Fast, accurate antibody structure prediction from deep learning on massive set of natural antibodies

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Antibodies have the capacity to bind a diverse set of antigens, and they have become critical therapeutics and diagnostic molecules. The binding of antibodies is facilitated by a set of six hypervariable loops that are diversified through genetic recombination and mutation. Even with recent advances, accurate structural prediction of these loops remains a challenge. Here, we present IgFold, a fast deep learning method for antibody structure prediction. IgFold consists of a pre-trained language model trained on 558M natural antibody sequences followed by graph networks that directly predict backbone atom coordinates. IgFold predicts structures of similar or better quality than alternative methods (including AlphaFold) in significantly less time (under one minute). Accurate structure prediction on this timescale makes possible avenues of investigation that were previously infeasible. As a demonstration of IgFold's capabilities, we predicted structures for 105K paired antibody sequences, expanding the observed antibody structural space by over 40 fold.

antibodies | deep learning | language modeling | structure prediction

Introduction

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Antibodies play a critical role in the immune response against foreign pathogens. Through genetic recombination and
 hyper-mutation, the adaptive immune system is capable of generating a vast number of potential antibodies. Immune

⁴ repertoire sequencing provides a glimpse into an individual's antibody population (1). Analysis of these repertoires

 $_{5}$ can further our understanding of the adaptive immune response (2) and even suggest potential therapeutics (3).

However, sequence data alone provides only a partial view into the immune repertoire. The interactions that facilitate 6 antigen binding are determined by the structure of a set of six loops that make up a complementarity determining 7 region (CDR). Accurate modeling of these CDR loops provides insights into these binding mechanisms and promises 8 to enable rational design of specific antibodies (4). Five of the CDR loops tend to adopt canonical folds that can 9 be predicted effectively by sequence similarity (5). However, the third CDR loop of the heavy chain (CDR H3) has 10 proven a challenge to model due to its increased diversity, both in sequence and length (6, 7). Further, the position of 11 the H3 loop at the interface between the heavy and light chains makes its conformation dependent on the inter-chain 12 orientation (8, 9). Given its central role in binding, advances in prediction of H3 loop structures are critical for 13

¹⁴ understanding antibody-antigen interactions and enabling rational design of antibodies.

Deep learning methods have brought about a revolution in protein structure prediction (10, 11). With the 15 development of AlphaFold, accurate protein structure prediction has largely become accessible to all (12). Beyond 16 monomeric proteins, AlphaFold-Multimer has demonstrated an impressive ability to model protein complexes (13). 17 However, performance on antibody structures remains to be extensively validated. Meanwhile, antibody-specific deep 18 learning methods such as DeepAb (14) and ABlooper (15) have significantly improved CDR loop modeling accuracy, 19 including for the challenging CDR H3 loop (7, 16). DeepAb predicts a set of inter-residue geometric constraints that 20 are fed to Rosetta to produce a complete F_V structure (14). ABlooper predicts CDR loop structures in an end-to-end 21 fashion, with minimal post-prediction refinement required, while also providing an estimate of loop quality (15). 22 While effective, certain design decisions limit the utility of both models. DeepAb predictions are relatively slow (ten 23

²⁴ minutes per sequence), cannot effectively incorporate template data, and offer little insight into expected quality.

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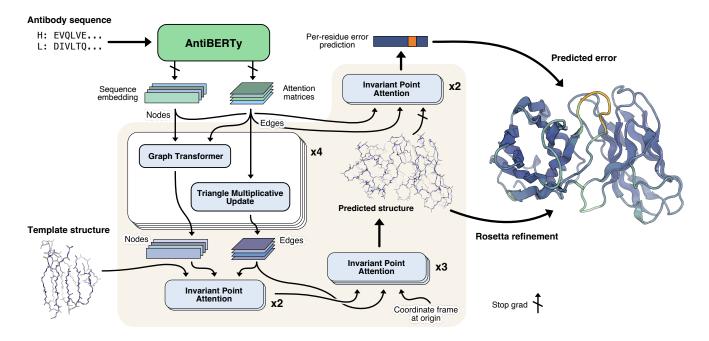


Fig. 1. Diagram of method for end-to-end prediction of antibody structures. Antibody sequences are converted into contextual embeddings using AntiBERTy, a pre-trained language model. From these representations, IgFold uses a series of transformer layers to directly predict atomic coordinates for the protein backbone atoms. For each residue, IgFold also provides an estimation of prediction quality. Refinement of predictions and addition of side chains is performed by Rosetta.

ABlooper predictions, while faster and more informative, rely on less accurate homology models for the framework structure and cannot incorporate CDR loop templates or predict nanobody structures.

Concurrent with advances in structure prediction, self-supervised learning on massive sets of unlabeled protein 27 sequences has shown remarkable utility across protein modeling tasks (17, 18). Embeddings from transformer encoder 28 models trained for masked language modeling have been used for variant prediction (19), evolutionary analysis (20, 21), 29 and as features for protein structure prediction (22, 23). Auto-regressive transformer models have been used to 30 generate functional proteins entirely from sequence learning (24). The wealth of immune repertoire data provided by 31 sequencing experiments has enabled development of antibody-specific language models. Models trained for masked 32 language modeling have been shown to learn meaningful representations of immune repertoire sequences (21, 25, 26), 33 and even repurposed to humanize antibodies (27). Generative models trained on sequence infilling have been shown 34 to generate high-quality antibody libraries (28, 29). 35

In this work, we present IgFold: a fast, accurate model for end-to-end prediction of antibody structures from sequence. IgFold leverages embeddings from AntiBERTy (21), a language model pre-trained on 558M natural antibody sequences, to directly predict the atomic coordinates that define the antibody structure. Predictions from IgFold match the accuracy of the recent AlphaFold models (10, 13) while being much faster (under one minute). IgFold also provides flexibility beyond the capabilities of alternative antibody-specific models, including robust incorporation of template structures and support for nanobody modeling.

42 Results

End-to-end prediction of antibody structure. Our method for antibody structure prediction, IgFold, utilizes learned
 representations from the pre-trained AntiBERTy language model to directly predict 3D atomic coordinates (Figure 1).

45 Structures from IgFold are accompanied by a per-residue accuracy estimate, which provides insights into the quality 46 of the prediction.

Embeddings from pre-trained model encode structural features. The limited number of experimentally determined antibody structures (thousands (30)) presents a difficultly in training an effective antibody structure predictor. In the absence of structural data, self-supervised language models provide a powerful framework for extracting patterns from the significantly greater number (billions (31)) of natural antibody sequences identified by immune repertoire sequencing studies. For this work, we used AntiBERTy (21), a transformer language model pre-trained on 558M natural antibody sequences, to generate embeddings for structure prediction. Similar to the role played by alignments

of evolutionarily related sequences for general protein structure prediction (32), embeddings from AntiBERTy act as a contextual representation that places individual sequences within the broader antibody space.

