cardiac variables.

Figure 3: Prototypical pressure-volume loops for RV and LV, with the corresponding landmark points that play a role in the characterization of the cardiac function.

left/right ventricle (SV, S ∈ {R, L}) - computed using P _{SV} -V _{SV} loop		
description	symbol	equation
ventricular end-systolic elastance	E_{esSV}	(25)
effective pulmonary/systemic arterial elastance	E_{aSV}	(28)
ventricular-arterial elastance ratio	$F_{SV}^{es/a}$	(29)
ventricular stroke work	SW_{SV}	(30)
end-systolic potential energy	PE_{SV}	(31)
pressure-volume area	PVA_{SV}	(32)
myocardial O ₂ consumption	MVO_{2SV}	(33)
ventricular efficiency	Eff_{SV}	(34)

pressure and flow rate indicators obtained from querying model variables		
description	symbol	equation
mean systemic arterial pressure	$\bar{P}_{sa}$	(35)
systolic systemic arterial pressure	P_{sa}^{max}	(36)
diastolic systemic arterial pressure	P_{sa}^{min}	(37)
mean pulmonary arterial pressure	$\bar{P}_{pa}$	(38)
systolic pulmonary arterial pressure	P_{pa}^{max}	(39)
diastolic pulmonary arterial pressure	P_{pa}^{min}	(40)
mean transvalvular pressure gradient	ΔP_{AoV}	(41)
mean aortic flow rate	$\bar{Q}_{AoV}$	(42)
mean LVAD flow rate	$\bar{Q}_{LVAD}$	(43)
volumetric aortic backflow	V_{AoV}^{back}	(45)
regurgitant fraction	RF	(46)

Table 4: List of properties that characterize the cardiac function and the cardiovascular system.

From the RV and LV pressure-volume loops we compute the following quantities for $S \in \{R, L\}$

$$E_{esSV} = C_P \max_{t \in [0, T]} \frac{P_{SV}(t)}{V_{SV}(t) - V_{SV}^0}, \quad (25)$$

$$t_{x,SV} = \arg \max_{t \in [0, T]} \frac{P_{SV}(t)}{V_{SV}(t) - V_{SV}^0}, \quad (26)$$

$$V_{SV}^{max} = \max_{t \in [0, T]} V_{SV}(t), \quad (27)$$

$$E_{aSV} = C_P \frac{P_{SV}(t_{x,SV})}{V_{SV}^{max} - V_{SV}(t_{x,SV})}, \quad (28)$$

$$F_{SV}^{es/a} = \frac{E_{esSV}}{E_{aSV}}, \quad (29)$$

$$SW_{SV} = C_P \int_0^T P_{SV} \frac{dV_{SV}}{dt} dt, \quad (30)$$

$$PE_{SV} = C_P \int_0^U P_{SV}^{PE} \frac{dV_{SV}^{PE}}{du} du, \quad (31)$$

$$PVA_{SV} = SW_{SV} + PE_{SV}, \quad (32)$$

$$MVO_{2SV} = C_1 PVA_{SV} + C_2 E_{esSV} + C_3, \quad (33)$$

$$Eff_{SV} = \frac{C_{J_2}}{C_{J_1}} \frac{SW_{SV}}{MVO_{2SV}}. \quad (34)$$

In (31), we define the parametric curves P_{SV}^{PE} and V_{SV}^{PE} as those curves formed by connecting the points $(V_{SV}^0, 0)$, $(V_{SV}(t_{y,SV}), P_{SV}^{min})$ and $(V_{SV}(t_{x,SV}), P_{SV}(t_{x,SV}))$ in Figure 3.

Parameters C_1 and C_2 in equation (33) are defined in Table 5. Also in that table, we report the parameters that play a role in the unit conversion process.

Also, from the results, we obtain the following values, converted to units of mmHg, corresponding to

description	symbol	value	units
pressure unit transformation coefficient	C_P	1.0/1333.32	(mmHg)/(dyn/cm ²)
flow rate unit transformation coefficient	C_Q	60/1000	(l/min)/(cm ³ /s)
oxygen consumption constant	C_1	$2.1 \cdot 10^{-5}$	mlO ₂ /(mmHg·ml)
oxygen consumption constant	C_2	$3.2 \cdot 10^{-3}$	(mlO ₂ /beat) · (ml/mmHg)
oxygen consumption constant	C_3	$1.04 \cdot 10^{-2}$	mlO ₂ /beat
Joule transformation coefficient 1	C_{J_1}	20.0	J/(mlO ₂ /beat)
Joule transformation coefficient 2	C_{J_2}	$1.33 \cdot 10^{-4}$	J/(mmHg·ml)

Table 5: Parameters that characterize the computation of derived quantities of interest in the analysis of the cardiac function.

