

1 **Noncovalent antibody catenation on a target surface drastically increases**
2 **the antigen-binding avidity**

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21 **ABSTRACT**

22 Immunoglobulin G (IgG) antibodies are widely used for diagnosis and therapy. Given the
23 unique dimeric structure of IgG, we hypothesized that, by genetically fusing a homodimeric
24 protein (catenator) to the C-terminus of IgG, reversible catenation of antibody molecules
25 could be induced on a surface where target antigen molecules are abundant, and that it could
26 be an effective way to greatly enhance the antigen-binding avidity. A thermodynamic
27 simulation shows that quite low homodimerization affinity of a catenator, *e.g.* dissociation
28 constant of 100 μ M, can enhance nanomolar antigen-binding avidity to a picomolar level, and
29 that the fold enhancement sharply depends on the density of the antigen. In a proof-of-
30 concept experiment where antigen molecules are immobilized on a biosensor tip, C-terminal
31 fusion of a weakly homodimerizing protein to two different antibodies enhanced the antigen-
32 binding avidity by at least 210 to 5,120 folds from the intrinsic binding avidity. Thus, the
33 homodimerization-induced antibody catenation would be a simple, powerful and general
34 approach to improve many antibody applications, including the detection of scarce
35 biomarkers and targeted anticancer therapies.

36

37 **Keywords**

38 IgG antibody, on-target antibody catenation, enormous avidity enhancement, innovative
39 technology, anticancer therapy

40

41 **INTRODUCTION**

42 Immunoglobulin G (IgG) antibodies have become the principal therapeutic biologic. IgG
43 antibodies are a homodimer of a heterodimer composed of two copies of each heavy chain
44 (~50 kDa) and light chain (~25 kDa). They have two functional regions: the antigen-binding
45 fragment (Fab) region at the N-terminal end and the fragment crystallizable (Fc) region at the
46 C-terminal end. With an overall shape of the letter Y, the two identical regions of Fab form
47 two arms that can bind two antigen molecules. This antibody-antigen engagement could
48 prevent the antigen from binding to cognate partners or eliminate the antigen molecules from
49 the cell surface by receptor-mediated endocytosis (Liu, 2018). The two copies of Fc form a
50 homodimeric tail that enables a long half-life via binding to the neonatal Fc receptor (FcRn)
51 and exerts effector functions via binding to the Fc γ receptors on effector immune cells or the
52 complement factor C1q (Hogarth and Pietersz, 2012, Lee et al., 2017), which could lead to
53 the death of cells to which antibody molecules are bound (Carter and Lazar, 2018, Goydel
54 and Rader, 2021, Jiang et al., 2011).

55 IgG antibodies have desirable properties for use as a therapeutic drug, including high
56 specificity for a target antigen, low immunogenicity and long serum half-life (Weiner et al.,
57 2010). On the other hand, therapeutic monoclonal antibodies (mAbs) show side effects, albeit
58 to a lesser degree in comparison with conventional chemotherapeutics, such as low or high
59 blood pressure and kidney damage (Hansel et al., 2010). In the case of targeted cancer
60 therapy, where mAbs target a specific antigen on cancer cells, the side effects likely arise due
61 to the expression of the target antigen not only on cancer cells but also on normal cells, which
62 therefore are targeted indiscriminately by mAbs administered in patients (Scott et al., 2012).
63 Moreover, mAbs often suffer from shortcomings such as moderate therapeutic efficacy

64 (resulting in the development of resistance) and their efficacy in a fraction of patients (as
65 observed for mAbs against immune checkpoint inhibitors) (Aldeghaither et al., 2019, Hansel
66 et al., 2010, Wang et al., 2021). Insufficient blockade of target antigens for various reasons,
67 including insufficient antigen-binding affinity, could be responsible for the moderate
68 therapeutic efficacy.

69 In general, diagnostic and therapeutic antibodies are required to exhibit low
70 nanomolar or higher antigen-binding affinity ($K_D < 10$ nM) (Sliwkowski and Mellman, 2013).
71 To reach this level of affinity, laborious experiments for affinity maturation are usually
72 followed after an initial discovery of an antibody (Hoogenboom, 2005). Increasing the
73 valency of binding interaction could be a method of choice. It was shown that irreversibly
74 dimerized monovalent binders can bind targets significantly better than monomeric
75 counterparts (Foreman, 2017). This enhancement of the binding affinity arises from the
76 proximity effect, where the binding of one subunit of the dimer to a target restricts the search
77 space for the other subunit. Reversibly dimerized binders could also exhibit significantly
78 enhanced binding affinity depending on the affinity for binder-target interaction, affinity for
79 homodimerization and the length of the connecting linker, as predicted by a reacted-site
80 probability approach (Foreman, 2017). Such approaches to increase the valency of binding
81 have been applied to IgG antibodies, and a considerable increase in the antigen-binding
82 affinity was observed *in vitro* (White et al., 2014). However, as the size of an IgG-type
83 antibody is large (~150 kDa), irreversible cross-linking or tight reversible dimer formation of
84 the antibody would result in poor solubility and tissue penetration *in vivo*.

85 Owing to the overall dimeric structure, IgG antibodies genetically fused to a
86 homodimeric protein at the C-terminus can be catenated in an arm-in-arm fashion as long as

87 the homodimer can be formed, not within an antibody molecule, but between two antibody
88 molecules. In theory, it would be possible to generate a soluble fusion protein that remains
89 monomeric in solution, but becomes catenated by the proximity effect on a cell surface where
90 target antigen molecules are abundant, provided that the fused protein has appropriately low
91 homodimerization affinity. Importantly, this proximity effect-driven catenation, in turn,
92 should result in enhanced bivalent antigen-binding affinity (=avidity). In this work, by agent-
93 based modeling (ABM) and proof-of-concept experiments, we demonstrate that antibody
94 catenation induced by the intermolecular homodimerization can enormously enhance the
95 antigen-binding avidity of an antibody on a target surface.

96

97 **RESULTS**

98 **The concept of antibody catenation on a target surface**

99 This concept was based on (i) the unique dimeric structure of the IgG-type antibody and (ii) a
100 proximity effect that potentially takes place on a target cell surface. In the structure of IgG,
101 the Fc domain is composed of two copies of the constant regions of the heavy chain (C_{H2} and
102 C_{H3}) forming a homodimer, in which the two C-termini are ~ 23 Å apart and point away from
103 each other (Figure 1A, *Left*). This structural feature indicated that a homodimer-forming
104 protein genetically fused to the C-terminus can be prevented from forming a homodimer
105 intramolecularly by controlling the length of the connecting linker or its homodimerization
106 affinity. Instead, the fusion protein can form a homodimer intermolecularly, and then such a
107 homodimerization could result in a catenation of the antibody molecules (Figure 1A, *Right*).
108 We designate the fusion protein between an antibody and a homodimeric protein as antibody-
109 catenator (^{cat}Ab). A proximity effect for ^{cat}Ab is expected on a target surface where multiple
110 copies of target antigen are present, because the local concentration of ^{cat}Ab on the surface
111 will increase owing to the antibody-antigen binding interaction. Consequently, the
112 homodimerization between the catenator molecules will increase to form catenated antibodies
113 in an arm-in-arm fashion (Figure 1B). Importantly, the effective antigen-binding affinity of
114 ^{cat}Ab will increase in parallel with the catenation, and the fold enhancement would depend on
115 the degree of the catenation. Thus, it appeared possible to enhance the antigen-binding
116 avidity of the IgG-type antibodies by genetically fusing a weakly homodimer-forming protein.

117

118 **Agent-based modeling to simulate the behavior of ^{cat}Ab**

119 ABM is a computational modeling approach that has been employed in a variety of research
120 areas, including statistical physics (Perc et al., 2017, Fu and Wang, 2008) and biological
121 sciences (An et al., 2009, Metzcar et al., 2019, McLane et al., 2011). ABM enables the
122 understanding of macroscopic behaviors of a complex system by defining a minimal set of
123 rules governing microscopic behaviors of agents which compose the system.

124 We constructed an ABM to simulate the behavior of the ^{cat}Ab molecules on a target
125 surface, where target antigen (Ag) molecules form antibody-binding sites. To circumvent
126 complexity, we presumed that each binding site is a pair of two antigen molecules (2Ag), and
127 ^{cat}Ab make a bivalent interaction with the binding site in a 1:1 stoichiometry to form an
128 occupied binding site (^{cat}Ab-2Ag) (Figure 2A, *Left*). For catenation to occur between two
129 adjacent ^{cat}Ab-2Ag complexes, the distance between the centers of two adjacent complexes (d)
130 should be closer than the reach length (L) defined as $l+c/2$, the sum of the linker length (l)
131 and the half the catenator length (c) (Figure 2A, *Right*). Therefore, multiple parameters affect
132 the catenation on the target surface. In our ABM model, we regarded every possible binding
133 site on the target surface as an individual agent in the ABM formalism, and each binding site
134 is assigned to a fixed position on a three-dimensional (3D) surface with a periodic boundary
135 condition. Three rules in our ABM govern the behaviors of the ^{cat}Ab molecules on the target
136 surface. The first rule is about the *intrinsic antibody-antigen binding*. An unoccupied binding
137 site binds to one free ^{cat}Ab through bivalent interaction to form an occupied binding site.
138 Bound ^{cat}Ab may dissociate from the occupied binding site, leaving the binding site
139 unoccupied. The equilibrium population of the occupied and unoccupied binding sites is
140 determined by the antibody's intrinsic avidity for the antigen with no effect of the catenator
141 on the antigen-binding avidity assumed. Then, the relative likelihood of the occupied state
142 compared to the unoccupied state for any binding site (the likelihood of intrinsic antigen