Prior work has demonstrated that protein language models can learn structural features from sequence pre-training 55 alone (17, 33). To investigate whether sequence embeddings from AntiBERTy contained nascent structural features, 56 we generated embeddings for the set of 3,467 paired antibody sequences with experimentally determined structures in 57 the PDB. For each sequence, we extracted the portions of the embedding corresponding to the six CDR loops and 58 averaged to obtain fixed-sized CDR loop representations (one per loop). We then collected the embeddings for each 59 CDR loop across all sequences and visualized using two-dimensional t-SNE (Figure S1). To determine whether the 60 CDR loop representations encoded structural features, we labeled each point according to its canonical structural 61 cluster. For CDR H3, which lacks canonical clusters, we instead labeled by loop length. For the five CDR loops that 62 adopt canonical folds we observed clear organization within the embedded space. For the CDR H3 loop, we found 63 that the embedding space did not separate into natural clusters, but was rather organized roughly in accordance with 64 loop length. These results suggest that AntiBERTy has learned to encode CDR loop structural features through 65 sequence pre-training alone. 66

Coordinate prediction from sequence embeddings. To predict 3D atomic coordinates from sequence embeddings, we 67 adopt a graphical representation of antibody structure, with each residue as a node and information passing between 68 all pairs of residues (Figure 1). The nodes are initialized using the final hidden layer embeddings from AntiBERTY. 69 To initialize the edges, we collect the full set of inter-residue attention matrices from each layer of AntiBERTy. These 70 attention matrices are a useful source of edge information as they encode the residue-residue information pathways 71 learned by the pre-trained model. For paired antibodies, we concatenate the sequence embeddings from each chain 72 and initialize inter-chain edges to zero. We do not explicitly provide a chain break delimiter, as the pre-trained 73 language model already includes a positional embedding for each sequence. The structure prediction model begins 74 with a series of four graph transformer (34) layers interleaved with edge updates via the triangle multiplicative layer 75 proposed for AlphaFold (10). 76

Following the initial graph transformer layers, we incorporate structural template information into the nascent 77 representation using invariant point attention (IPA) (10). In contrast to the application of IPA for the AlphaFold 78 structure module, we fix the template coordinates and use IPA as a form of structure-aware self-attention. This 79 enables the model to incorporate the local structural environment into the sequence representation directly from the 80 3D coordinates, rather than switching to an inter-residue representation (e.g., distance or contact matrices). We use 81 three IPA layers to incorporate template information. Rather than search for structural templates for training, we 82 generate template-like structures by corruption of the true label structures. Specifically, for 50% of training examples, 83 we randomly select one to six consecutive segments of twenty residues and move the atomic coordinates to the origin. 84 The remaining residues are provided to the model as a template. The deleted segments of residues are hidden from the 85 IPA attention, so that the model only incorporates structural information from residues with meaningful coordinates. 86 Finally, we use another set of IPA layers to predict the final 3D antibody structure. Here, we employ a strategy 87 similar to the AlphaFold structure module (10) and train a series of three IPA layers to translate and rotate each 88 residue from an initialized position at the origin to the final predicted position. We depart slightly from the AlphaFold 89 implementation and learn separate weights for each IPA layer, as well as allow gradient propagation through the 90 rotations. To train the model for structure prediction, we minimize the mean-squared error between the predicted 91 coordinates and the experimental structure after Kabsch alignment. In practice, we observe that the first IPA layer is 92 sufficient to learn the global arrangement of residues (albeit in a compact form), while the second and third layers 93 function to produce the properly scaled structure with correct bond lengths and angles (Figure S2). 94

Per-residue error prediction. Simulatneously with structure prediction training, we additionally train the model to 95 estimate the error in its own predictions. For error estimation, we use two IPA layers that operate similarly to the 96 template incorporation layers (i.e., without coordinate updates). The error estimation layers take as input the final 97 predicted structure, as well as a separate set of node and edge features derived from the initial AntiBERTy features. 98 We stop gradient propagation through the error estimation layers into the predicted structure to prevent the model 99 from optimizing for accurately estimated, but highly erroneous structures. For each residue, the error estimation 100 layers are trained to predict the deviation of the C_{α} atom from the experimental structure after a Kabsch alignment 101 of the beta barrel residues. We use a different alignment for error estimation than structure prediction to more closely 102 mirror the conventional antibody modeling evaluation metrics. The model is trained to minimize the L1 norm of the 103 predicted C_{α} deviation minus the true deviation. 104

¹⁰⁵ Structure dataset augmentation with AlphaFold. We sought to train the model on as many immunoglobulin structures ¹⁰⁶ as possible. From the Structural Antibody Databae (SAbDab) (30), we obtained 4,275 structures consisting of

paired antibodies and single-chain nanobodies. Given the remarkable success of AlphaFold for modeling both protein 107 monomers and complexes, we additionally explored the use of data augmentation to produce structures for training. 108 To produce a diverse set of structures for data augmentation, we clustered (35) the paired and unpaired partitions 109 of the Observed Antibody Space (31) at 40% and 70% sequence identity, respectively. This clustering resulted in 110 16,141 paired sequences and 26,971 unpaired sequences. We predicted structures for both sets of sequences using the 111 original AlphaFold model. For the paired sequences, we modified the model inputs to enable complex modeling by 112 inserting a gap in the positional embeddings (i.e., AlphaFold-Gap (12, 13)). For the unpaired sequences, we discarded 113 the predicted structures with average pLDDT (AlphaFold error estimate) less than 85, leaving 22,132 structures. 114 These low-confidence structures typically corresponded to sequences with missing residues at the N-terminus. During 115 training, we sample randomly from the three datasets with examples weighted inversely to the size of their respective 116 datasets, such that roughly one third of total training examples come from each dataset. 117

Antibody structure prediction benchmark. To evaluate the performance of IgFold against recent methods for antibody structure prediction, we assembled a non-redundant set of antibody structures deposited after compiling our training dataset. We chose to compare performance on a temporally separated benchmark to ensure that none of the methods evaluated had access to any of the structures during training. In total, our benchmark contains 67 paired antibodies and 21 nanobodies.

Predicted structures are high quality before refinement. As an end-to-end model, IgFold directly predicts structural 123 coordinates as its output. However, these immediate structure predictions are not guaranteed to satisfy realistic 124 molecular geometries. In addition to incorporating missing atomic details (e.g., side chains), refinement with 125 Rosetta (36) corrects any such abnormalities. To better understand the impact of this refinement step, we compared 126 the directly predicted structures for each target in the benhmark to their refined counterparts. In general, we 127 observed very little change in the structures (Figure S3), with an average RMSD less than 0.5 Å before and after 128 refinement. The exception to this trend is abnormally long CDR loops, particularly CDR H3. We compared the 129 pre- and post-refinement structures for benchmark targets with three of the longest CDR H3 loops to those with 130 shorter loops and found that the longer loops frequently contained unrealistic bond lengths and backbone torsion 131 angles (Figure S4). Similar issues have been observed in recent previous work (15), indicating that directly predicting 132 atomically correct long CDR loops remains a challenge. 133

Accurate antibody structures in fraction of time. We compared the performance of IgFold against a mixture of grafting 134 and deep learning methods for antibody structure prediction. Although previous work has demonstrated significant 135 improvements by deep learning over grafting-based methods, we continue to benchmark against grafting to track its 136 performance as increasingly many antibody structures become available. For each benchmark target, we predicted 137 structures using ABodyBuilder (37), DeepAb (14), ABlooper (15), and AlphaFold-Multimer (13). Of these methods, 138 ABodyBuilder utilizes a grafting-based algorithm for structure prediction and the remaining use some form of deep 139 learning. DeepAb and ABlooper are both trained specifically for paired antibody structure prediction, and have 140 previously reported comparable performance. AlphaFold-Multimer has demonstrated state-of-the-art performance for 141 protein complex prediction – however, performance on antibody structures specifically remains to be evaluated. 142