the mean, maximum and minimum systemic and pulmonary arterial pressures

$$\bar{P}_{sa} = \frac{C_P}{T} \int_0^T P_{sa} dt, \quad (35)$$

$$P_{sa}^{\max} = C_P \max_{t \in [0, T]} P_{sa}(t), \quad (36)$$

$$P_{sa}^{\min} = C_P \min_{t \in [0, T]} P_{sa}(t), \quad (37)$$

$$\bar{P}_{pa} = \frac{C_P}{T} \int_0^T P_{pa} dt, \quad (38)$$

$$P_{pa}^{\max} = C_P \max_{t \in [0, T]} P_{pa}(t), \quad (39)$$

$$P_{pa}^{\min} = C_P \min_{t \in [0, T]} P_{pa}(t), \quad (40)$$

$$\Delta P_{AoV} = \frac{C_P}{T} \int_0^T (P_{sa} - P_{LV}) dt. \quad (41)$$

Analogously, we compute the mean flow rate through the aortic root, and through the LVAD, converted to units of l/min

$$\bar{Q}_{AoV} = \frac{C_Q}{T} \int_0^T Q_{AoV} dt, \quad (42)$$

$$\bar{Q}_{LVAD} = \frac{C_Q}{T} \int_0^T Q_{LVAD} dt. \quad (43)$$

The resulting volumetric backflow through the aortic valve is computed as follows

$$Q_{AoV}^- = \begin{cases} 0 & \text{if } Q_{AoV} > 0, \\ Q_{AoV} & \text{otherwise,} \end{cases} \quad (44)$$

$$V_{AoV}^{\text{back}} = \int_0^T Q_{AoV}^- dt. \quad (45)$$

The regurgitant fraction (RF) is defined as follows

$$\text{RF} = -\frac{\bar{Q}_{AoV}}{\bar{Q}_{LVAD}}. \quad (46)$$

Note that since RF is defined whenever $\bar{Q}_{AoV} < 0$, and in that case $\text{RF} > 0$.

3. Local circulation model

3.1. 3D Model geometry

The mathematical model to simulate the the local blood flow occurring in the proximal aorta and its branches is given by the Navier-Stokes equations. Let Ω be the vascular domain (proximal aorta including

major branches) and let Γ be its boundary, which is divided into different parts as follows

- Γ_L : the lateral wall (endothelial wall),
- Γ_{LVAD} : the boundary corresponding to the LVAD cannula
- Γ_{AoV} : the boundary corresponding to the aortic root, right after the aortic valve
- Γ_{lccsi} : the boundary corresponding to the inlet of the left common carotid systemic territory
- Γ_{rccsi} : the boundary corresponding to the inlet of the left common carotid systemic territory
- Γ_{lssi} : the boundary corresponding to the inlet of the left subclavian systemic territory
- Γ_{rssi} : the boundary corresponding to the inlet of the right subclavian systemic territory
- Γ_{dasi} : the boundary corresponding to the inlet of the descending aorta systemic territory

The outward unit normal vector to the boundary is denoted by $\mathbf{n}$. Figure 4 illustrates, over the left, the geometry of the proximal aorta and the basic local circulation model ingredients, and over the right the division of the endothelial surface into four major regions for analysis.

Figure 4: Patient-specific vascular geometry of the proximal aorta, connected to the LVAD through a 14mm cannula, with its major branches, and division of lateral endothelial wall into four major regions (c: cannula, aa: ascending aorta, ab: aortic branches and da: descending aorta) for analysis.

3.2. 3D Model equations

Let $p(t, \mathbf{x})$ (scalar-valued field) and $\mathbf{v}(t, \mathbf{x})$ (vector-valued field) be the 3D dimensional functions that describe, respectively, the blood pressure and the blood velocity for all coordinate points $\mathbf{x}$ in Ω along time t . The blood flow is assumed to be incompressible, blood is assumed to behave as a Newtonian fluid, and we neglect the gravity and turbulence effects. The Navier-Stokes equations read

$$\rho \frac{\partial \mathbf{v}}{\partial t} + \rho(\nabla \mathbf{v})\mathbf{v} = -\nabla p + \mu \Delta \mathbf{v} \quad \text{in } \Omega, \quad (47)$$

$$\text{div } \mathbf{v} = 0 \quad \text{in } \Omega. \quad (48)$$

The problem is fully described once proper initial conditions and boundary conditions are prescribed. As initial conditions we prescribe null velocity

$$\mathbf{v} = \mathbf{0} \quad \text{at } t = 0, \text{ in } \Omega. \quad (49)$$

Boundary conditions must be prescribed for all the parts that describe the boundary. Over the lateral wall we assume no-slip flow. At the cannula boundary and at the aortic root, we prescribe the flow rate given by the global circulation model under the different simulation protocols that characterize the cardiovascular conditions of interest in the present study (see Section 4).