143 binding) is defined as $[\text{catAb-2Ag}]/[2\text{Ag}]$ and thus can be expressed as $[\text{catAb}]/K_D$, where
144 $[\text{catAb}]$ is the concentration of catAb and K_D is the dissociation constant for the bivalent catAb-
145 2Ag interaction (Figure 2B, *Left*). The second rule is about *catenation*. A pair of catAb-2Ag
146 complexes on the target surface can be bridged by intermolecular homodimerization between
147 catenators (Figure 2B, *Middle*). For a pair of catAb-2Ag complexes separated by d (Figure 2A,
148 *Right*), the relative likelihood of the catenation state as compared to the non-catenation state
149 is the ratio of the forward reaction rate (catenation) to the reverse reaction rate (decatenation).
150 The forward reaction rate ($R_{\text{catenation}}$) and the reverse reaction rate ($R_{\text{decatenation}}$) are given as,

$$R_{\text{catenation}} = (k_f)_{\text{catenation}} * \left(\frac{1}{N_A} * \frac{1}{V_{\text{sphere}}} \right)^2 * V_{\text{overlap}}(d)$$

$$R_{\text{decatenation}} = (k_r)_{\text{catenation}} * \frac{1}{N_A}$$

151 , where k_f and k_r are the reaction rate constant of the forward and reverse reaction,
152 respectively, N_A is the Avogadro number, V_{sphere} is the local spherical volume within the
153 reach of the catenator, and $V_{\text{overlap}}(d)$ is the volume where two catenators can come in contact
154 to form a homodimer (Figure 2A, *Right*). In approximating the forward reaction rate, the
155 catenator was assumed to sample V_{sphere} uniformly. The relative likelihood, defined as
156 $R_{\text{catenation}}/R_{\text{decatenation}}$, is then expressed as

$$157 \frac{R_{\text{catenation}}}{R_{\text{decatenation}}} = \frac{(k_f)_{\text{catenator}}}{(k_r)_{\text{catenator}}} * \frac{1}{N_A} * \left(\frac{1}{V_{\text{sphere}}} \right)^2 * V_{\text{overlap}}(d) = \frac{f(d)}{(K_D)_{\text{catenator}}}$$

158 where

$$f(d) = \frac{1}{N_A} * \left(\frac{1}{V_{\text{sphere}}} \right)^2 * V_{\text{overlap}}(d)$$

159 The relative likelihood is thus a function of d , and it is inversely proportional to the
160 dissociation constant of the catenator in the bulk medium, $(K_D)_{\text{catenator}}$. The function $f(d)$ can

161 be viewed as the effective local concentration of the catenator in $V_{\text{overlap}}(d)$. As expected, $f(d)$
162 and thus the relative likelihood is sensitively affected by the reach length and limited by the
163 $^{\text{cat}}\text{Ab}$ - $^{\text{cat}}\text{Ab}$ distance (Figure 2—figure supplement 1). Finally, the third rule is about *restricted*
164 *dissociation* which assumes that catenated antibodies are not allowed to dissociate from the
165 binding site, because the catenated arms would hold the dissociated antibody near its binding
166 site, forcing it to rebind immediately (Liese and Netz, 2018). Under this assumption, antibody
167 molecules are allowed to dissociate from the binding site, only if its catenator is not engaged
168 in the homodimerization with nearby $^{\text{cat}}\text{Ab}$ -2Ag complexes (Figure 2B, *Right*).

169

170 **Simulations show significant enhancement of the antigen-binding avidity**

171 According to the postulated rules, we simulated the effects of the antibody catenation on the
172 binding interaction between $^{\text{cat}}\text{Ab}$ and 2Ag on a three-dimensional surface by using the
173 Markov Chain Monte-Carlo (MCMC) sampling method (Hooten and Wikle, 2010) (see
174 Methods section). Our sampling procedure is composed of three steps (Figure 2C). The first
175 step is an *initialization*, where a target surface with the antibody-binding sites is defined by
176 specifying the coordinates for each site. A set of binding sites are positioned equidistant from
177 each other or randomly positioned, and the inter-site distance or the number of binding sites
178 were set as variables. The next step is an *MCMC stochastic update* step. In each iteration, a
179 binding site is randomly selected from the target surface, and the probability of changing the
180 status of the selected binding site (occupied or not) is calculated by the Metropolis-Hasting
181 algorithm (Hastings, 1970, Grazzini et al., 2017). Then, the ‘on’ or ‘off’ state of this site is
182 updated with the calculated probability. Accordingly, the catenation state is probabilistically
183 updated for each update step. In the following sampling step, the total number of the
184 occupied binding sites is counted, which is then collected through multiple simulation runs

185 for the statistical analysis of the binding site occupancy and the effective antigen-binding
186 avidity. The binding site occupancy is the mean value of the number of occupied binding
187 sites collected for more than 1024 MCMC samplings. For each simulation, we calculated the
188 mean binding occupancy and the effective dissociation constant, $(K_D)_{eff}$, which takes into
189 account the effect of the antibody catenation, and is expressed as:

$$(K_D)_{eff} = \frac{(1 - \text{Binding Site Occupancy}) * [^{cat}Ab]}{\text{Binding Site Occupancy}}$$

190 Since the catenator homodimerization should be affected by how the binding sites are
191 distributed on a 3D surface, simulations were conducted for different arrays of binding sites.
192 In the simulations, $(K_D)_{catenator}$ was the main variable, while other parameters were set
193 constant. First, we simulated the binding sites forming a square lattice to find that the Ab-
194 catenator exhibited enhanced binding site occupancy in a sigmoidal manner, and that it could
195 be enhanced to near full saturation by a catenator that forms a homodimer with quite low
196 binding affinity. For instance, a ^{cat}Ab with $(K_D)_{catenator}$ of $\sim 1 \mu M$ exhibited ~ 70 -fold
197 enhancement of the effective antigen-binding avidity (=reduction of $(K_D)_{eff}$) in comparison
198 with the same antibody without a fused catenator (Figure 3). As a means of comparison
199 across different simulation setups, we employed ' $(K_D)_{catenator,50}$ ' which is defined as the
200 $(K_D)_{catenator}$ that enables half-maximal enhancement of the binding site occupancy (Figure 3).

201

202 **Comparison of the simulations for different arrays of the binding sites**

203 Next, we carried out simulations for other regular arrays of the binding sites and for randomly
204 distributed binding sites. Depending on the pattern of regularly distributed binding sites, the
205 number of possible catenations for a given binding site (designated as connectivity number)
206 varies: 3, 4 and 6 for a hexagonal, square or triangular array of the binding sites, respectively

207 (Figure 4A). These three arrays showed varying but similar enhancement of the binding site
208 occupancy and the effective antigen-binding avidity by the catenator (Figure 4A). As
209 expected, the higher the connectivity number was, the lower $(K_D)_{\text{catenator},50}$ an array exhibited;
210 the $(K_D)_{\text{catenator},50}$ was 8.0, 9.2 and 12.2 μM for the hexagonal, square and triangular array of
211 the binding sites, respectively. The simulations showed that, as the connectivity number
212 increased, the effective antigen-binding avidity increased with the maximum 41-, 73- and 93-
213 fold enhancement for the triangular, square and hexagonal array, respectively (Figure 4A).
214 Thus, regardless of the distribution patterns, the effective antigen-binding avidity could be
215 increased by at least 41 folds under the simulation conditions where the target surface
216 contains only 98 binding sites.

217 For the case of randomly distributed binding sites on a 3D surface, which is relevant
218 to target antigen distribution on cell surfaces, we introduced the binding site density (ρ), the
219 number of binding sites per unit area which is set to the square of the reach length (7 nm)
220 (Figure 4B). In the simulations, the total surface area was 5,760 nm^2 , and the number of
221 binding sites was 15, 30, 45, 90 or 120, which correspond to the ρ of 1.47, 2.94, 4.41, 8.82 or
222 11.76. Denser binding sites would increase the connectivity number for a given binding site.
223 As expected, simulations showed that higher binding site density resulted in a higher level of
224 binding site saturation and a much more significant increase in the effective antigen-binding
225 avidity; the maximum fold enhancement ranged from 15 ($\rho= 1.47$) to 1,062 ($\rho= 11.76$).
226 Likewise, significantly different $(K_D)_{\text{catenator},50}$ values were observed: *e.g.*, 4.2×10^{-6} M at the ρ
227 of 11.76 *versus* 74×10^{-6} M at the ρ of 1.47 (Figure 4B). The maximal saturation and the onset
228 $(K_D)_{\text{catenator}}$, which begins to exert the catenation effect, were also considerably different. Thus,
229 the catenation effects are sensitively affected by the binding site density, in contrast with the
230 all-or-none catenation effect observed for the regular arrays of the binding sites (Figure 4B).

231 In particular, the catenation-induced enhancement of the antigen-binding avidity was
232 remarkably and sensitively affected by the $(K_D)_{\text{catenator}}$ values at high binding site density ($\rho >$
233 4.41) (Figure 4B). Much greater enhancement was observed as we further increased the
234 density of randomly distributed binding sites: ~29,000 maximum fold enhancement at the ρ
235 of 58.8 (Figure 4—figure supplement 1), which roughly corresponds to two hundredths of the
236 density of the HER2 receptor on HER2-overexpressing breast cancer cells (Peckys et al.,
237 2019). Together, our simulations show that randomly distributed binding sites at high density
238 enormously enhance the effective antigen-binding avidity of $^{\text{cat}}\text{Ab}$.