The performance of each method was assessed by measuring the backbone heavy-atom RMSD between the predicted 143 and experimentally determined structures for the framework residues and each CDR loop. All RMSD values are 144 measured after alignment of the framework residues. In general, we observed state-of-the-art performance for all of 145 the deep learning methods while grafting performance continued to lag behind (Figure 2A, Table 1). On average, all 146 methods predicted both the heavy and light chain framework structures with high accuracy (0.43-0.54 Å and 0.38 -147 0.45 Å, respectively). Similarly, for the CDR1 and CDR2 loops, all deep learning methods produced sub-angstrom 148 predictions on average, with the grafting-based ABodyBuilder performing marginally worse. The largest improvement 149 in prediction accuracy by deep learning methods is observed for the CDR3 loops. 150

We also considered the predicted orientation between the heavy and light chains, which is an important determinant 151 of the overall binding surface (8, 9). Accuracy of the inter-chain orientation was evaluated by measuring the deviation 152 from native of the inter-chain packing angle, inter-domain distance, heavy-opening angle, and light-opening angle. 153 Each of these orientional coordinates are rescaled by dividing by their respective standard deviations (calculated 154 over the set of experimentally determined antibody structures) and summed to obtain an orientational coordinate 155 distance (OCD) (9). We found that in general deep learning methods produced F_V structures with OCD values below 156 four, indicating that the predicted structures are typically within one standard deviation of the native structures for 157 each of the components of OCD. The exception to this trend is ABlooper, which utilizes framework structures from 158 ABodyBuilder and thus achieves a similar OCD value to the grafting-based method. 159

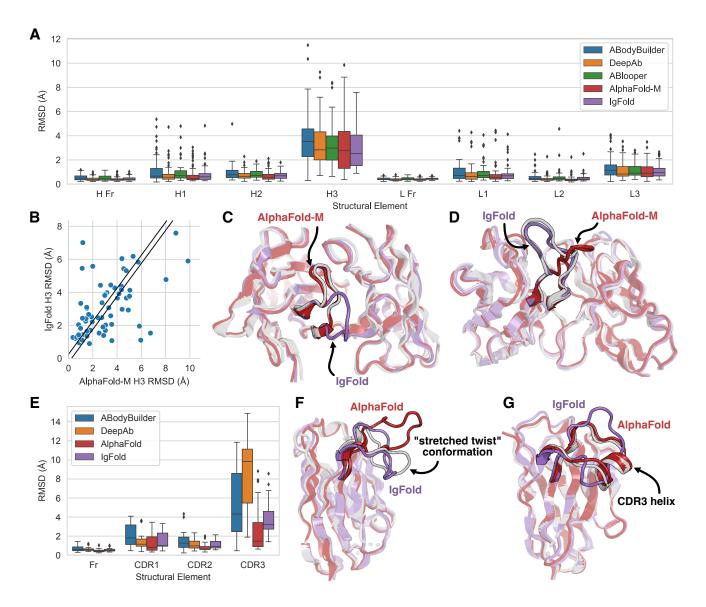


Fig. 2. Comparison of methods for antibody structure prediction. All root-mean-squared-deviation (RMSD) values calculated over backbone heavy atoms after alignment of the respective framework residues. (A) Benchmark performance of ABodyBuilder, DeepAb, ABlooper, AlphaFold-Multimer, and IgFold for paired antibody structure prediction. (B) Per-target comparison of CDR H3 loop structure prediction for IgFold and AlphaFold-Multimer, with each point representing the RMSD_{H3} for both methods on a single benchmark target. (C) Comparison of predicted CDR H3 loop predictions for target 7N3G (L_{H3} = 10 residues) for IgFold (RMSD_{H3} = 7.01 Å) and AlphaFold-Multimer (RMSD_{H3} = 1.18 Å). (D) Comparison of predicted CDR H3 loop predictions for target 7ORA (L_{H3} = 14 residues) for IgFold (RMSD_{H3} = 1.10 Å) and AlphaFold-Multimer (RMSD_{H3} = 5.95 Å). (E) Benchmark performance of ABodyBuilder, DeepAb, AlphaFold, and IgFold for nanobody structure prediction. (F) Comparison of predicted CDR H3 loop predictions for target 7QRA (L_{L0B3} = 7.74 Å). (G) Comparison of predicted CDR H3 loop predictions for target 7AQZ (L_{CDR3} = 17 residues) for IgFold (RMSD_{CDR3} = 3.93 Å) and AlphaFold (RMSD_{CDR3} = 0.94 Å).

Given the comparable aggregate performance of the deep learning methods, we further investigated the similarity 160 between the structures predicted by each method. For each pair of methods, we measured the RMSD of framework and 161 CDR loop residues, as well as the OCD, between the predicted structures for each benchmark target (Figure S8). We 162 additionally plotted the distribution of structural similarities between IgFold and the alternative methods (Figure S9). 163 We found that the framework structures (and their relative orientations) predicted by IgFold resembled those of 164 DeepAb and AlphaFold-Multimer, but were less similar to those of ABodyBuilder and ABlooper. This is expected, 165 given that ABlooper frameworks are based on ABodyBuilder grafts, while the frameworks from the remaining methods 166 are entirely learned (and tend to be more accurate). Interestingly, we also observed that the CDR1 and CDR2 loops 167 from IgFold, DeepAb, and AlphaFold-Multimer were quite similar on average. It is unclear why CDR loop structures 168 from ABlooper, which was trained on a dataset similar to that of DeepAb and predicts CDR loops in an end-to-end 169 manner like IgFold, tend to be disimilar to those of DeepAb and IgFold. This may be due to framework inaccuracies 170 degrading the quality of CDR loop structures. 171

Although the performance of the deep learning methods for antibody structure prediction is largely comparable, 172 the speed of prediction is not. Grafting-based methods, such as ABodyBuilder, tend to be much faster than deep 173 learning methods (if a suitable template can be found). For the present benchmark, ABodyBuilder was able to 174 predict structures in seconds for 65 of 67 targets, only twice resorting to a time-consuming CDR H3 loop building 175 procedure. However, as reported above, this speed is obtained at the expense of accuracy. DeepAb and ABlooper, 176 which are more accurate and trained specifically for antibodies, require more time to predict full-atom structures (up 177 to one minute for ABlooper and ten minutes for DeepAb). AlphaFold-Multimer, trained for general protein structure 178 prediction from multiple sequence alignments, requires approximately one hour to predict full-atom structures. IgFold 179 prediction speed is comparable to ABlooper, and is able to predict full-atom structures in less than a minute. 180

Method	OCD	H Fr (Å)	H1 (Å)	H2(Å)	H3 (Å)	L Fr (Å)	L1 (Å)	L2(Å)	L3 (Å)
ABodyBuilder	4.90	0.54	1.10	0.94	3.75	0.43	1.07	0.58	1.37
DeepAb	3.60	0.43	0.80	0.74	3.28	0.38	0.86	0.45	1.11
ABlooper	4.53	0.51	0.95	0.82	3.20	0.45	0.99	0.59	1.15
AlphaFold-Multimer	3.69	0.43	0.75	0.69	3.02	0.39	0.82	0.41	1.13
IgFold	3.77	0.45	0.80	0.75	2.99	0.45	0.83	0.51	1.07