$$\mathbf{v} = \mathbf{0} \quad \text{over } \Gamma_L, \quad (50)$$

$$\int_{\Gamma_{LVAD}} \mathbf{v} \cdot \mathbf{n} d\Gamma = -Q_{LVAD} \quad \text{at } \Gamma_{LVAD}, \quad (51)$$

$$\int_{\Gamma_{AoV}} \mathbf{v} \cdot \mathbf{n} d\Gamma = -Q_{AoV} \quad \text{at } \Gamma_{AoV}, \quad (52)$$

$$-p\mathbf{n} + \mu(\nabla\mathbf{v} + \nabla\mathbf{v}^T)\mathbf{n} = R_t^{\text{tot}} \left(\int_{\Gamma_{tsi}} \mathbf{v} \cdot \mathbf{n} d\Gamma \right) \mathbf{n} \quad \text{at } \Gamma_{tsi}, t \in \{\text{lcc, rcc, ls, rs, da}\}. \quad (53)$$

The second and third boundary conditions are called defective boundary conditions. Together with such boundary data, we assume that the traction vectors associated to the flow rate constraints are uniform at Γ_{LVAD} and at Γ_{AoV} , correspondingly.

3.3. Simulation

The initial condition for the model is a resting condition (null blood velocity). Three cardiac cycles are simulated to ensure that the model reaches a periodic regime. The local circulation model is discretized in time using a fully implicit backward Euler scheme, and in space using the finite element method, with equal order interpolation for pressure and velocity, with the velocity space enriched through bubble functions (mini-element). Non-linearities are treated using Picard iterations. Spatial discretization is accomplished by using a tetrahedral mesh with boundary layer elements (X layers). The number of tetrahedra, and degrees of freedom in the problem are 10430016 and 6933796, respectively. The resulting algebraic system of equations is solved using GMRES method, with an overlapping additive Schwarz preconditioner. The local circulation model is run using a distributed computing paradigm in a supercomputer, using 480 computing cores, and takes on average 8 hours to simulate 1 cardiac cycle.

3.4. Post-processing

Once the simulations are finished, we take the velocity field $\mathbf{v}$ in the last cardiac cycle and compute the shear stress over the endothelial wall, that is

$$\boldsymbol{\tau}_w = \mu(\nabla\mathbf{v} + \nabla\mathbf{v}^T)\mathbf{n} \quad \text{over } \Gamma_L. \quad (54)$$

Then, we average the shear stress along the cardiac period T , as follows

$$\bar{\boldsymbol{\tau}}_w = \frac{1}{T} \int_0^T \boldsymbol{\tau}_w dt. \quad (55)$$

This vector field is analyzed in four large regions within the geometric model, as illustrated in Figure 4. These regions are

- Γ_c : cannula
- Γ_{aa} : ascending aorta
- Γ_{ab} : aortic branches
- Γ_{da} : descending aorta

Thus, we compute the average of the time-averaged shear stress field, $\bar{\tau}_w$, in these four endothelial surfaces, and then we compute the magnitude of the resulting vector value, that is

$$\text{WSS}_f = \frac{1}{|\Gamma_f|} \left| \int_{\Gamma_f} \bar{\tau}_w d\Gamma \right| \quad f \in \{c, aa, ab, da\}, \quad (56)$$

where $|\Gamma_f|$, denotes the endothelial area corresponding to the f region (cannula, ascending aorta, aortic branches and descending aorta).

4. Simulation protocols

4.1. Reference parameters

The entire list of reference parameters is split into several tables. These parameters are properly modified to create the different cardiovascular conditions of interest for the present study.

These are: Table 6 for cardiac chambers, Table 7 for cardiac valves, Table 8 for opening angle dynamics, Table 9 for systemic arterial territories, Table 10 for venous systemic regions, Table 11 for pulmonary arterial and venous circulations, and Table 12 for the LVAD.