239 Additionally, we performed simulations for different values of $[^{\text{cat}}\text{Ab}]/K_D$ to estimate
240 the effect of K_D with respect to $[^{\text{cat}}\text{Ab}]$. Varying $[^{\text{cat}}\text{Ab}]/K_D$ from 0.01 to 1.0 resulted in 85- to
241 900-fold enhancement of the antigen-binding avidity, suggesting that the catenation effect
242 works for a broad range of K_D values (Figure 4—figure supplement 2).

243

244 **Proof-of-concept experiments**

245 For experimental validation, we chose stromal cell-derived factor 1 α (SDF-1 α) as a catenator.
246 SDF-1 α is a small ($M_r = 8$ kDa) and weakly homodimerizing protein ($K_D = 150$ μM)
247 (Veldkamp et al., 2005), indicating that this protein fused to an antibody by a ~40 Å-long
248 linker would not form an intramolecular homodimer within a fusion protein. By using a 10-
249 residue connecting linker (GGGGSGGGSGG), SDF-1 α was fused to two different antibodies:
250 Trastuzumab(N30A/H91A), a variant of the clinically used anti-HER2 antibody Trastuzumab
251 and gICV30, an antibody against the receptor-binding domain (RBD) of the severe acute
252 respiratory syndrome coronavirus 2 (SARS-CoV-2) spike protein. The Fab fragment of
253 Trastuzumab(N30A/H91A) binds to the ectodomain of HER2 with a K_D of 353 nM (Slaga et
254 al., 2018), and gICV30 binds to the RBD with a similar binding affinity ($K_D = 407$ nM)

255 (Hurlburt et al., 2020). We produced the SDF-1 α -fused antibodies,
256 Trastuzumab(N30A/H91A)-SDF-1 α and gICV-SDF-1 α , and also the unmodified antibodies
257 to compare their binding avidities by bio-layer interferometry (BLI) where respective target
258 antigen was immobilized on a sensor tip. Unlike the similar antigen-binding affinities of the
259 Fab fragments, the binding avidities of the full-form antibodies were quite different in our
260 quantification, Trastuzumab(N30A/H91A) and gICV30 exhibiting the K_D of 2.1 nM and 51.2
261 nM, respectively (Figure 5). The SDF-1 α -fused antibodies exhibited association kinetics
262 similar to those of the mother antibodies; association rate constants (k_a s) of the
263 Trastuzumab(N30A/H91A) and Trastuzumab(N30A/H91A)-SDF-1 α were $1.5 \times 10^5 \text{ Ms}^{-1}$ and
264 $3.1 \times 10^5 \text{ Ms}^{-1}$, respectively. Similarly, those of gICV30 and gICV30-SDF-1 α were 25.0×10^4
265 Ms^{-1} and $5.0 \times 10^4 \text{ Ms}^{-1}$, respectively. However, the two pairs of the antibodies exhibited
266 significantly different dissociation kinetics; dissociation rate constants (k_d s) of the
267 Trastuzumab(N30A/H91A) pair were $3.1 \times 10^{-4} \text{ Ms}^{-1}$ *versus* $< 1.0 \times 10^{-7} \text{ Ms}^{-1}$ and
268 those for the gICV30 pair were $1.3 \times 10^{-4} \text{ Ms}^{-1}$ *versus* $< 1.0 \times 10^{-7} \text{ Ms}^{-1}$ (Figure 5). These
269 observed kinetics are consistent with the expectation that fused SDF-1 α would not affect the
270 association of the antibodies, but would slow down the dissociation of the SDF-1 α -fused
271 antibodies into the bulk solution, as it catenates the antibody molecules on the sensor tip. As a
272 result, Trastuzumab(N30A/H91A)-SDF-1 α exhibited the K_D of $< 10 \text{ pM}$, at least 210-fold
273 higher binding avidity compared with Trastuzumab(N30A/H91A), and likewise, The SDF-1 α
274 fusion to gICV30 increased the binding avidity by at least 5,120 folds, demonstrating that
275 two-digit nanomolar binding avidity of an antibody can be increased to picomolar binding
276 avidity by fusing a weakly homodimerizing protein.

277

278 **DISCUSSION**

279 In the current phage display for antibody screening, many candidates that do not satisfy a
280 required affinity for a target antigen are rejected, although they might have high specificity of
281 binding. A simple and general way of increasing the antigen-binding affinity of antibodies
282 would be highly valuable for various applications of antibodies. Taking advantage of the
283 particular homodimeric structure of IgG antibodies, we put forth a concept to enhance the
284 bivalent antigen-binding interaction by fusing a weakly homodimerizing protein to the C-
285 terminus of Fc. The validity of the concept was tested by simulations based on an ABM and
286 supported by experimental demonstrations.

287 Our ABM with the three postulated rules was the basis for predicting the
288 enhancement of effective antigen-binding avidity. The model has caveats. First, the
289 assumption of uniform density for the fused catenators within a sphere oversimplifies the
290 dynamics of the catenators, which would highly depend on physical contexts, such as
291 molecular orientations and potential intramolecular interaction with the antibody (Zhou,
292 2001). Second, the binding sites representing antigens are fixed on a surface in our model, but
293 in real situations, antigens move their positions, *e.g.*, receptor molecules on cellular
294 membranes (Saxton and Jacobson, 1997). Advanced molecular dynamics simulations
295 incorporated into the ABM would take account of these microscopic details to result in a
296 more accurate prediction of the behaviors of the ^{cat}Ab molecules and the binding sites.
297 Despite these caveats, the simulations provided valuable insights into the proper ranges of the
298 antigen-binding avidity of an antibody and catenator-catenator binding affinity. According to
299 the simulation, we adopted SDF-1 α , a weakly homodimerizing protein (K_b of 150 nM), as a
300 catenator. When fused to antibodies, it resulted in remarkable enhancement of the effective

301 antigen-binding avidity of the antibodies, which was due to drastically reduced rate of
302 dissociation of the fused antibody molecules from the immobilized antigens.

303 The “antibody catenation on a target surface” method presented herein might find
304 practical applications. First, it can be applied to therapeutic antibodies against viruses, which
305 have multiple copies of target antigens on their surface. Second, it can be used for sandwich-
306 type point-of-care biosensors in which a second antibody is catenated to increase the
307 sensitivity of detection. Third, this method can be used to sense biomarkers that exist in a
308 very low number on a target cell (*e.g.*, copy number < 10), which requires an extremely high-
309 binding avidity of a probe antibody. For this application, employing an antibody with high
310 antigen-binding affinity (*e.g.*, $K_D < 1$ nM) and a catenator with high homodimerization
311 affinity (*e.g.*, $(K_D)_{\text{catenator}} < 1$ μ M), would be necessary to overcome low proximity effect due
312 to the scarcely present antigen molecules. Fourth, it might also be applied to antibody-based
313 targeted cancer therapy where side effects arising from antibody binding to normal cells are a
314 general problem. Since cancer-associated antigen molecules are lower in number on normal
315 cells than they are on cancer cells, catenated anticancer antibodies would be concentrated on
316 the surface of cancer cells, because the effective binding avidity of a ^{cat}Ab depends on the
317 number of antigen molecules on a target surface. In particular, this approach would greatly
318 reduce the intrinsic toxicity of antibody-drug conjugates that are widely used currently. Of
319 note, a catenator fused to the C-terminus of Fc would not affect the effector functions of Fc
320 through the Fc γ receptor-binding site and FcRn binding site on it. We observed that ^{cat}Ab
321 molecules could be internalized into HER2-positive cells presumably via receptor-mediated
322 endocytosis (data not shown).

323 In conclusion, the presented strategy of the antibody catenation on a target surface is
324 simple and powerful, and thus it could be widely applicable, although the homodimerization
325 affinity of a catenator and the length of the linker need to be optimized case by case.
326 Improvement of the simulation method will better guide the decision on the variables in
327 constructing catenator-fused antibodies.

328

329 **Materials and Methods**

330 **MCMC simulation**

331 Simulation runs were carried out in the three steps stated below with specification of the
332 target surface, K_D (for antibody-antigen interaction), $(K_D)_{\text{catenator}}$ (for catenator-catenator
333 interaction) and $f(d)$ (effective local concentration of the catenator). In all simulations, the
334 number of $^{\text{cat}}\text{Ab}$ was far more than that of the binding sites, and therefore, the concentration
335 of free $^{\text{cat}}\text{Ab}$ was assumed to be the same as that of total $^{\text{cat}}\text{Ab}$ (free $^{\text{cat}}\text{Ab}$ + antigen-bound
336 $^{\text{cat}}\text{Ab}$). Simulation parameters their set values are listed in Table 1.

337 Step 1. Initialization step

- 338 1. A specified 3D target surface is implemented by assigning binding sites to specific
339 locations on the surface.
- 340 2. Each binding site is set to be unoccupied.

341 Step 2. MCMC stochastic update step

342 The following sub-steps (1-3) are iterated sufficient times to ensure thermodynamic
343 equilibration.

- 344 1. A random binding site BSI is chosen from the target surface.
- 345 2. The binding status of BSI is updated.
346 If BSI is unoccupied, its status is changed to the occupied status with the acceptance
347 probability of $\max(1, \frac{[^{\text{cat}}\text{Ab}]}{K_D})$.
348 If BSI is occupied, its status is changed to the unoccupied status with the acceptance
349 probability of $\max(1, \frac{K_D}{[^{\text{cat}}\text{Ab}]})$.
- 350 3. An occupied binding site $BS2$ right next to BSI is picked on the target surface, and the
351 catenation status of the pair ($BSI, BS2$) is updated.