Table 1. Accuracy of predicted antibody Fv structures

Deep learning methods converge on CDR H3 accuracy. The average prediction accuracy for the highly variable, confor-181 mationally diverse CDR H3 loop was relatively consistent among the four deep learning methods evaluated (Table 1), 182 though AlphaFold-Multimer and IgFold performed slightly better. Given this convergence in performance, we again 183 considered the similarity between the CDR H3 loop structures predicted by each method. DeepAb and ABlooper 184 produced the most similar CDR H3 loops, with an average RMSD of 2.29 Å between predicted structures (Figure S8). 185 This may be reflective of the similar training datasets used for both methods, which were limited to experimentally 186 determined antibody structures. AlphaFold-Multimer, by contrast, predicted the most distinct CDR H3 loops, with 187 an average RMSD 2.81 - 2.95 Å to the other deep learning methods. Finally, IgFold CDR H3 loops were most similar 188 to those of ABlooper, perhaps reflective of both models training for end-to-end coordinate prediction, but less similar 189 than those of DeepAb. 190

The disimilarity of predictions between IgFold and AlphaFold-Multimer is surprising, given the extensive use 191 of AlphaFold-predicted structures for training IgFold. When we compared the per-target accuracy of IgFold and 192 AlphaFold-Multimer, we found many cases where one method predicted the CDR H3 loop accurately while the other 193 failed (Figure 2B). Indeed, approximately 20% of CDR H3 loops predicted by the two methods were greater than 194 4 Å RMSD apart, meaning the methods often predict distinct conformations. In one such case (target 7N3G (38), 195 Figure 2C), AlphaFold-Multimer effectively predicts the CDR H3 loop structure (RMSD_{H3} = 1.18 Å) while IgFold 196 predicts a distinct, and incorrect, conformation (RMSD_{H3} = 7.01 Å). However, for another example (target 7ORA (39), 197 Figure 2D), IgFold more accurately predicts the CDR H3 loop structure (RMSD_{H3} = 1.10 Å) while AlphaFold-198 Multimer predicts an alternative conformation ($\text{RMSD}_{H3} = 5.95$ Å). In practice, these distinct predictions may be 199 useful for generating conformational ensembles for the CDR H3 loop. 200

Fast nanobody structure prediction remains a challenge. Single domain antibodies, or nanobodies, are an increasingly popular format for therapeutic development (40). Structurally, nanobodies share many similarities with paried antibodies, but with the notable lack of a second immunoglobulin chain. This, along with increased nanobody CDR3

loop length, makes accessible a wide range of CDR3 loop conformations not observed for paired antibodies (41). We
compared the performance of IgFold for nanobody structure prediction to ABodyBuilder (37), DeepAb (14), and
AlphaFold (10) (Figure 2E, Table 2). We omitted ABlooper from the comparison as it predicts only paired antibody
structures.

As with paired antibodies, all methods evaluated produced highly accurate predictions for the framework residues, 208 with the average RMSD ranging from 0.47 Å to 0.68 Å. For CDR1 and CDR2 loops, we observe a substantial 209 improvement by IgFold and the other deep learning methods over ABodyBuilder, with AlphaFold achieving the 210 highest accuracy on average. For the CDR3 loop, ABodyBuilder prediction quality is highly variable (average RMSD 211 of 5.40 Å), reflective of the increased difficultly of identifying suitable template structures for the long, conformationally 212 diverse loops. DeepAb achieves the worst performance for CDR3 loops, with an average RMSD of 8.41 Å, probably 213 because its training dataset was limited to paired antibodies (14), and thus the model has never observed the full 214 range of conformations accessible to nanobody CDR3 loops. AlphaFold displays remarkable performance for CDR3 215 loops, with an average RMSD of 2.90 Å, consistent with its high accuracy on general protein sequences. IgFold CDR3 216 predictions tend to be less accurate than those of AlphaFold (average RMSD of 3.85 Å), but are significantly faster to 217 produce (less than 30 seconds for IgFold, versus 30 minutes for AlphaFold). 218

To better understand the distinctions between IgFold- and AlphaFold-predicted nanobody structures, we highlight 219 two examples from the benchmark. First, we compared the structures predicted by both methods for the benchmark 220 target 7AQZ (to be published, Figure 2F). This nanbody features a 15-residue CDR3 loop that adopts the "stretched-221 twist" conformation (41), in which the CDR3 loop bends to contact the framework residues that would otherwise be 222 obstructed by a light chain in a paired antibody. IgFold correctly predicts this nanobody-specific loop conformation 223 $(RMSD_{CDR3} = 3.20 \text{ Å})$, while AlphaFold predicts an extended CDR3 conformation $(RMSD_{CDR3} = 7.74 \text{ Å})$. Indeed, 224 there are other cases where either IgFold or AlphaFold correctly predicts the CDR3 loop conformation while the 225 other fails (see off-diagonal points in Figure S7G). In the majority of such cases, AlphaFold predicts the correct 226 conformation, yielding the lower average CDR3 RMSD. However, the distinct conformations from both methods 227 may be useful for producing an ensemble of structures for some applications. In the second example, we compared 228 the structures predicted by both methods for the benchmark target 7AQY (to be published, Figure 2G). This 229 nanobody has a long 17-residue CDR3 loop with a short helical region. Although both methods correctly predict 230 the loop conformation, IgFold fails to predict the helical secondary structure, resulting in a less accurate prediction 231 $(RMSD_{CDR3} = 3.93 \text{ Å})$ than that of AlphaFold $(RMSD_{CDR3} = 0.94 \text{ Å})$. Such structured loops highlight a key strength 232 of AlphaFold, which was trained on a large dataset of general proteins and has thus encountered a broad variety of 233 structral arrangements, over IgFold, which has observed relatively few such structures within its training dataset. 234 Although AlphaFold performed better than IgFold for nanobdies, the distinct conformations from both methods may 235 be useful for generating diverse predictions when large movement of CDR3 loops are expected. 236

Method	Fr (Å)	CDR1 (Å)	CDR2(Å)	CDR3 (Å)
ABodyBuilder	0.68	2.10	1.49	5.40
DeepAb	0.62	1.61	1.11	8.41
AlphaFold	0.47	1.26	0.79	2.90
IgFold	0.55	1.58	1.06	3.85

Table 2. Accuracy of predicted nanobody structures

Error predictions identify inaccurate CDR loops. Although antibody structure prediction methods continue to improve, accurate prediction of abnormal CDR loops (particularly long CDR H3 loops) remains inconsistent (6, 14, 15). Determining whether a given structural prediction is reliable is critical for effective incorporation of antibody structure prediction into workflows. During training, we task IgFold with predicting the deviation of each residue's C_{α} atom from the native (under alignment of the beta barrel residues). We then use this predicted deviation as a per-residue error estimate to assess expected accuracy of different structural regions.

To assess the utility of IgFold's error predictions for identifying inaccurate CDR loops, we compared the average predicted error for each CDR loop to the RMSD between the predicted loop and the native structure for the paired F_V and nanobody benchmarks. For five of the six paired F_V CDR loops, we observed significant correlations between the predicted error and the loop RMSDs from native (Figure S10). For CDR L2 loops were no significant correlations were observed; however, given the relatively high accuracy of CDR L2 loop predictions, there was little error to detect. For nanobodies, we observed significant correlations between the predicted error and RMSD for all of the CDR loops (Figure S11).