Cardiac chamber parameters			
description	symbol	value	units
external cardiac pressure	P_{ex}	0.0	dyn/cm ²
cardiac viscoelasticity	α	$5.0 \cdot 10^{-4}$	s/cm ³
cardiac period	T	1.0	s
right atrium relaxed volume	V_{RA}^0	4.0	cm ³
right ventricle relaxed volume	V_{RV}^0	10.0	cm ³
left atrium relaxed volume	V_{LA}^0	4.0	cm ³
left ventricle relaxed volume	V_{LV}^0	5.0	cm ³
right atrium proportional elastance	E_{A}^{RA}	40.0	dyn/cm ⁵
right atrium baseline elastance	E_{B}^{RA}	153.0	dyn/cm ⁵
right ventricle proportional elastance	E_{A}^{RV}	350.0	dyn/cm ⁵
right ventricle baseline elastance	E_{B}^{RV}	119.0	dyn/cm ⁵
left atrium proportional elastance	E_{A}^{LA}	45.0	dyn/cm ⁵
left atrium baseline elastance	E_{B}^{LA}	204.0	dyn/cm ⁵
left ventricle proportional elastance	E_{A}^{LV}	1750.0	dyn/cm ⁵
left ventricle baseline elastance	E_{B}^{LV}	170.0	dyn/cm ⁵
right atrium septal coupling	$\kappa_{\text{sep}}^{\text{RA}}$	2.0	—
right ventricle septal coupling	$\kappa_{\text{sep}}^{\text{RV}}$	6.0	—
left atrium septal coupling	$\kappa_{\text{sep}}^{\text{LA}}$	2.0	—
left ventricle septal coupling	$\kappa_{\text{sep}}^{\text{LV}}$	6.0	—
right atrium relaxation time	$t_{\text{ar}}^{\text{RA}}$	0.97	s
right atrium relaxation period	$T_{\text{ar}}^{\text{RA}}$	0.17	s
right atrium contraction time	$t_{\text{ac}}^{\text{RA}}$	0.80	s
right atrium contraction period	$T_{\text{ac}}^{\text{RA}}$	0.17	s
right ventricle relaxation time	$t_{\text{ar}}^{\text{RV}}$	0.15	s
right ventricle contraction period	$T_{\text{ac}}^{\text{RV}}$	0.34	s
left atrium relaxation time	$t_{\text{ar}}^{\text{LA}}$	0.97	s
left atrium relaxation period	$T_{\text{ar}}^{\text{LA}}$	0.17	s
left atrium contraction time	$t_{\text{ac}}^{\text{LA}}$	0.80	s
left atrium contraction period	$T_{\text{ac}}^{\text{LA}}$	0.17	s
left ventricle relaxation time	$t_{\text{ar}}^{\text{LV}}$	0.15	s
left ventricle contraction period	$T_{\text{ac}}^{\text{LV}}$	0.34	s

Table 6: Description of model parameters that characterize the cardiac chamber compartments.

The model parameters and boundary conditions for the local circulation model are described in Table 13.

4.2. Cardiovascular conditions

Parameters reported in the tables described above are mostly shared by the two physiological conditions involving the right ventricle (RV) considered in the present study, these are: coupled and uncoupled RV. The RV was deemed to be uncoupled when the ratio of RV end-systolic elastance (E_{es}) relative to the pulmonary effective arterial elastance (E_{a}) was $\frac{E_{\text{es}}}{E_{\text{a}}} < 0.7$ and coupled when the RV ratio satisfied

Cardiac valve parameters			
description	symbol	value	units
tricuspid flow inertance	L_{TrV}	$5.0 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
pulmonary flow inertance	L_{PuV}	$5.0 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
mitral flow inertance	L_{MiV}	$5.0 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
aortic flow inertance	L_{AoV}	$5.0 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
tricuspid flow resistance	R_{TrV}	$6.0 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}/\text{cm}^5$
pulmonary flow resistance	R_{PuV}	$6.0 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}/\text{cm}^5$
mitral flow convectance	B_{MiV}	$6.0 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}/\text{cm}^5$
aortic flow resistance	R_{AoV}	$6.0 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}/\text{cm}^5$
tricuspid flow convectance	B_{TrV}	$6.40 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}^2/\text{cm}^8$
pulmonary flow convectance	B_{PuV}	$7.56 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}^2/\text{cm}^8$
mitral flow resistance	R_{MiV}	$6.40 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}^2/\text{cm}^8$
aortic flow convectance	B_{AoV}	$7.56 \cdot 10^{-3}$	$\text{dyn}\cdot\text{s}^2/\text{cm}^8$

Table 7: Description of model parameters that characterize the cardiac valve compartments.

Opening angle parameters			
description	symbol	value	units
tricuspid valve moment of inertia	I_{TrV}	0.0	$\text{g}\cdot\text{cm}^2$
pulmonary valve moment of inertia	I_{PuV}	0.0	$\text{g}\cdot\text{cm}^2$
mitral valve moment of inertia	I_{MiV}	0.0	$\text{g}\cdot\text{cm}^2$
aortic valve moment of inertia	I_{AoV}	0.0	$\text{g}\cdot\text{cm}^2$
tricuspid orifice viscosity	k_{TrV}^F	5.0	$\text{g}\cdot\text{cm}^2/\text{s}$
pulmonary orifice viscosity	k_{PuV}^F	5.0	$\text{g}\cdot\text{cm}^2/\text{s}$
mitral orifice viscosity	k_{MiV}^F	5.0	$\text{g}\cdot\text{cm}^2/\text{s}$
aortic orifice viscosity	k_{AoV}^F	5.0	$\text{g}\cdot\text{cm}^2/\text{s}$
tricuspid orifice pressure	k_{TrV}^P	50.0	cm^3
pulmonary orifice pressure	k_{PuV}^P	50.0	cm^3
mitral orifice pressure	k_{MiV}^P	50.0	cm^3
aortic orifice pressure	k_{AoV}^P	50.0	cm^3
tricuspid orifice acceleration 1	k_{TrV}^Q	2.0	$\text{g}/\text{cm}/\text{s}$
pulmonary orifice acceleration 1	k_{PuV}^Q	2.0	$\text{g}/\text{cm}/\text{s}$
mitral orifice acceleration 1	k_{MiV}^Q	2.0	$\text{g}/\text{cm}/\text{s}$
aortic orifice acceleration 1	k_{AoV}^Q	2.0	$\text{g}/\text{cm}/\text{s}$
tricuspid orifice acceleration 2	k_{TrV}^V	3.5	$\text{g}/\text{cm}/\text{s}$
pulmonary orifice acceleration 2	k_{PuV}^V	3.5	$\text{g}/\text{cm}/\text{s}$
mitral orifice acceleration 2	k_{MiV}^V	3.5	$\text{g}/\text{cm}/\text{s}$
aortic orifice acceleration 2	k_{AoV}^V	7.0	$\text{g}/\text{cm}/\text{s}$
tricuspid maximum opening angle	$\varphi_{TrV}^{\max}$	75°	—
pulmonary maximum opening angle	$\varphi_{PuV}^{\max}$	75°	—
mitral maximum opening angle	$\varphi_{MiV}^{\max}$	75°	—
aortic maximum opening angle	$\varphi_{AoV}^{\max}$	75°	—
tricuspid minimum opening angle	$\varphi_{TrV}^{\min}$	(m) 5° (s) 10°	—
pulmonary minimum opening angle	$\varphi_{PuV}^{\min}$	(m) 5° (s) 10°	—
mitral minimum opening angle	$\varphi_{MiV}^{\min}$	(m) 5° (s) 10°	—
aortic minimum opening angle	$\varphi_{AoV}^{\min}$	(m) 5° (s) 10°	—