352 If (BS_1, BS_2) is uncatenated, and if both BS_1 and BS_2 have an unengaged catenator, its
353 status is changed to the catenation status with the acceptance probability of
354 $\max(1, \frac{f(d)}{(K_D)_{catenator}})$.

355 If (BS_1, BS_2) is catenated, its status is changed to the uncatenated status with the
356 acceptance probability of $\max(1, \frac{(K_D)_{catenator}}{f(d)})$

357 Step 3. Sampling step

358 1. The update step is stopped, and the final status of the target surface is recorded.

359 2. The total number of occupied and unoccupied binding sites are counted.

360

361 The codes for the model system and simulations are available in MATLAB and available on

362 Github (https://github.com/JinyeopSong/Antibody_ThermoCalc_JY). The detailed

363 description is provided in Readme.

364

365 **Preparation of antibodies and catenator-fused antibodies**

366 Each DNA fragment encoding heavy chain variable regions (V_H) and light chain variable

367 regions (V_L) of gICV30 were synthesized (IDT) and cloned into the pCEP4 vector

368 (Invitrogen). DNA fragments of C_{H1} - C_{H2} - C_{H3} of the gamma heavy chain and C_L of the kappa-

369 type light chain were inserted into the V_H and V_L , and the resulting vectors were named

370 gICV30 Hc and gICV30 Lc, respectively. DNA fragment encoding SDF-1 α was synthesized

371 (IDT) and cloned into the gICV30 Hc next to C_{H3} of gICV30 with (Gly-Gly-Gly-Gly-Ser)₂

372 linker sequence (gICV30-SDF-1 α Hc). For antibody production, the three vectors were

373 amplified using the NucleoBond Xtra Midi kit (Macherey-Nagel), and a combination of the

374 gICV30 Hc and gICV30 Lc vectors or a combination of the gICV30-SDF-1 α Hc and gICV30

375 Lc vectors were introduced into the CHO-S cells (Gibco). The transfected cells were grown

376 in the ExpiCHO expression medium (Gibco) for ten days post-transfection. Supernatants
377 were collected by centrifugation at 4 °C, filtered through 0.45 µm filters (Millipore), diluted
378 by the addition of a binding buffer (150 mM NaCl, 20 mM Na₂HPO₄, pH 7.0) to a 1:1 ratio,
379 loaded onto an open column containing Protein A resin (Sino Biological), and eluted with an
380 elution buffer (0.1 M glycine, pH 3.0). The eluent was immediately neutralized by a
381 neutralizing buffer (1M Tris-HCl, pH 8.5), and the antibodies were further purified using a
382 HiLoad 26/60 Superdex 200 gel-filtration column (Cytiva) equilibrated with a buffer solution
383 containing 20 mM Tris-HCl (pH 7.5) and 150 mM NaCl. For preparing
384 Trastuzumab(N30A/H91A) and Trastuzumab(N30A/H91A)-SDF-1 α , each DNA fragment
385 encoding V_H and V_L(N30A/H91A) of Trastuzumab was synthesized (IDT). The cloning,
386 protein production and purification procedures were virtually identical to those used for
387 gICV30 and gICV30-SDF-1 α .

388

389 **Bio-layer interferometry**

390 BLI experiments were performed to measure dissociation constants using an Octet R8
391 (Sartorius). Biotinylated SARS-CoV-2 RBD (Acrobio system) or biotinylated Her2/ERBB2
392 (Sino Biological) was loaded to a streptavidin biosensor tip (Sartorius) for 120 s. A baseline
393 was determined by incubating the sensor with Kinetics Buffer (Sartorius) for 60 s. Antibody
394 samples at different concentrations went through the association phase for 240 s and the
395 dissociation phase for 720 s. All reactions were carried out in the Kinetics Buffer (Sartorius).
396 The binding kinetics were analyzed using the Octet DataAnalysis 10.0 software (Sartorius) to
397 deduce the kinetic parameters. Experiments were performed in triplicate for gICV30 and
398 gICV30-SDF-1 α and duplicate for Trastuzumab(N30A/H91A) and
399 Trastuzumab(N30A/H91A)-SDF-1 α .

400

401 **Figure preparation**

402 The computational models of an antibody and an antibody-catenator in Figure 1A were
403 generated by using the ROSETTA software (Leman et al., 2020), and are presented by
404 PyMOL (DeLano, 2004).

405

406 **ACKNOWLEDGMENTS**

407 This work was supported by the Samsung Research Funding & Incubation Center of
408 Samsung Electronics under Project Number SRFC-MA2002-06.

409

410 **AUTHOR CONTRIBUTIONS**

411 B.-H.O. directed the work, and B.-S.J., J.S., W.C. and M.-J.A. further conceptualized the
412 research. J.S. performed simulations. B.-S.J., S.-W.K. and S.-B.I. performed cloning and
413 purification of the antibodies and the SARS-CoV-2 RBD. B.-H.O., J.S., B.-S.J. and W.C.
414 wrote the original draft. All authors reviewed and accepted the final manuscript.

415

416 **DISCLOSURE OF INTEREST**

417 B.-H.O., B.-S.J., J.S., S.-B.I. and S.-W.K. are co-inventors in a patent application covering
418 the antibody catenation method presented in this article.

419

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517

518

519 **FIGURE LEGENDS**

520 **Figure 1. The concept of antibody catenation on a target surface by fusion of a catenator.**

521 (A) Molecular model for catenator-fused antibodies. A flexible linker (Gly-Gly-Ser) between
522 Fc and the catenator and the hinge segment between Fc and Fab were modeled by using the
523 ROSETTA software. The catenator is an α -helical hairpin that forms four-helix anti-parallel
524 coiled coils (PDB entry: 1ROP). The structure of Fc was derived from the IgG1 antibody
525 (PDB entry: 1IGY) and that of Fab from an antibody against the receptor-binding domain of
526 the SARS-CoV-2 spike protein (PDB entry: 6XE1).

527 (B) Decreased dissociation by antibody catenation. Pairs of $^{\text{cat}}$ Ab-antigen complexes adjacent
528 to each other can be catenated, and the $^{\text{cat}}$ Ab molecules are increasingly harder to dissociate
529 from each other with increased catenation. The effective antigen-binding avidity would
530 increase owing to a decreased off rate of $^{\text{cat}}$ Ab.

531

532 **Figure 2. ABM for simulating the binding dynamics of a catenator-fused antibody.**

533 (A) (Left) Each binding site is composed of two antigen molecules (2Ag). (Right) The grey
534 circles indicate the sphere sampled by the catenator, and V_{overlap} is the overlapping volume
535 between the adjacent spheres. Catenation between two $^{\text{cat}}$ Ab molecules is possible only in
536 V_{overlap} .

537 (B) The three rules of the ABM model. (Left) $^{\text{cat}}$ Ab-2Ag binding occurs with a relative
538 likelihood, $[^{\text{cat}}\text{Ab}]/K_D$. (Middle) The catenation between adjacent $^{\text{cat}}$ Ab-2Ag complexes
539 occurs with an indicated relative likelihood, $f(d)/(K_D)_{\text{Catenator}}$, determined by $(K_D)_{\text{Catenator}}$ and
540 the inter-complex distance d . (Right) It was assumed that $^{\text{cat}}$ Ab molecules that are catenated
541 cannot dissociate from the surface.

542 (C) The simulation requires specification of the parameters for the binding site, antibody and
543 catenator. Through the MCMC sampling, the state of binding sites on the target surface is
544 iteratively updated with the ABM rules and eventually sampled. A sufficient number of
545 sampling results are collected to quantify the binding occupancy and the effective
546 dissociation constant.

547

548 **Figure 3. Simulations of the binding site occupancy and $(K_D)_{\text{eff}}$ in response to $(K_D)_{\text{catenator}}$.**

549 (Left) Binding site occupancy. The simulations were carried out for a square array of the
550 binding sites. The values for a set of variables were $K_D = 10^{-8}$ M, $[\text{catAb}] = 10^{-9}$ M, reach
551 length = 7 nm, spacing between the binding sites = 12 nm and the number of total binding
552 sites = 98. The mean value and standard deviations of 1024 MCMC simulations for each
553 $(K_D)_{\text{catenator}}$ value are shown in blue, and the data are shown as a scatter plot of representative
554 runs (orange).

555 (Right) The effective dissociation constant. The data shown on the left were converted into
556 the $(K_D)_{\text{eff}}$ values. The dashed line represents the K_D value for the same antibody without a
557 catenator. The maximum fold enhancement of the effective binding avidity, which is
558 equivalent to the reduction of $(K_D)_{\text{eff}}$, is 70.6.

559

560 **Figure 4. Simulations for different arrays of the binding sites.**

561 (A) Comparison for regularly distributed binding sites. Three different regular arrays of the
562 binding sites are shown at the top. The black dots represent the binding sites and grey lines
563 the connectable pairs by the catenators. The red circles and the blue lines represent the
564 maximum range of catenation and the connectivity number, respectively, for a given binding
565 site. Binding site occupancy and $(K_D)_{\text{eff}}$ in response to $(K_D)_{\text{catenator}}$ are shown at the bottom.