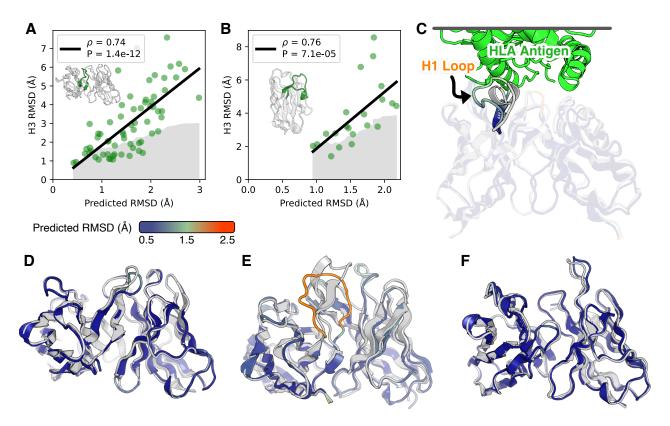


Fig. 3. Error estimation for predicted antibody structures. (A) Comparison of CDR H3 loop RMSD to predicted error for paired antibody structure benchmark. Gray space represents cumulative average RMSD of predicted CDR H3 loops from native structure. (B) Comparison of CDR3 loop RMSD to predicted error for nanobdy structure benchmark. Gray space represents cumulative average RMSD of predicted CDR3 loops from native structure. (C) Predicted structure and error estimation for anti-HLA antibody with a randomized CDR H1 loop. (D) Predicted structure and error estimation for benchmark target 7RAH (L_{H3} = 12 residues). (E) Predicted structure and error estimation for benchmark target 7Q33 (L_{H3} = 3 residues).

For the challenging-to-predict, conformationally diverse CDR3 loops, we observed significant correlations for both 250 paired antibody H3 loops (Figure 3A, $\rho = 0.70$) and nanobody CDR3 loops (Figure 3B, $\rho = 0.63$). To illustrate the 251 utility of error estimation for judging CDR H3 loop predictions, we highlight three examples from the benchmark. 252 The first is the benchmark target 7RAH (42), a mouse anti-adenylate-cyclase antibody with a 12-residue CDR H3 253 loop. For 7RAH, IgFold accurately predicts the extended beta sheet structure of the CDR H3 loop $(RMSD_{H3})$ 254 = 1.43 Å), and estimates a correspondingly lower RMSD (Figure 3D). The second target is 7RKS (43), a human 255 anti-SARS-CoV-2-receptor-binding-domain antibody with a 18-residue CDR H3 loop. IgFold struggles to predict the 256 structured beta sheet within this long H3 loop, instead predicting a broad ununstructured conformation $(RMSD_{H3})$ 257 = 6.18 Å). Appropriately, the error estimation for the CDR H3 loop of 7RKS is much higher (Figure 3E). The third 258 example is 7033 (44), a mouse anti-PAS (proine/alanine-rich sequence) antibody with a 3-residue CDR H3 loop. 259 Again, IgFold accurately predicts the structure of this short loop $(RMSD_{H3} = 1.64 \text{ Å})$ and provides a correspondingly 260 low error estimate (Figure 3F). 261

Antibody engineering campaigns often deviate significantly from the space of natural antibody sequences (45). 262 Predicting structures for such heavily engineered sequences is challenging, particularly for models trained primarily on 263 natural antibody structural data (such as IgFold). To investigate whether IgFold's error estimations can identify likely 264 mistakes in such sequences, we predicted the structure of an anti-HLA (human leukocyte antigen) antibody with a 265 sequence randomized CDR H1 loop (46) (Figure 3C). As expected, there is significant error in the predicted CDR H1 266 loop structure. However, the erroneous structure is accompanied by a high error estimate, revealing that the predicted 267 conformation is likely to be incorrect. This suggests that the RMSD predictions from IgFold are well-calibrated to 268 unnatural antibody sequences and should be informative for a broad range of antibody structure predictions. 269

Template data is successfully incorporated into predictions. For many antibody engineering workflows, partial structural information is available for the antibody of interest. For example, crystal structures may be available for the parent antibody upon which new CDR loops were designed. Incorporating such information into structure predictions is useful for improving the quality of structure models. We simulated IgFold's behavior in this scenario

by predicting structures for the paired antibody and nanobody benchmark targets while providing the coordinates 274 of all non-H3 residues as templates. In general, we found that IgFold was able to incorporate the template data 275 into its predictions, with the average RMSD for all templated CDR loops being significantly reduced (IgFold[Fv-H3]: 276 Figure 4A, IgFold[Fv-CDR3]: Figure 4E). To illustrate the effectiveness of structural data incorporation, we identified 277 a paired antibody benchmark target with challenging-to-predict non-H3 CDR loops that were corrected by inclusion 278 of templates. We consider the benchmark target 7AJ6 (to be published), for which IgFold inaccurately predicted the 279 H2 and L1 loops (1.27 Å and 2.01 Å RMSD, respectively). We found that the model correctly inorporates the the 280 template data for both loops (Figure 4B), reducing the H2 and L1 loop RMSD to 0.73 Å and 0.70 Å, respectively. 281

Having demonstrated successful incorporation of structural data into predictions using templates, we next investi-282 gated the impact on accuracy of the untemplated CDR H3 loop predictions. For the majority of targets, we found 283 little change in the accuracy of CDR H3 loop structures with the addition of non-H3 template information. However, 284 for several paired benchmark targets we observe notable improvements in predicted CDR H3 loop quality (Figure 4C). 285 In one such case, for benchmark target 7RDL, inclusion of non-H3 structural data reduces the RMSD of the CDR 286 H3 loop from 5.45 Å to 2.86 Å (Figure 4D). For nanobodies, we observe fewer cases with substantial improvement 287 to CDR3 loop predictions given template data (Figure 4F). In only one case, benchmark target 7CZ0, do we see a 288 meaningful improvement in RMSD (from 2.03 Å to 1.05 Å). For this target, the improvement in CDR3 accuracy is 289 due to correction of C-terminal residues that anchor the end of the loop to the framework (Figure 4G). 290

We additionally experimented with providing the entire crystal structure to IgFold as template information. In this scenario, IgFold successfully incorporates the structural information of all CDR loops (including H3) into its predictions (IgFold[Fv]: Figure 4A, Figure 4E). Although this approach is of little practical value for structure prediction (as the correct structure is already known) it may be a useful approach for instilling structural information into pre-trained embeddings, which are valuable for other antibody learning tasks.