(m): mild AI condition.

(s): severe AI condition.

Table 8: Description of model parameters that characterize the opening angle model.

Systemic arterial parameters			
description	symbol	value	units
left common carotid systemic inertance	L_{lccs}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
right common carotid systemic inertance	L_{rccs}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
left subclavian systemic inertance	L_{lss}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
right subclavian systemic inertance	L_{rss}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
descending aorta systemic inertance	L_{das}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
left common carotid systemic resistance	R_{lccs}	2143	$\text{dyn}\cdot\text{s}/\text{cm}^5$
right common carotid systemic resistance	R_{rccs}	2143	$\text{dyn}\cdot\text{s}/\text{cm}^5$
left subclavian systemic resistance	R_{lss}	3000	$\text{dyn}\cdot\text{s}/\text{cm}^5$
right subclavian systemic resistance	R_{rss}	3000	$\text{dyn}\cdot\text{s}/\text{cm}^5$
descending aorta systemic resistance	R_{das}	197	$\text{dyn}\cdot\text{s}/\text{cm}^5$
left common carotid systemic compliance	C_{lccs}	$7.88 \cdot 10^{-5}$	cm^5/dyn
right common carotid systemic compliance	C_{rccs}	$7.88 \cdot 10^{-5}$	cm^5/dyn
left subclavian systemic compliance	C_{lss}	$5.63 \cdot 10^{-5}$	cm^5/dyn
right subclavian systemic compliance	C_{rss}	$5.63 \cdot 10^{-5}$	cm^5/dyn
descending aorta systemic compliance	C_{das}	$8.55 \cdot 10^{-4}$	cm^5/dyn
left common carotid peripheral inertance	L_{lccp}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
right common carotid peripheral inertance	L_{rccp}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
left subclavian peripheral inertance	L_{lsp}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
right subclavian peripheral inertance	L_{rsp}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
descending aorta peripheral inertance	L_{dap}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
left common carotid peripheral resistance	R_{lccp}	19286	$\text{dyn}\cdot\text{s}/\text{cm}^5$
right common carotid peripheral resistance	R_{rccp}	19286	$\text{dyn}\cdot\text{s}/\text{cm}^5$
left subclavian peripheral resistance	R_{lsp}	27000	$\text{dyn}\cdot\text{s}/\text{cm}^5$
right subclavian peripheral resistance	R_{rsp}	27000	$\text{dyn}\cdot\text{s}/\text{cm}^5$
descending aorta peripheral resistance	R_{dap}	1776	$\text{dyn}\cdot\text{s}/\text{cm}^5$
left common carotid peripheral compliance	C_{lccp}	$8.75 \cdot 10^{-6}$	cm^5/dyn
right common carotid peripheral compliance	C_{rccp}	$8.75 \cdot 10^{-6}$	cm^5/dyn
left subclavian peripheral compliance	C_{lsp}	$6.25 \cdot 10^{-6}$	cm^5/dyn
right subclavian peripheral compliance	C_{rsp}	$6.25 \cdot 10^{-6}$	cm^5/dyn
descending aorta peripheral compliance	C_{dap}	$9.50 \cdot 10^{-5}$	cm^5/dyn

Table 9: Description of model parameters that characterize the blood flow in the systemic arterial territories.