566 1024 trials were sampled for each $(K_D)_{\text{catenator}}$ value and the results are plotted. The variables
567 were $K_D = 10^{-8}$ M, $[\text{cat Ab}] = 10^{-9}$ M, reach length = 7 nm, spacing between the binding sites = 12
568 nm, and the number of total binding sites were 98 for the square array and 102 for hexagonal
569 and triangular array, respectively. The numbers on the right are the maximum fold
570 enhancement of the effective binding avidity for each array.

571 **(B)** Comparison for randomly distributed binding sites. Three random arrays of the binding
572 sites with different binding site density (ρ) are shown at the top. The surface area for the
573 simulation was $5,760 \text{ nm}^2$. The simulation conditions were the same as in (A). Binding site
574 occupancy and $(K_D)_{\text{eff}}$ in response to $(K_D)_{\text{catenator}}$ are plotted as in (A).

575

576 **Figure 5. BLI runs demonstrating the effect of catenation on the binding avidity.**

577 The binding kinetics were measured with the indicated targets immobilized on a sensor tip.
578 The concentration of the antibodies was varied as shown. The experimental signals and fitted
579 curves are shown in red and black, respectively. For curve fitting, 1:1 binding was assumed.
580 The kinetic parameters are shown in the insets. k_a , association rate constant; k_d , dissociation
581 rate constant.

582 **(A)** High-affinity antibody. Trastuzumab(N30A/H91A) exhibited the K_D of 2.1 nM for the
583 immobilized ectodomain of HER2.

584 **(B)** Low-affinity antibody. gICV30 exhibits the K_D of 51.2 nM for the immobilized RBD of
585 SARS-CoV-2. For both Trastuzumab(N30A/H91A)-SDF-1 α and gICV30-SDF-1 α , the K_D
586 values could not be accurately determined due to the instrumental insensitivity ($K_D < 10$ pM).

587 The experiments were performed in triplicates, and representative sensorgrams are shown.

588

589 **Figure supplements**

590 **Figure 2—figure supplement 1. Calculation of $f(d)$ using uniform local density**
591 **approximation.**

592 The forward catenation rate at which two catenators dimerize is proportional to the
593 volumetric overlap ($V(d)$) between the effective concentration of the catenator, which is
594 assumed to be uniformly distributed over a sphere defined by the reach length (L). $V(d)$
595 depends on the distance (d) between the two adjacent ^{cat}Ab-2Ag complexes as well as the
596 reach length. Shown on the left is a plot of $f(d)$ as a function of d calculated for the indicated
597 reach length (L).

598

599 **Figure 4—figure supplement 1. Simulations for randomly distributed, high-density**
600 **binding sites.**

601 1024 trials were sampled for each $(K_D)_{\text{catenator}}$ value at the indicated density and the results are
602 plotted. The variables were $K_D = 10^{-8}$ M, $[\text{catAb}] = 10^{-9}$ M, reach length= 7 nm, spacing
603 between the binding sites= 12 nm, and the surface area= 5,760 nm². The maximum fold
604 enhancement of the effective binding avidity and $(K_D)_{\text{catenator},50}$ are tabulated at the bottom.

605

606 **Figure 4—figure supplement 2. Influence of the likelihood of intrinsic antigen binding**
607 **($[\text{catAb}]/K_D$) on binding site occupancy and $(K_D)_{\text{eff}}$.**

608 **(A)** The binding occupancy and **(B)** The effective dissociation constant $(K_D)_{\text{eff}}$ in response to
609 $[\text{catAb}]/K_D$ for $[\text{catAb}]/K_D = 1.0, 0.3, 0.1, 0.03, 0.01$. The simulations were carried out with a
610 square array of the binding sites as in Figure 3. The set values for the variable parameters
611 were $[\text{catAb}] = 10^{-9}$ M, reach length= 7 nm, spacing between the binding sites= 12 nm and the
612 number of total binding sites= 98. The mean binding occupancy of 1024 MCMC simulations
613 was plotted. $(K_D)_{\text{catenator}}$ was varied from 3 mM to 30 nM. The antibody binding avidity is
614 substantially enhanced across a broad range of $[\text{catAb}]/K_D$.

615

616 **Table 1. Simulation specifications**

617 The definition and values of the parameters used in the presented simulations are tabulated:

Parameters	Description	Values
Specification of ^{cat}Ab		
K_D	Dissociation constant of antibody	10 nM
$(K_D)_{\text{catenator}}$	Dissociation constant of catenator	10 nM-10 mM
$[\text{catAb}]$	Antibody concentration	1 nM
l	Length of the flexible linker	6 nm
c	Length of the catenator	2 nm
L	Reach length ($l+c/2$)	7 nm
Specification of the target surface		
$N_{\text{total_binding_sites}}$ (in Fig. 3,4)	Number of antibody-binding sites	98 - 102
Connectivity number (in Fig. 3,4)	Number of possible catenation	3 (Hexagonal) 4 (Square) 6 (Triangular)
d (in Fig. 3,4)	Distance between adjacent binding sites	12 nm
L_{surface} (in Fig. 4)	Surface area of the target surface	40 nm ²
Binding site density (in Fig. 4)	Surface density of the binding sites	1.47-11.76 (per 7x7 nm ²)
Specification of Simulation		
Updates/MCMC step	Number of updates in one MCMC step	30,000-100,000
Sampling size	Number of sampling for a parameter set	1,024

618

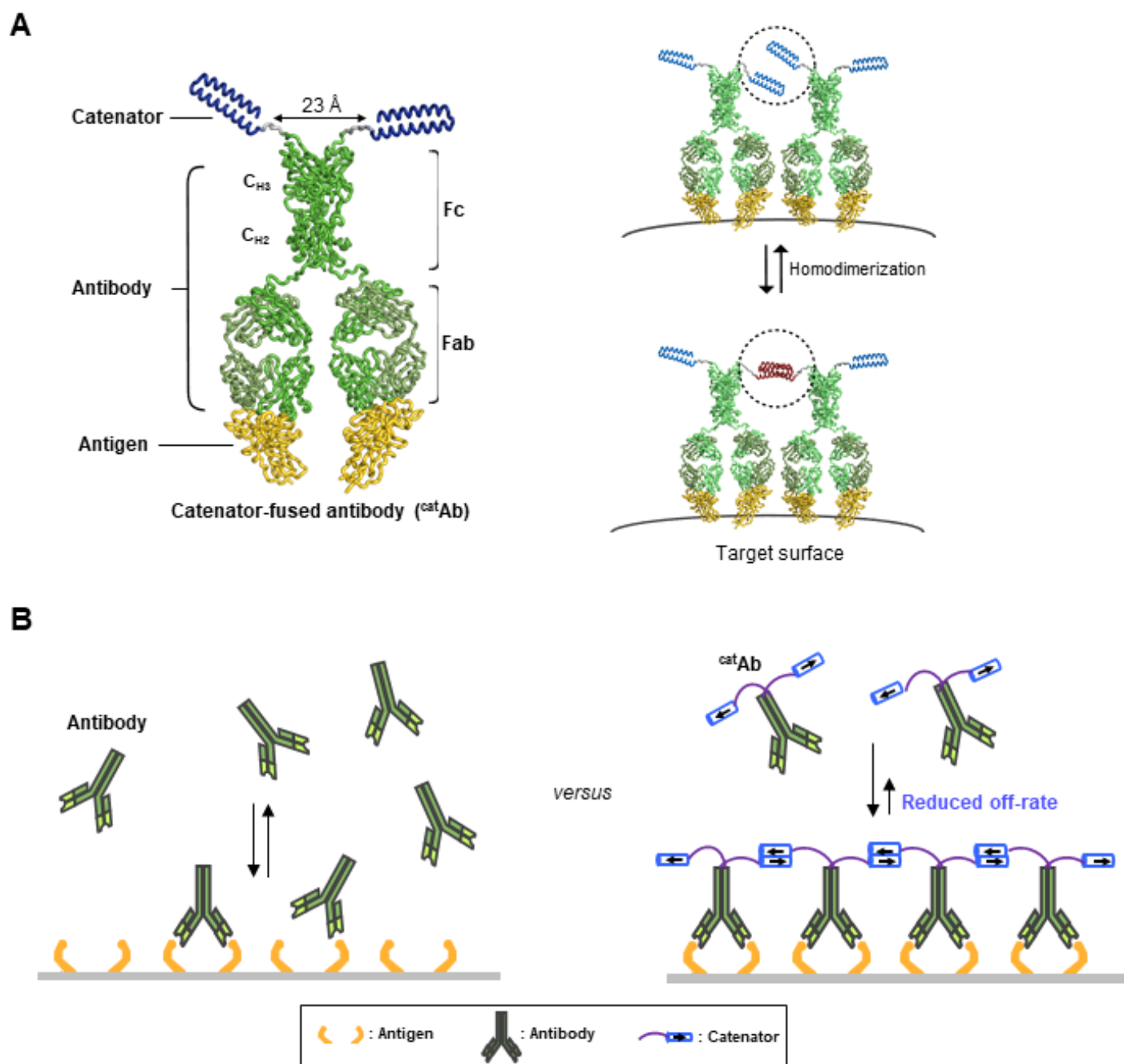
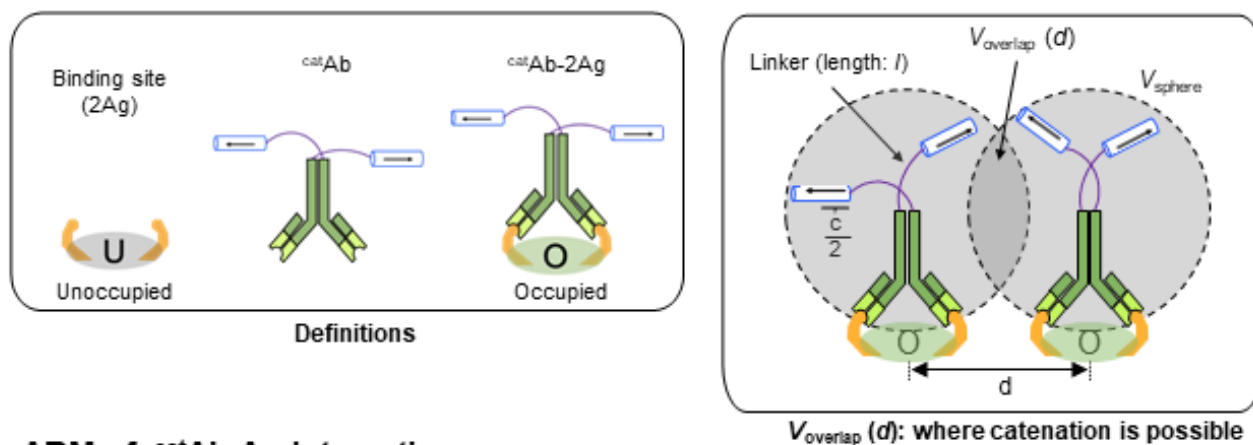
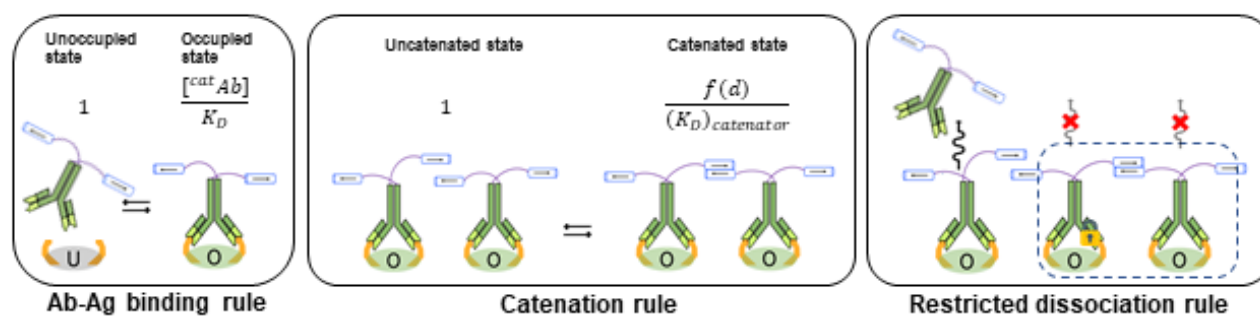