Large-scale prediction of paired antibody structures. The primary advantage of IgFold over highly accurate methods 296 like AlphaFold is its speed at predicting antibody structures. This speed enables large-scale of antibody structures on 297 modest compute resources. To demonstrate the utility of IgFold's speed, we predicted structures for a non-redundant 298 set of 104,994 paired antibody sequences (clustered at 95% sequence identity) from the OAS database (31). These 299 sequences are made up of 35,731 human, 16,356 mouse, and 52,907 rat antibodies. The structures are predicted with 300 low estimated RMSD by IgFold, indicating that they are accurate (Figure S12). As of this publication, only 2,431 301 unique paired antibody structures have been determined experimentally, and thus our predicted dataset represents an 302 over 40-fold expansion of antibody structural space. These structures are made available for use in future studies. 303

304 Discussion

Protein structure prediction methods have advanced significantly in recent years, and they are now approaching 305 the accuracy of the experimental structures upon which they are trained (10). These advances have been enabled 306 in large part by effective exploitation of the structural information present in alignments of evolutionarily related 307 sequences (MSAs). However, constructing a meaningful MSA is time-consuming, contributing significantly to the 308 runtime of general protein structure prediction models, and making high-throughput prediction of many protein 309 structures computationally prohibitive for many users. In this work, we presented IgFold: a fast, accurate model that 310 specializes in prediction of antibody structures. We demonstrated that IgFold matches the accuracy of the highly 311 accurate AlphaFold-Multimer model (13) for paired antibdy structure prediction, and approaches the accuracy of 312 AlphaFold for nanobodies. Though prediction accuracy is comparable, IgFold is significantly faster than AlphaFold. 313 and is able to predict structures in under one minute. Further, for many targets IgFold and AlphaFold produce 314 predict distinct conformations, which should be useful in assembling structural ensembles for applications where 315 flexibility is important. Predicted structures are accompanied by informative error estimates, which provide critical 316 information on the reliability of structures. 317

Analyses of immune repertoires have traditionally been limited to sequence data alone (1), as high-throughput 318 antibody structure determination was experimentally prohibitive and prediction methods were too slow or inaccurate. 319 However, incorporation of structural context has proven valuable, particularly for identification of sequence-disimilar 320 binders to common epitopes (47). For example, grafting-based methods have been used to identify sequence-diverse 321 but structurally similar antibodies against SARS-CoV-2 (48). The increased accuracy of IgFold, coupled with its 322 speed, will make such methods more effective. Additionally, consideration of structural uncertainty via IgFold's error 323 estimation should reduce the rate of false positives when operating on large volumes of sequences. As a demonstration 324 of IgFold's capabilities, we predicted structures for over 100 thousand paired antibody sequences spanning three 325 species. These structures expand on the number of experimentally determined antibody structures by a factor of 40. 326 The vast majority of these structures are predicted with high confidence, suggesting that they are reliable. Although 327

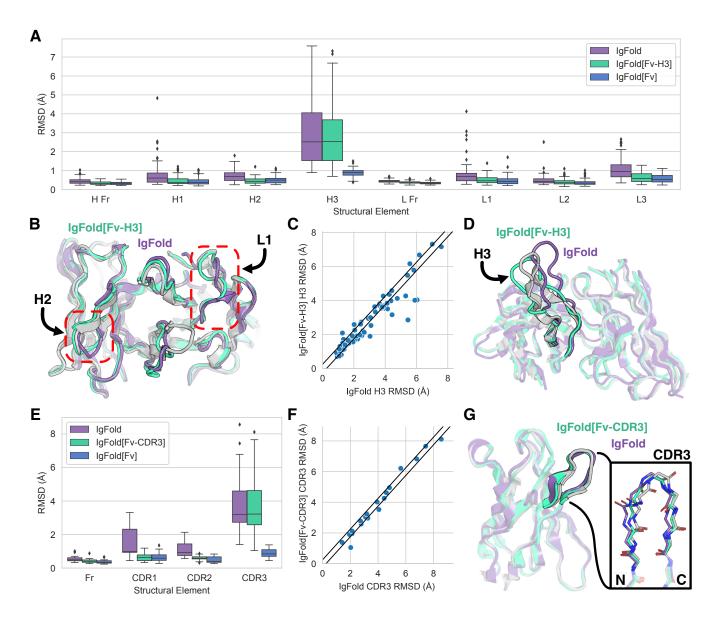


Fig. 4. Incorporation of structure data into IgFold predictions. (A) Paired antibody structure prediction benchmark results for IgFold without templates, IgFold given the F_V structure without the CDR H3 loop (IgFold[Fv-H3]), and IgFold given the complete Fv structre (IgFold[Fv]). (B) Superimposition of IgFold and IgFold[Fv-H3] predictions for benchmark target 7AJ6 onto native (gray). Errors in the predicted CDR H2 and L1 loops are corrected by inclusion of template data. (C) Per-target comparison of CDR H3 loop structure prediction for IgFold and IgFold[Fv-H3], with each point representing the RMSD_{H3} for both methods on a single benchmark target. (D) Superimposition of predicted CDR H3 loop predictions for target 7RDL ($L_{H3} = 20$ residues) for IgFold (RMSD_{H3} = 5.45 Å) and IgFold[Fv-H3] (RMSD_{H3} = 2.86 Å) onto native (gray). (E) Nanobody structure prediction benchmark targets for IgFold without templates, IgFold given the F_V structure without the CDR3 loop (IgFold[Fv-CDR3]), and IgFold given the complete Fv structre (IgFold[Fv]). (F) Per-target comparison of CDR3 loop structure prediction for IgFold [Fv-CDR3], with each point representing the RMSD_{CDR3} for both methods on a single benchmark target. (G) Superimposition of predicted CDR3 loop predictions for target 7CZ0 ($L_{CDR} = 6$ residues) for IgFold (RMSD_{CDR3} = 2.03 Å) and IgFold[Fv-H3] (RMSD_{CDR3} = 1.05 Å) onto native (gray).

³²⁸ our analysis of these structures was limited, we are optimistic that this large dataset will be useful for future studies ³²⁹ and model development.

Despite considerable improvements by deep learning methods for general protein complex prediction, prediction of 330 antibody-antigen binding remains a challenge. Even the recent AlphaFold-Multimer model, which can accurately 331 predict the interactions of many proteins, is still unable to predict how or whether an antibody will bind to a given 332 antigen (13). One of the key barriers to training specialized deep learning models for antibody-antigen complex 333 prediction is the limited availability of experimentally determined structures. The large database of predicted antibody 334 structures presented in this work may help reduce this barrier if it can be employed effectively. In the meantime, 335 IgFold will provide immediate benefits to existing antibody-antigen docking methods. For traditional docking methods, 336 the improvements to speed and accuracy by IgFold should be sufficient to make them more effective (49, 50). For 337 newer docking methods that incorporate structural flexibility, the error estimates from IgFold may be useful for 338 directing enhanced sampling (51). 339

Deep learning methods trained on antibody sequences and structures hold great promise for design of novel 340 therapeutic and diagnostic molecules. Generative models trained on large numbers of natural antibody sequences 341 can produce effective libraries for antibody discovery (28, 29). Self-supervised models have also proven effective 342 for humanization of antibodies (27). Meanwhile, methods like AlphaFold and RoseTTAFold have been adapted for 343 gradient-based design of novel protein structures and even scaffolding binding loops (52, 53). IgFold will enable similar 344 applications, and will additionally be useful as an oracle to test or score novel antibody designs. Finally, embeddings 345 from IgFold (particularly when injected with structural information from templates) will be useful features for future 346 antibody design tasks. 347

Code and Data Availability

Code and pre-trained models for IgFold will be made available at https://github.com/Graylab/IgFold. Paired antibody structures predicted by IgFold for the 104,994 OAS sequences will be made available online shortly. All structures generated by IgFold and alternative methods for benchmarking will be deposited at Zenodo and released upon publication.