Systemic venous parameters			
description	symbol	value	units
upper body venules inertance	L_{ubve}	1.333	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
upper body veins inertance	L_{ubv}	0.667	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
superior vena cava inertance	L_{svc}	0.667	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
upper body venules resistance	R_{ubve}	187	$\text{dyn}\cdot\text{s}/\text{cm}^5$
upper body veins resistance	R_{ubv}	40.0	$\text{dyn}\cdot\text{s}/\text{cm}^5$
superior vena cava resistance	R_{svc}	0.667	$\text{dyn}\cdot\text{s}/\text{cm}^5$
upper body venules compliance	C_{ubve}	$3.75 \cdot 10^{-4}$	cm^5/dyn
upper body veins compliance	C_{ubv}	$1.13 \cdot 10^{-2}$	cm^5/dyn
superior vena cava compliance	C_{svc}	$3.75 \cdot 10^{-3}$	cm^5/dyn
lower body venules inertance	L_{lbve}	1.333	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
lower body veins inertance	L_{lbv}	0.667	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
inferior vena cava inertance	L_{ivc}	0.667	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
lower body venules resistance	R_{lbve}	53.3	$\text{dyn}\cdot\text{s}/\text{cm}^5$
lower body veins resistance	R_{lbv}	12.0	$\text{dyn}\cdot\text{s}/\text{cm}^5$
inferior vena cava resistance	R_{ivc}	0.667	$\text{dyn}\cdot\text{s}/\text{cm}^5$
lower body venules compliance	C_{lbve}	$1.13 \cdot 10^{-3}$	cm^5/dyn
lower body veins compliance	C_{lbv}	$5.63 \cdot 10^{-2}$	cm^5/dyn
inferior vena cava compliance	C_{ivc}	$1.13 \cdot 10^{-2}$	cm^5/dyn

Table 10: Description of model parameters that characterize the blood flow in the upper and lower venous regions.

Pulmonary parameters			
description	symbol	value	units
pulmonary arteries inertance	L_{pa}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
pulmonary veins inertance	L_{pv}	0.0	$\text{dyn}\cdot\text{s}^2/\text{cm}^5$
pulmonary arteries resistance	R_{pa}	(c)160 (u)267	$\text{dyn}\cdot\text{s}/\text{cm}^5$
pulmonary veins resistance	R_{pv}	(c)20 (u)33	$\text{dyn}\cdot\text{s}/\text{cm}^5$
pulmonary arteries compliance	C_{pa}	(c) $2.32 \cdot 10^{-3}$ (u) $3.09 \cdot 10^{-4}$	cm^5/dyn
pulmonary veins compliance	C_{pv}	(c) $2.25 \cdot 10^{-2}$ (u) $3.00 \cdot 10^{-3}$	cm^5/dyn

(c): coupled RV condition.

(u): uncoupled RV condition.

Table 11: Description of model parameters that characterize the blood flow in the pulmonary arteries and veins.

LVAD parameters			
description	symbol	value	units
LVAD speed	S_{LVAD}	$\{5500, 6400\}^\dagger$	rpm

† : depending on the simulation protocol

Table 12: Description of additional model parameters that characterize closed-loop model coupled to the LVAD.

3D model parameters		
description	symbol	value
viscosity	μ	$0.035 \text{ P}^\S$
density	ρ	$1.06 \text{ g}/\text{cm}^3$
LVAD flow rate	Q_{LVAD}	unknown global model ‡
aortic valve flow rate	Q_{AoV}	unknown global model ‡
left common carotid total resistance	R_{lcc}^{tot}	$R_{lccs} + R_{lccp}^\ddagger$
right common carotid total resistance	R_{rcc}^{tot}	$R_{rccs} + R_{rccp}^\ddagger$
left subclavian total resistance	R_{ls}^{tot}	$R_{lss} + R_{lsp}^\ddagger$
right subclavian total resistance	R_{rs}^{tot}	$R_{rss} + R_{rsp}^\ddagger$
descending aorta total resistance	R_{da}^{tot}	$R_{das} + R_{dap}^\ddagger$

§ : $1 \text{ P} = 1 \text{ dyn}\cdot\text{s}/\text{cm}^2$.

‡ : time-dependent function obtained only after solving the global circulation model under a specific simulation protocol (see Section 2).

‡ : value depends on a specific simulation protocol (see Section 4).

Table 13: Description of model parameters that characterize the local circulation model.

$\frac{E_{es}}{E_a} > 0.7$. These two physiological conditions are differentiated in the tables by the preceding symbols (c) and (u), for coupled and uncoupled conditions, respectively.

Concerning aortic insufficiency (AI), we propose two different scenarios, these are: severe AI, which was defined as a regurgitant fraction (RF) of $> 50\%$, and mild/moderate AI as a RF of $< 50\%$. These two conditions are described in the tables by the preceding symbols (s) and (m), for severe and mild AI, respectively.