Figure 1

A Conditions for catenation



B ABM of catAb-Ag interaction



C Simulation procedure

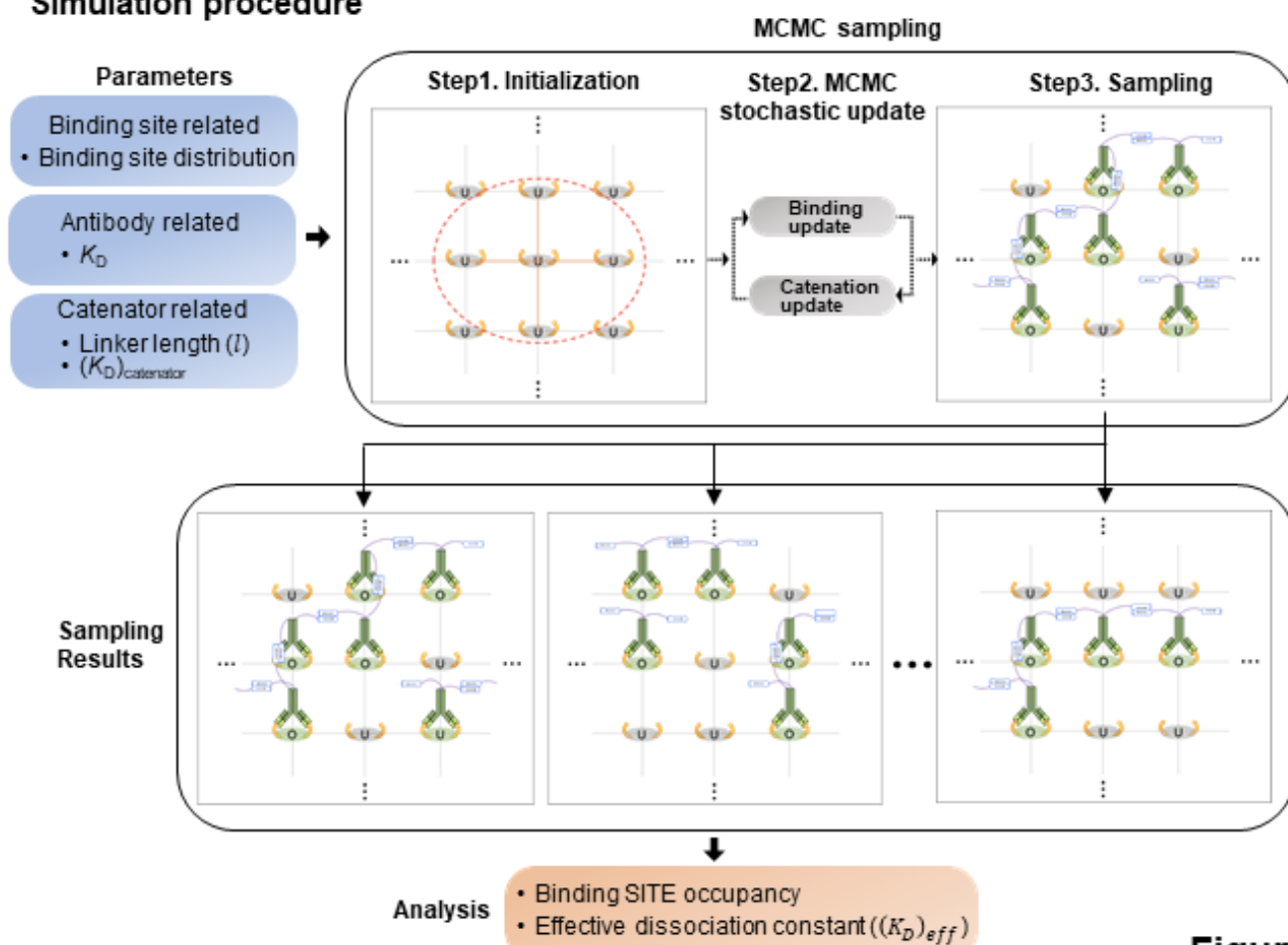
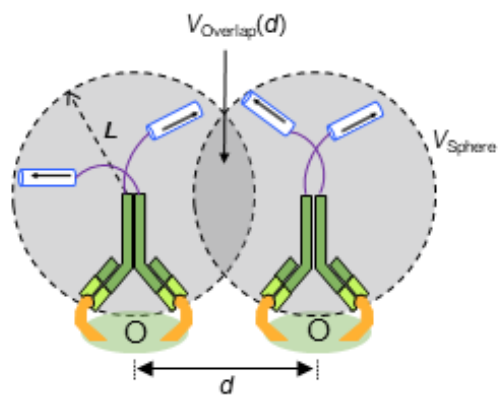


Figure 2

A



$$f(d) = \frac{1}{N_A} \times \left(\frac{1}{V_{\text{Sphere}}} \right)^2 \times V_{\text{Overlap}}(d)$$