353 Methods

A. Predicting antibody structure from sequence. The architecture and training procedure for IgFold are described
 below. Full details of the model architecture hyperparameters are detailed in Table 3. In total, IgFold contains 1.6M
 trainable parameters.

A.1. Generating AntiBERTy embeddings. To generate input features for structure prediction, we use the pre-trained AntiBERTy language model (21). AntiBERTy is a bidirectional transformer trained by masked language modeling on a set of 558M antibody sequences from the Observed Antibody Space. For a given sequence, we collect from AntiBERTy the final hidden layer state and the attention matrices for all layers. The hidden state of dimension $L \times 512$ is reduced to dimension $L \times d_{node}$ by a fully connected layer. The attention matrices from all 8 layers of AntiBERTy (with 8 attention heads per layer) are stacked to form an $L \times L \times 64$ tensor. The stacked attention tensor is transformed to dimension $L \times d_{edge}$ by a fully connected layer.

A.2. IgFold model implementation. The IgFold model takes as input per-residue embeddings (nodes) and inter-residue attention features (edges). These initial features are processed by a series node updates via graph transformer layers (34) and edge updates via triangular multiplicative operations (10). Next, template data is incorporated via fixed-coordinate invariant point attention. Finally, the processed nodes and edges are used to predict the antibody backbone structure via invariant point attention. We detail each of these steps in the following subsections. Where possible, we use the same notation as in the original papers.

Node updates via graph transformer layers. Residue node embeddings are updated by graph transformer (GT) layers, which extend the powerful transformer architecture to include edge information (34). Each GT layer takes as input a series of node embeddings $H^{(l)} = \{h_1, h_2, ..., h_L\}$, with $h_i \in \mathbb{R}^{d_{\text{node}}}$, and edges $e_{ij} \in \mathbb{R}^{d_{\text{edge}}}$. We calculate the multi-head attention for each node *i* to all other nodes *j* as follows:

374	$q_{c,i} = \mathbf{W}_{c,q} h_i$
375	
376	$k_{c,j} = \mathbf{W}_{c,k} h_j$
377	
378	$e_{c,ij} = \mathbf{W}_{c,e} e_{ij}$

$$\alpha_{c,ij} = \frac{\langle q_{c,i}, k_{c,j} + e_{c,ij} \rangle}{\sum_{u \in L} \langle q_{c,i}, k_{c,u} + e_{c,iu} \rangle}$$

where $\mathbf{W}_{c,q}, \mathbf{W}_{c,k}, \mathbf{W}_{c,e} \in \mathbb{R}^{d_{\text{node}} \times d_{\text{gt-head}}}$ are learnable parameters for the key, query, and edge tranformations for the *c*-th attention head with hidden size $d_{\text{gt-head}}$. In the above, $\langle q, k \rangle = \exp \frac{q^T k}{\sqrt{d}}$ is the exponential of the standard scaled dot product attention operation. Using the calculated attention, we aggregate updates from all nodes *j* to node *i* as follows:

 $v_{c,j} = \mathbf{W}_{c,v}h_j$ $\hat{h}_i = \|_c^C \left[\sum_{j \in L} \alpha_{c,ij}(v_{c,j} + e_{c,ij})\right]$

where $\mathbf{W}_{c,v} \in \mathbb{R}^{d_{\text{node}} \times d_{\text{gt-head}}}$ is a learnable parameter for the value transformation for the *c*-th attention head. In the above, \parallel is the concatenation operation over the outputs of the *C* attention heads. Following the original GT, we use a gated residual connection to combine the updated node embedding with the previous node embedding:

391
$$eta_i = ext{sigm}(\mathbf{W}_g[\hat{h}_i;h_i;\hat{h}_i-h_i])$$

392
393
$$h_i^{
m new} = (1-eta_i)h_i + eta_i\hat{h}_i$$

where $\mathbf{W}_{g} \in \mathbb{R}^{3 * d_{\text{node}} \times 1}$ is a learnable parameter that controls the strength of the gating function.

Edge updates via triangular multiplicative operations. Inter-residue edge embeddings are updated using the efficient triangular multiplicative operation proposed for AlphaFold (10). Following AlphaFold, we first calculate updates using the "outgoing" triangle edges, then the "incoming" triangle edges. We calculate the outgoing edge transformations as follows:

$$a_{ij} = \operatorname{sigm}(\mathbf{W}_{a,g}e_{ij})\mathbf{W}_{a,v}e_{ij}$$

401
$$b_{ij} = \operatorname{sigm}(\mathbf{W}_{b,g}e_{ij})\mathbf{W}_{b,v}e_{ij}$$

where $\mathbf{W}_{a,v}, \mathbf{W}_{b,v} \in \mathbb{R}^{d_{edge} \times 2*d_{edge}}$ are learnable parameters for the transformations of the "left" and "right" edges of each triangle, and $\mathbf{W}_{a,g}, \mathbf{W}_{b,g} \in \mathbb{R}^{d_{edge} \times 2*d_{edge}}$ are learnable parameters for their respective gating functions. We calculate the outgoing triangle update for edge ij as follows:

$$g_{ij}^{\text{out}} = \operatorname{sigm}(\mathbf{W}_{c,q}^{out}e_{ij})$$

$$\hat{e}_{ij}^{\text{out}} = g_{ij}^{\text{out}} \odot \mathbf{W}_{c,v}^{\text{out}} \sum (a_{ik} \odot b_{jk})$$

$$s_{ij} \quad g_{ij} \cup \cdots \cup c_{,v} \sum_{k \in L}$$

$$e_{ij}^{\mathrm{new}} = e_{ij} + \hat{e}_{ij}^{\mathrm{o}}$$

where $\mathbf{W}_{c,v}^{out} \in \mathbb{R}^{2*d_{edge} \times d_{edge}}$ and $\mathbf{W}_{c,g}^{out} \in \mathbb{R}^{d_{edge} \times d_{edge}}$ are learnable parameters for the value and gating transformations, respectively, for the outgoing triangle update to edge e_{ij} . After applying the outgoing triangle update, we calculate the incoming triangle update similarly as follows:

$$g_{ij}^{\mathrm{in}} = \mathrm{sigm}(\mathbf{W}_{c,q}^{\mathrm{in}} e_{ij})$$

ain in a train
$$\sum (a - b)$$

$$\hat{e}_{ij}^{\text{in}} = g_{ij}^{\text{in}} \odot \mathbf{W}_{c,v}^{\text{in}} \sum_{k \in L} (a_{ki} \odot b_{kj})$$

$$e_{ij}^{\mathrm{new}} = e_{ij} + \hat{e}_{ij}^{\mathrm{in}}$$

where $\mathbf{W}_{c,v}^{\text{in}} \in \mathbb{R}^{2*d_{\text{edge}} \times d_{\text{edge}}}$ and $\mathbf{W}_{c,g}^{\text{in}} \in \mathbb{R}^{d_{\text{edge}} \times d_{\text{edge}}}$ are learnable parameters for the value and gating transformations, respectively, for the incoming triangle update to edge e_{ij} . Note that a_{ij} and b_{ij} are calulated using separate sets of learnable parameters for the outgoing and incoming triangle updates.