For both, coupled and uncoupled RV conditions, we consider the following physiological scenarios:

- baseline (BL)
- blood pressure (BP) control
- speed augmentation (SA)
- pulmonary vasodilation (PV) for the uncoupled RV condition
- pulmonary vasodilation (PV-BP) and BP control for the uncoupled RV condition

The parameters that are modified in each scenario are described in Table 14.

coupled RV – multiplicative factors (not for LVAD speed)					
parameters	scenario				
	BL	BP	SA		
S_{LVAD}	5500 rpm	5500 rpm	6400 rpm		
$\{R_{lccs}, R_{rccs}, R_{lss}, R_{rss}, R_{das}\}$	(s)2.0 (m)0.9	(s)0.8 (m)0.5	(s)1.5 (m)0.6		
$\{R_{lccp}, R_{rccp}, R_{lsp}, R_{rsp}, R_{dap}\}$	(s)2.0 (m)0.9	(s)0.8 (m)0.5	(s)1.5 (m)0.6		
$\{C_{lccs}, C_{rccs}, C_{lss}, C_{rss}, C_{das}\}$	1.5	1.5	1.5		
$\{C_{lccp}, C_{rccp}, C_{lsp}, C_{rsp}, C_{dap}\}$	1.5	1.5	1.5		
$\{R_{pa}, R_{pv}\}$	(s)2.0 (m)0.9	(s)0.8 (m)0.5	(s)1.5 (m)0.6		
$\{C_{pa}, C_{pv}\}$	1.5	1.5	1.5		

uncoupled RV – multiplicative factors (not for LVAD speed)					
parameters	scenario				
	BL	BP	SA	PV	PV-BP
S_{LVAD}	5500 rpm	5500 rpm	6400 rpm	5500 rpm	5500 rpm
$\{R_{lccs}, R_{rccs}, R_{lss}, R_{rss}, R_{das}\}$	(s)2.0 (m)0.9	(s)1.5 (m)0.6	(s)1.5 (m)0.6	(s)2.0 (m)0.9	(s)0.8 (m)0.5
$\{R_{lccp}, R_{rccp}, R_{lsp}, R_{rsp}, R_{dap}\}$	(s)2.0 (m)0.9	(s)1.5 (m)0.6	(s)1.5 (m)0.6	(s)2.0 (m)0.9	(s)0.8 (m)0.5
$\{C_{lccs}, C_{rccs}, C_{lss}, C_{rss}, C_{das}\}$	0.8	1.3	0.8	1.5	1.5
$\{C_{lccp}, C_{rccp}, C_{lsp}, C_{rsp}, C_{dap}\}$	0.8	1.3	0.8	1.5	1.5
$\{R_{pa}, R_{pv}\}$	(s)2.0 (m)0.9	(s)1.5 (m)0.6	(s)1.5 (m)0.6	(s)1.2 (m)0.54	(s)0.48 (m)0.3
$\{C_{pa}, C_{pv}\}$	0.8	1.3	0.8	11.25	11.25

(m): mild AI condition.

(s): severe AI condition.

Table 14: Description of multiplicative factors (except for the LVAD speed) that change the parameter values to simulate the physiological scenarios of interest.

5. Results

Figure 5 shows the pressure-volume loops for both RV and LV in the case of a coupled RV. In that figure, the left column corresponds to the severe AI condition, and the right column to the moderate AI condition. The first row is the BL (baseline) scenario, the second row is the SA (speed augmentation) scenario and the third row is for the BP (blood pressure control) scenario. Analogously, Figure 6 shows the RV and LV pressure-volume loops in the case of an uncoupled RV. While the left column corresponds to the severe AI condition, the right column is for the moderate AI condition. The first, second and third rows are for the BL, SA and BP scenarios, respectively. Finally, fourth and fifth rows correspond to the PV (pulmonary vasodilation) and PV-BP (pulmonary vasodilation + blood pressure control) scenarios, respectively.

Table 15 reports the indexes related to the cardiac function for both RV and LV in the case of a coupled RV. For the case of an uncoupled RV, these data are reported in Table 15.

Figure 5: Pressure-volume loops in the case of a coupled RV for strong and moderate AI, and for the different physiological scenarios (BL, SA, BP).

Figure 7 displays the evolution of some hemodynamic quantities along the cardiac cycle for the case of a coupled RV, and for strong and strong (top) and moderate (bottom) AI, respectively. In these figures, we report the RV and LV pressure and volume signatures, the systemic arterial and pulmonary arterial pressures, the left atrium and pulmonary veins pressure contours, the flow rate through the aortic root and through the LVAD, and the pressure-volume loops. Each figure features the hemodynamic signals for the three scenarios of interest, namely baseline (BL), speed augmentation (SA) and blood pressure (BP) control. Similar plots are reported in Figure 8 for the case of an uncoupled RV and strong (top) and moderate (bottom) AI, and for the five scenarios of interest, baseline (BL), speed augmentation (SA), blood pressure (BP) control, pulmonary vasodilation (PV) and pulmonary vasodilation plus blood pressure control (PV-BP).

Figure 6: Pressure-volume loops in the case of an uncoupled RV for strong and moderate AI, and for the different physiological scenarios (BL, SA, BP, PV, PV-BP).