B

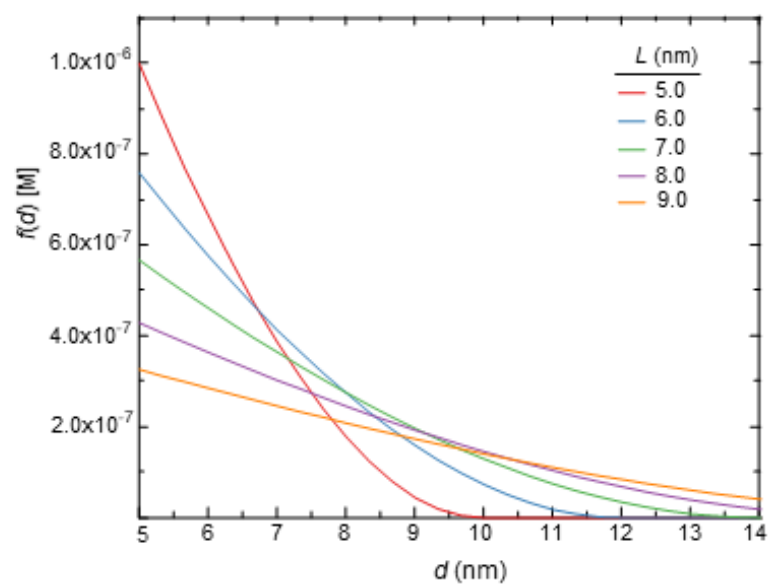


Figure 2—figure supplement 1

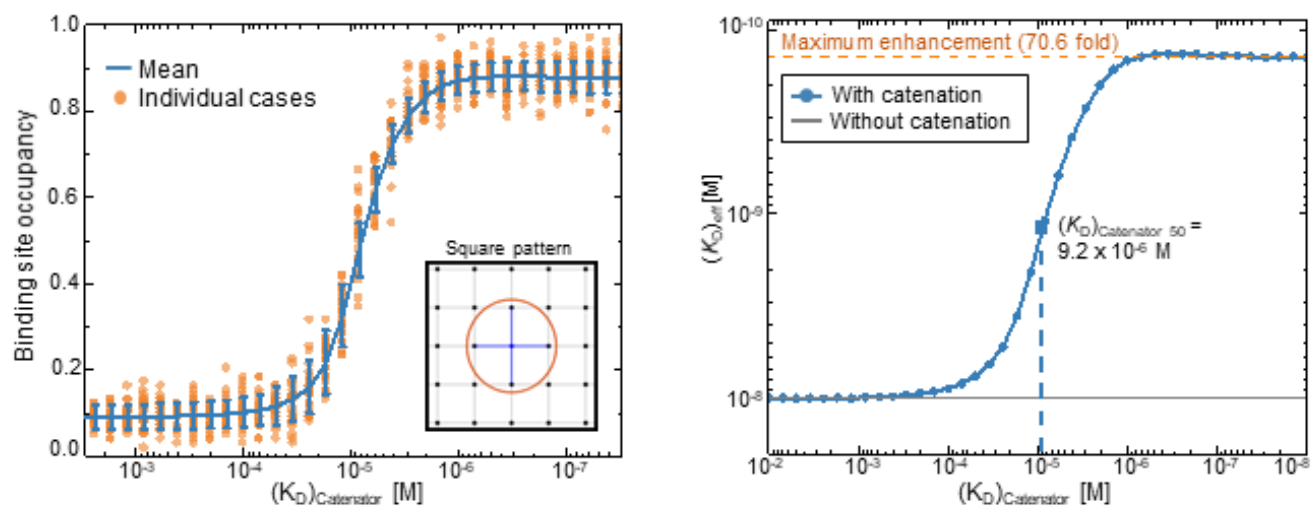
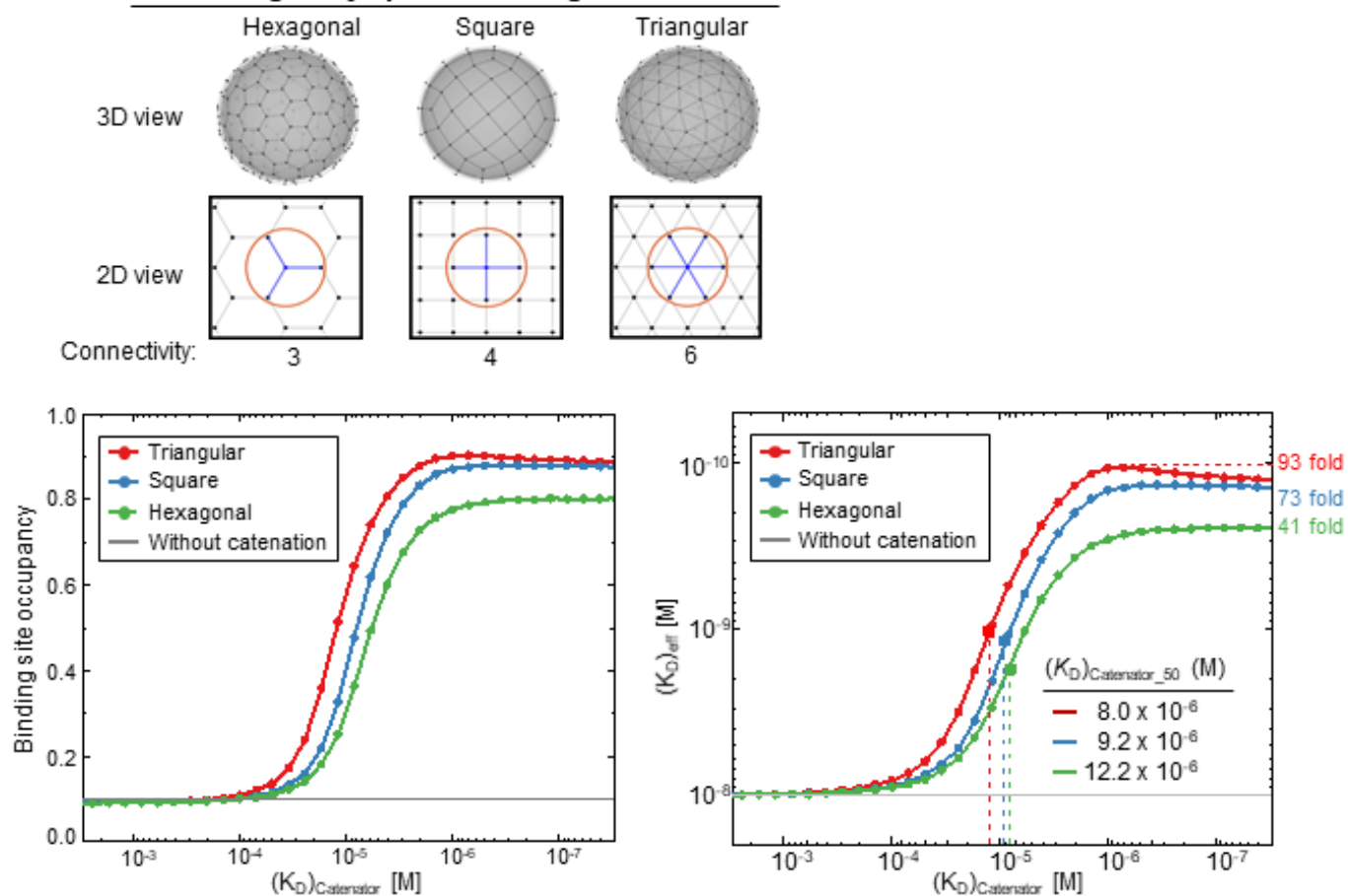


Figure 3

A

Regularly spaced binding sites



B

Irregularly spaced binding sites

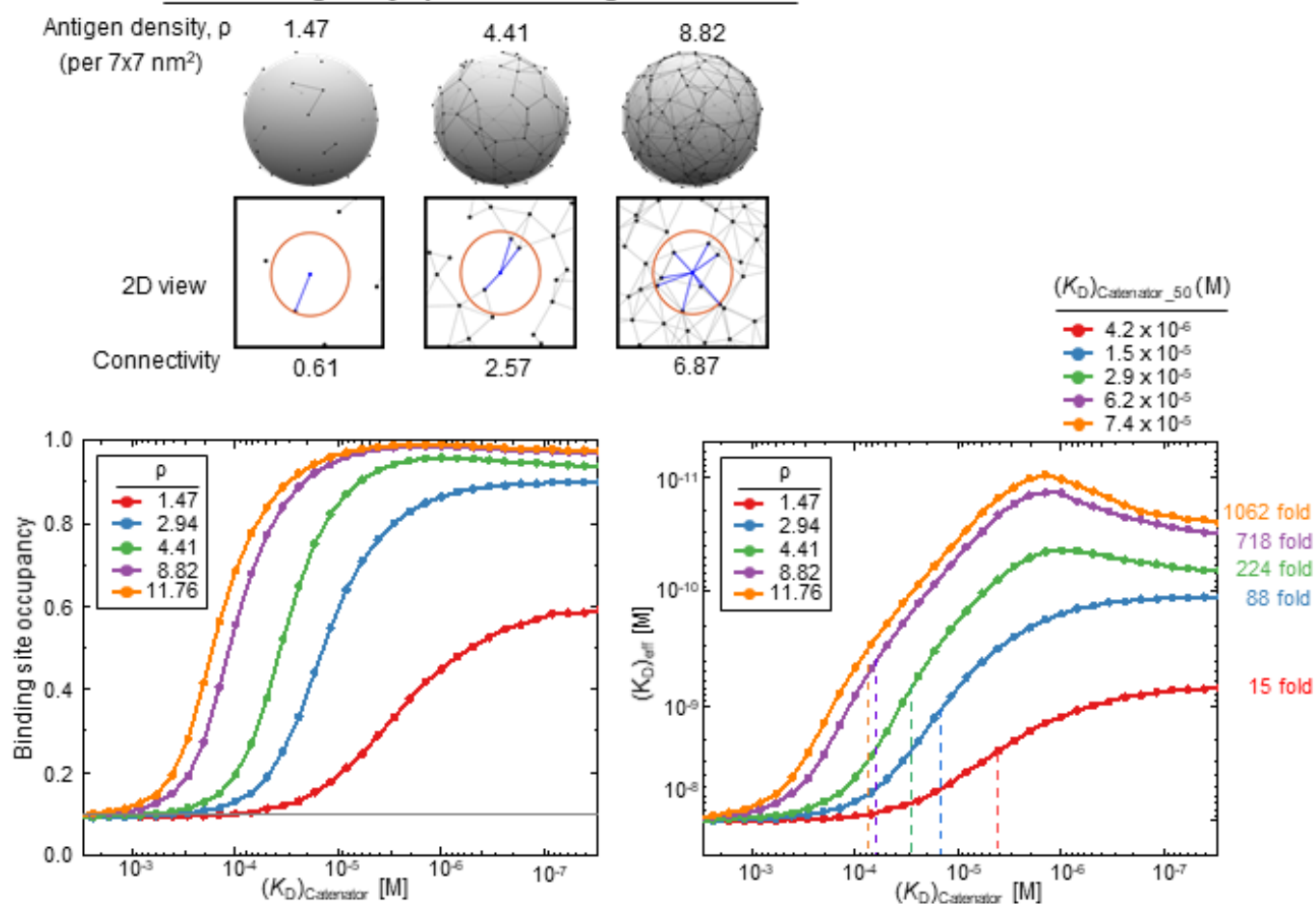
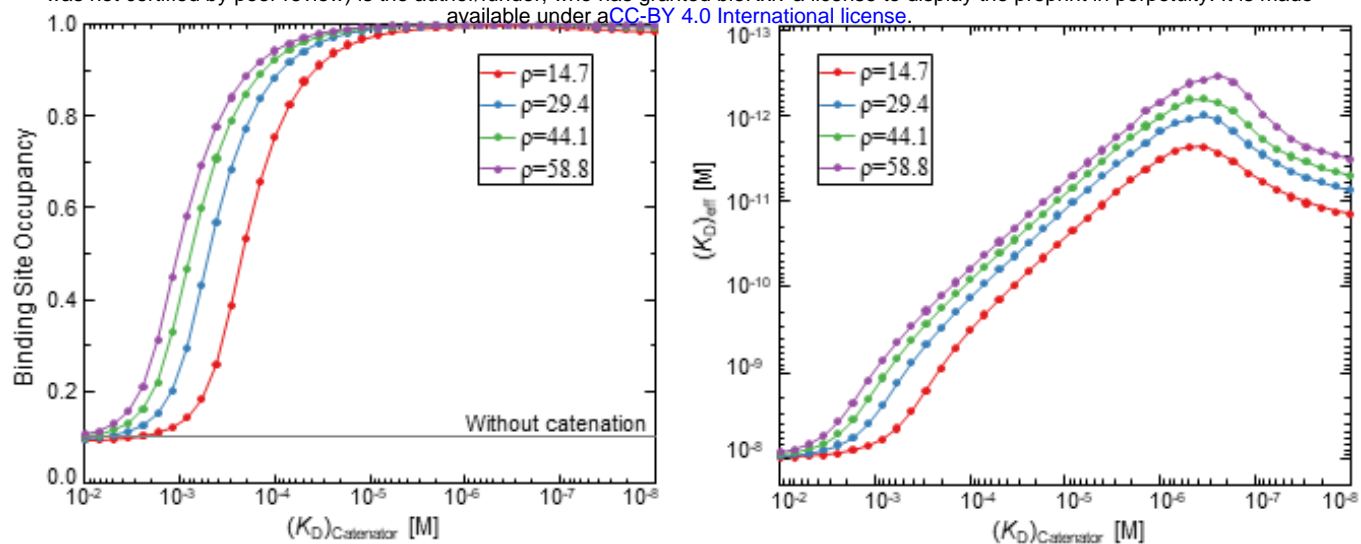