Template incorporation via invariant point attention. To incorporate structural template information into the node embeddings, we adopt the invariant point attention (IPA) algorithm proposed for AlphaFold (10). The updated node and edge embeddings correspond to the single and paired representations, respectively, as described in the original implementation. The IPA layer is followed by a three-layer feedforward transition block as in the original implementation. Because our objective is to incorporate known structural data into the embedding, we omit the translational and rotational updates used in the AlphaFold structure module. We incorporate partial structure

⁴²⁷ information by masking the attention between residue pairs that do not both have known coordinates. As a result,
⁴²⁸ when no template information is provided, the node embeddings are updated only using the transition layers.

Structure realization via invariant point attention. The processed node and edge embeddings are passed to a 429 block of three IPA layers to predict the residue atomic coordinates. Following the structure module of AlphaFold, 430 we adopt a "residue gas" representation, in which each residue is represented by an independent coordinate frame. 431 The coordinate frame for each residue is defined by four atoms (N, C_{α} , C, and C_{β}) placed with ideal bond lengths 432 and angles. We initialize the structure with all residue frames having C_{α} at the origin and task the model with 433 predicting a series of translations and rotations that assemble the complete structure. Contrary to the AlphaFold 434 implementation, we do not share parameters across the IPA layers, but instead learn separate parameters for each 435 layer. 436

A.3. Training procedure. The model is trained using a combination of structure prediction and error estimation loss terms. The primary structure prediction loss is the mean-squared-error between the predicted residue frame atom coordinates (N, C_{α} , C, and C_{β}) and the label coordinates after Kabsch alignment of all atoms. We additionally apply an L1 loss to the inter-atomic distances of the (i, i + 1) and (i, i + 2) backbone atoms to encourage proper bond lengths and secondary structures. Finally, we use an L1 loss for error prediction, where the label error is calculated as the C_{α} deviation of each residue after Kabsch alignment of all atoms belonging to beta sheet residues. The total loss is the sum of the structure prediction loss, the inter-atomic distance loss, and the error prediction loss:

 $\text{Loss}(x_{\text{pred}}, x_{\text{label}}) = L_{\text{coords}} + \text{clamp}(10 \times L_{\text{bonds}}, 1) + L_{\text{error}}$

where x_{pred} and x_{label} are the predicted and experimentally determined structures, respectively. We scale the bond length loss by a factor of 10 (effectively applying the loss on the nanometer scale) and clamp losses greater than 1. Clamping the bond length loss allows the model to learn global arrangement of residues early in training then improve smaller details (e.g., bond lengths) later in training.

⁴⁴⁹ During training we sampled structures evenly between the SAbDab dataset (30) and the paired and unpaired ⁴⁵⁰ synthetic structre datasets. We held out 10% of the SAbDab structures for validation during training. We used the ⁴⁵¹ RAdam optimizer (54) with an initial learning rate of 5×10^{-4} , with learning rate decayed on a cosine annealing ⁴⁵² schedule. We trained an ensemble of four models with different random seeds. Each model trained for 2×10^6 steps, ⁴⁵³ with a batch size of one structure. Training took approximately 110 hours per model on a single A100 GPU.

A.4. Ensemble structure prediction. To generate a structure prediction for a given sequence, we first make predictions
with each of the four ensemble models. We then use the predicted error to select a single structure from the set
of four. Rather than use the average predicted error over all residues, we instead rank the structures by the 90th
percentile residue error. Typically, the 90th percentile residue error corresponds to the challenging CDR3 loop. Thus,
we effectively select the structure with the lowest risk of significant error in the CDR3 loop.

459 B. Benchmarking antibody structure prediction methods.

B.1. Benchmark datasets. To evaluate the performance of IgFold and other antibody structure prediction methods, we
collected a set of high-quality paired and single-chain antibody structures from SAbDab. To ensure none of the deep
learning models were trained using structures in the benchmark, we only used structures deposited after July 1, 2021
(after DeepAb, ABlooper, AlphaFold, and IgFold were trained). Structures were filtered at 99% sequence identity.
From these structures, we selected those with resolution greater than 3.0 Å. Finally, we removed structures with
CDR H3 loops longer than 20 residues (according to Chothia numbering). These steps resulted in 67 paired and 21
single-chain antibody structures for benchmarking methods.

B.2. Alternative methods. We compared the performance of IgFold to four alternative methods for antibody structure 467 prediction: ABodyBuilder, DeepAb, ABlooper, and AlphaFold. ABodyBuilder structures were predicted using the web server. Because the ABodyBuilder web server only allows exclusion of up to 50 PDB structures for grafting, we 469 could not completely restrict access to newer structures. Instead, we omitted structures released after July 1, 2021 470 (benchmark collection date) and with greater than 70% sequence identity. DeepAb structures are generated using 471 the public code repository, with five decoys per sequence as recommended in the publication. ABlooper structures 472 are predicted using the public code repository, with CDR loops built onto grafted frameworks from ABodyBuilder. 473 AlphaFold (and AlphaFold-Multimer) structures were predicted using the public code repository. For nanobody 474 predictions with AlphaFold, we used the CASP14 pre-trained models. For both AlphaFold and AlphaFold-Multimer, 475 we made predictions with all five pre-trained models and selected the highest-ranked structure for benchmarking. 476

Parameter Value		Description		
d _{node} 64		Node dimension		
d_{edge}	64	Edge dimension		
$d_{gt-head}$	32	Graph transformer attention head dimension		
ngt-head	8	Graph transformer attention head number		
$d_{gt-ff-dim}$	256	Graph transformer feedforward transition dimension		
ngt-layers	4	Graph transformer layers		
$d_{\sf ipa-temp-head-scalar}$	16	Template IPA scalar attention head dimension		
$d_{\sf ipa-temp-head-point}$	4	Template IPA point attention head dimension		
$n_{ m ipa-temp-head}$	8	Template IPA attention head number		
$d_{\sf ipa-temp-ff-dim}$	64	Template IPA feedforward transition dimension		
$d_{\sf ipa-temp-ff-layers}$	3	Template IPA feedforward transition layers		
$n_{ m ipa-temp-layers}$	2	Template IPA layers		
$d_{\sf ipa-str-head-scalar}$	16	Structure IPA scalar attention head dimension		
$d_{\sf ipa-str-head-point}$	4	Structure IPA point attention head dimension		
$n_{ m ipa-str-head}$	8	Structure IPA attention head number		
$d_{\sf ipa-str-ff-dim}$	64	Structure IPA feedforward transition dimension		
$d_{\sf ipa-str-ff-layers}$	3	Structure IPA feedforward transition layers		
$n_{ m ipa-str-layers}$	3	Structure IPA layers		
$d_{\sf ipa-err-head-scalar}$	16	Error prediction IPA scalar attention head dimension		
$d_{\sf ipa-err-head-point}$	4	Error prediction IPA point attention head dimension		
nipa-err-head	4	Error prediction IPA attention head number		
$d_{\sf ipa-err-ff-dim}$	64	Error prediction IPA feedforward transition dimension		
dipa-err-ff-layers	3	Error prediction IPA feedforward transition layers		
$n_{\rm ipa-err-layers}$	2	Error prediction IPA layers		

Table 3. IgFold hyperparameters

⁴⁷⁷ We permitted the use of template structures released prior to July 1, 2021, though the AlphaFold authors note that ⁴⁷⁸ templates have a minimal effect on performance.

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