Coupled RV							
Cardiac index	Units	severe AI			moderate AI		
		BL	SA	BP	BL	SA	BP
E_{esRV}	mmHg/ml	0.364	0.360	0.356	0.364	0.351	0.354
E_{aRV}	mmHg/ml	0.477	0.408	0.333	0.379	0.273	0.271
$F_{RV}^{es/a}$	-	0.762	0.884	1.069	0.959	1.285	1.310
SW_{RV}	mmHg.ml	851	860	827	862	805	816
MVO_{2RV}	mlO ₂	0.0447	0.0440	0.0413	0.0435	0.0401	0.0398
PE_{RV}	mmHg.ml	726	684	589	659	555	532
PVA_{RV}	mmHg.ml	1577	1544	1416	1520	1360	1348
Eff_{RV}	-	0.127	0.130	0.133	0.132	0.134	0.136
$\bar{P}_{sa}$	mmHg	92	99	73	92	88	72
P_{sa}^{max}	mmHg	97	101	78	94	89	75
P_{sa}^{min}	mmHg	88	96	69	90	87	70
$\bar{P}_{pa}$	mmHg	24	22	20	22	19	18
P_{pa}^{max}	mmHg	28	28	26	27	25	25
P_{pa}^{min}	mmHg	19	18	16	17	14	14
ΔP_{AoV}	mmHg	56.6	66.6	42.6	58.1	62.7	43.7
Q_{AoV}	l/min	-3.33	-4.07	-2.47	-0.87	-0.99	-0.42
Q_{LVAD}	l/min	5.42	7.05	6.26	5.35	7.20	6.22
V_{AoV}^{back}	ml	-59	-68	-50	-15	-16	-12
$Q_{AoV} + Q_{LVAD}$	l/min	2.10	2.97	3.80	4.47	6.21	5.80
RF	-	61.3%	57.8%	39.4%	16.3%	13.7%	6.7%

Table 15: Indexes that characterize the cardiac function in the case of a coupled RV.

Uncoupled RV											
Cardiac index	Units	severe AI					moderate AI				
		BL	SA	BP	PV	PV-BP	BL	SA	BP	PV	PV-BP
E_{esRV}	mmHg/ml	0.340	0.331	0.339	0.364	0.356	0.327	0.315	0.326	0.364	0.354
E_{aRV}	mmHg/ml	1.192	0.979	0.918	0.477	0.333	0.857	0.585	0.597	0.379	0.271
$F_{RV}^{es/a}$	-	0.285	0.338	0.370	0.762	1.069	0.381	0.540	0.547	0.959	1.310
SW_{RV}	mmHg.ml	754	842	822	851	827	891	994	977	862	816
MVO_{2RV}	mlO ₂	0.0602	0.0595	0.0578	0.0447	0.0413	0.0584	0.0530	0.0538	0.0435	0.0398
PE_{RV}	mmHg.ml	1564	1445	1384	726	589	1345	988	1038	659	532
PVA_{RV}	mmHg.ml	2318	2287	2206	1577	1416	2235	1982	2015	1520	1348
Eff_{RV}	-	0.083	0.094	0.095	0.127	0.133	0.101	0.125	0.121	0.132	0.136
$\bar{P}_{sa}$	mmHg	83	89	79	92	73	84	82	72	92	72
P_{sa}^{max}	mmHg	88	92	82	97	78	86	82	73	94	75
P_{sa}^{min}	mmHg	79	87	76	88	69	82	82	71	90	70
$\bar{P}_{pa}$	mmHg	21	21	21	24	20	20	19	19	22	18
P_{pa}^{max}	mmHg	41	39	39	28	26	38	34	34	27	25
P_{pa}^{min}	mmHg	13	13	13	19	16	13	12	13	17	14
ΔP_{AoV}	mmHg	56.8	71.7	52.6	56.6	42.6	68.8	74.5	54.6	58.1	43.7
Q_{AoV}	l/min	-3.78	-4.34	-3.62	-3.33	-2.47	-1.05	-1.10	-0.93	-0.87	-0.42
Q_{LVAD}	l/min	5.56	6.92	5.80	5.42	6.26	5.05	6.86	5.80	5.35	6.22
V_{AoV}^{back}	ml	-63	-72	-60	-59	-50	-17	-18	-15	-15	-12
$Q_{AoV} + Q_{LVAD}$	l/min	1.78	2.59	2.19	2.10	3.80	4.00	5.77	4.87	4.47	5.80
RF	-	67.9%	62.6%	62.4%	61.3%	39.4%	20.8%	16.0%	16.0%	16.3%	6.7%

Table 16: Indexes that characterize the cardiac function in the case of an uncoupled RV.

Figure 7: Pressure, volume and flow rate waveforms in the heart, systemic arteries and pulmonary vasculature for the case of a coupled RV. Top: condition with strong AI. Bottom: condition with moderate AI.

Figure 8: Pressure, volume and flow rate waveforms in the heart, systemic arteries and pulmonary vasculature for the case of an uncoupled RV. Top: condition with strong AI. Bottom: condition with moderate AI.

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