Figure 4



ρ	Maximum enhancement	$(K_D)_{\text{Catenator},50}$ (M)
14.7	4256.7	$5.25 \cdot 10^{-5}$
29.4	9986.3	$8.50 \cdot 10^{-5}$
44.1	15401.4	$9.00 \cdot 10^{-5}$
58.8	28988.2	$9.50 \cdot 10^{-5}$

ρ : Number of binding sites per $7 \times 7 \text{ nm}^2$

Figure 4—figure supplement 1

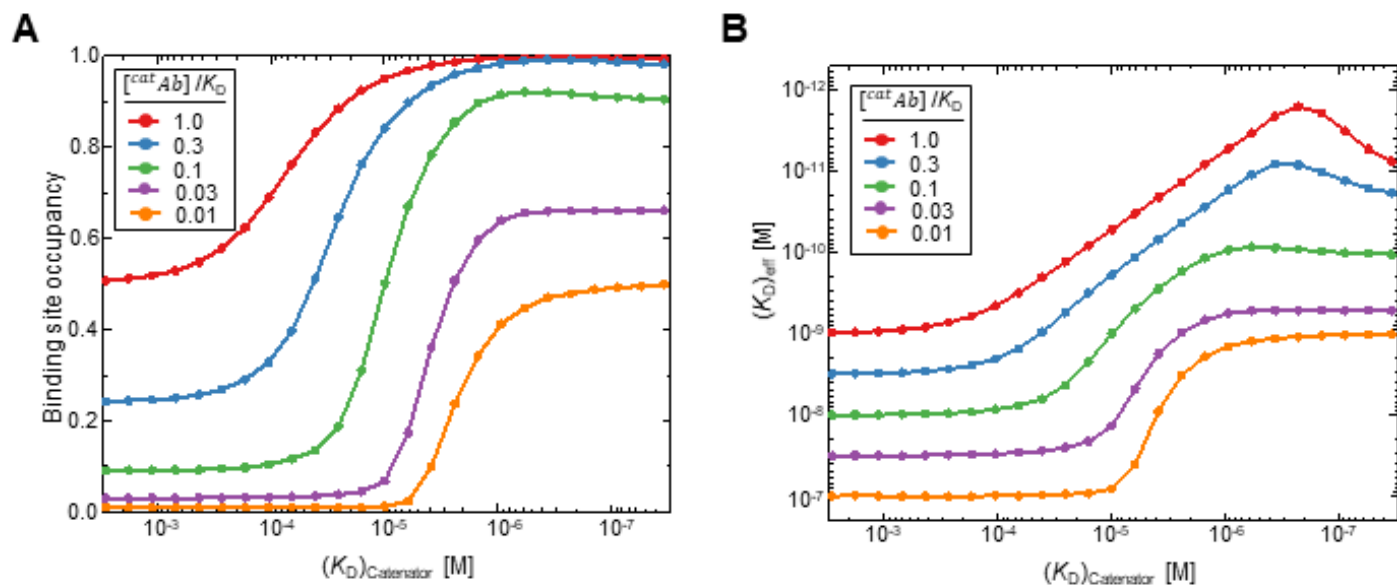


Figure 4—figure supplement 2

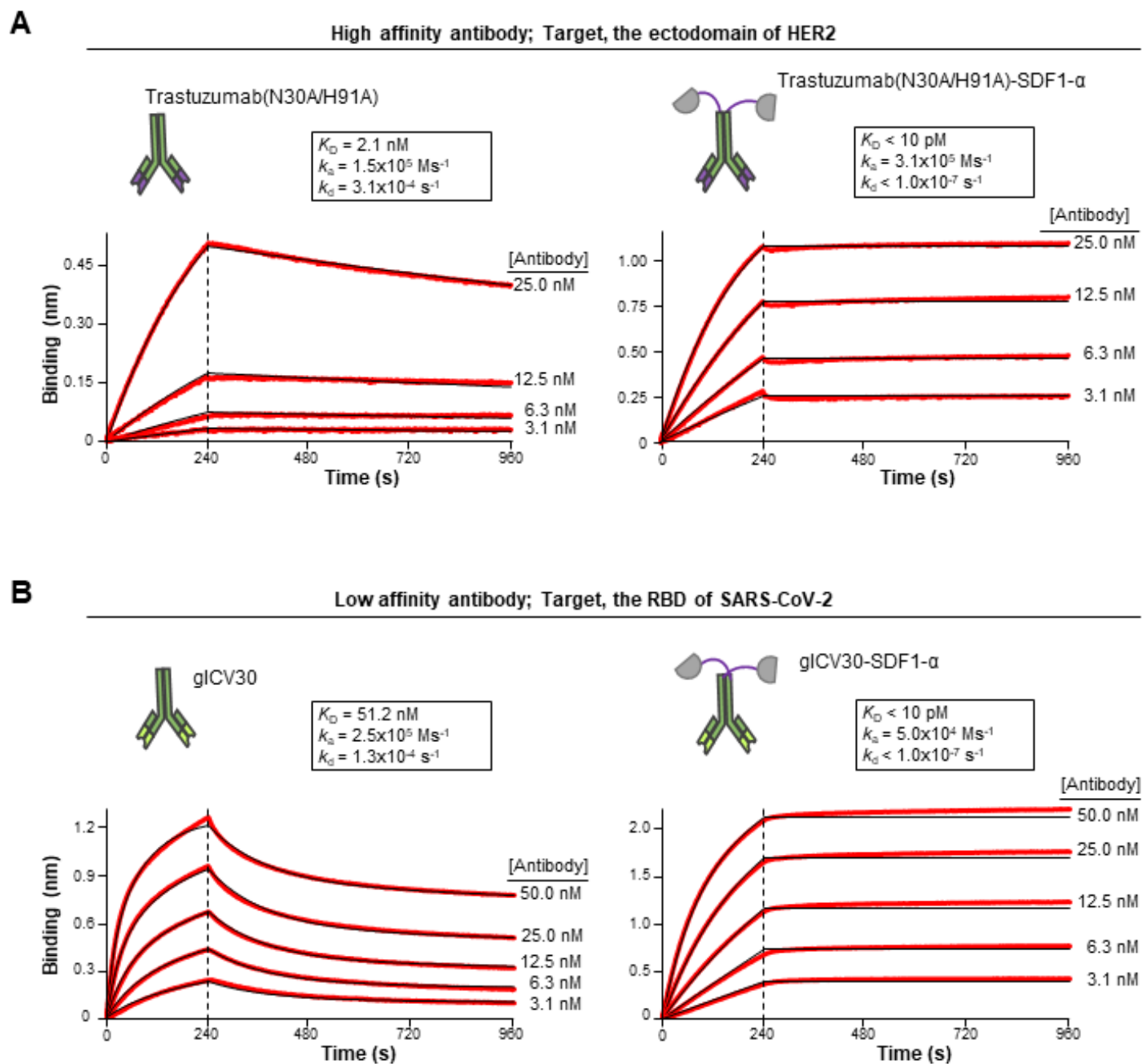


Figure 5