Deciphering the brain’s structure-function relationship is key to understanding the neuronal mechanisms underlying perception and cognition. The cortical column, a vertical organization of neurons with similar functions, is a classic example of primate neocortex structure-function organization. While columns have been identified in primary sensory areas using parametric stimuli, their prevalence across higher-level cortex is debated. A key hurdle in identifying columns is the difficulty of characterizing complex nonlinear neuronal tuning, especially with high-dimensional sensory inputs. Here, we asked whether area V4, a mid-level area of the macaque visual system, is organized into columns. We combined large-scale linear probe recordings with deep learning methods to systematically characterize the tuning of >1,200 V4 neurons using in silico synthesis of most exciting images (MEIs), followed by in vivo verification. We found that the MEIs of single V4 neurons exhibited complex feature selectivities like textures, shapes, or even high-level attributes such as eye-like structures. Neurons recorded on the same silicon probe, inserted orthogonal to the cortical surface, were selective to similar spatial features, as expected from a columnar organization. We quantified this finding using human psychophysics and by measuring MEI similarity in a non-linear embedding space, learned with a contrastive loss. Moreover, the selectivity of the neuronal population was clustered, suggesting that V4 neurons form distinct functional groups of shared feature selectivity, reminiscent of cell types. These functional groups closely mirrored the feature maps of units in artificial vision systems, hinting at shared encoding principles between biological and artificial vision. Our findings provide evidence that columns and functional cell types may constitute universal organizing principles of the primate neocortex, simplifying the cortex’s complexity into simpler circuit motifs which perform canonical computations.

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Introduction

From the intricate layering of neurons with diverse functions in the retina (e.g. Masland, 2001) to the topographic maps of the cerebral cortex (e.g. Penfield & Boldrey, 1937), for decades neuroscientists have been pursing the quest to discover general organizing principles that relate the structure (anatomy) and function (physiology) of the brain. For instance, the concept of functional cortical columns, discovered by Mountcastle (1957) in the somatosensory cortex and later in the primary visual cortex (V1) by Hubel & Wiesel (1968), has been hypothesized to represent a fundamental computational circuit motif repeated throughout the primate neocortex (discussed in Horton & Adams, 2005). In this arrangement, neurons with similar function are vertically organized across cortical layers. Considering that connections within the cortex are locally dense and span cortical layers, this configuration enables neurons with similar response functions to synaptically interact, thereby facilitating computations to transform information within and across the layers (e.g. Cadwell et al., 2020; Campagnola et al., 2022; Jiang et al., 2015).

Obtaining a comprehensive understanding of the relationship between anatomy and function requires a thorough characterization of neuronal stimulus selectivity or tuning. The selectivity of neurons in monkey and cat V1 for simple visual features, such as orientation, phase, or spatial frequency (Issa et al., 2000; Victor et al., 1994), enables the characterization of these neurons’ tuning properties using well-defined parametric stimuli like gratings. This has greatly facilitated the identification of general organizing principles of neuronal function in early visual areas of the cortical hierarchy (e.g. Ohki & Reid, 2014). However, neurons in higher visual areas prefer more complex visual features found in natural scenes, such as shapes, textures, objects, and faces (e.g. Bashivan et al., 2019; Kim et al., 2019a; Tang et al., 2020; Tsao et al., 2003), which are not easily described using parametric stimuli. The immense diversity and high dimensionality of the natural image space make it challenging to systematically characterize more complex visual function and link it to an organizing structure. Therefore it remains unknown whether neuronal tuning to complex spatial patterns like shapes and textures in higher visual areas, such as in area V4...
in the macaque visual cortex (Bashivan et al., 2019; Gallant et al., 1993; Kim et al., 2019a; Pasupathy & Connor, 2002; Tang et al., 2020), is also organized topologically across cortical layers, and whether cortical columns represent a universal principle reflecting the organization of the primate cortex. Addressing this question requires a flexible method to comprehensively characterize neuronal function without making strong assumptions about the underlying neuronal tuning model.

Advancements in deep learning promise to overcome these challenges. Specifically, recent deep learning functional models of the brain can accurately predict responses to arbitrary stimuli (Bashivan et al., 2019; Cadena et al., 2019, 2022), enabling essentially unlimited in silico experiments including ones that are virtually impossible in the real brain. This can be used for a comprehensive characterization of neuronal tuning function, such as identifying the neurons’ optimal stimuli (Bashivan et al., 2019; Franke et al., 2022; Höfling et al., 2022; Walker et al., 2019), map their invariances (Ding et al., 2023b), characterize contextual modulation (Fu et al., 2023) or characterize how multiple distinct tuning properties or nonlinear contextual effects relate to each other (Ustyuzhaninov et al., 2022). The predictions derived from these in silico analyses can then be verified through in vivo closed-loop experiments, known as inclusion loops, which have been successfully applied to single neurons in mice (Ding et al., 2023b; Franke et al., 2022; Fu et al., 2023; Höfling et al., 2022; Walker et al., 2019) and populations of neurons in macaque visual cortex (Bashivan et al., 2019).

In this study, we adapted the inception loop paradigm for macaque electrophysiological single-unit recordings to systematically map stimulus selectivity and analyze the structure-function organization for neurons in visual area V4. We used deep neural networks to build an accurate model of >1,200 recorded V4 neurons, capable of predicting responses to arbitrary images and used it to synthesize the most exciting image (MEI) for individual neurons, which we subsequently verified in vivo. We found that neurons recorded on the same silicon probe orthogonal to the cortical surface appeared to have similar spatial features compared to MEIs of neurons recorded across silicon probes inserted in different locations, and verified this impression with human psychophysics and a non-linear embedding space based on image similarity. Furthermore, the MEIs formed isolated clusters in the non-linear embedding space, indicating that V4 neurons separate into distinct functional groups that are selective for specific complex visual features such as eye-like structures, oriented fur patterns, grid-like motifs, or curvatures. Interestingly, these functional groups closely resemble the feature maps of early- to mid-level units in deep neural networks trained on image classification (Olah et al., 2020), suggesting that computational principles are shared among biological and artificial visual systems. Our findings provide evidence that functional cortical columns may be a generalizable canonical organizing principle in the cortex also beyond primary sensory areas like V1 and S1.

Results

Deep neural network approach captures tuning properties of individual monkey V4 neurons To systematically study the neuronal tuning properties of monkey V4 neurons in the context of natural scenes, we combined large-scale neuronal recordings with deep neural network modeling. To this end, we presented natural images to awake, head-fixed macaque monkeys and monitored the spiking population activity of V4 neurons using acute electrophysiological recordings with 32-channel linear arrays spanning 1,920 µm in depth, covering the majority of the 2 mm cortical depth (Fig. 1a; Denfield et al., 2018). In each recording session, we displayed 9,000–12,075 gray-scale images from the ImageNet database (Deng et al., 2009) organized in a trial structure, where each trial consisted of 15 images, each presented for 120 ms, followed by a gray screen 1,200 ms inter-trial period. During image presentation, the monkey was trained to maintain fixation on a fixation spot offset from the center of the monitor (Fig. 1a). The spot’s exact location was selected prior to each recording session such that the neurons’ population receptive field (RF), determined by using a sparse random dot stimulus, was centered on the monitor. Post-hoc spike sorting of the neuronal activity recorded across 100 sessions from two monkeys isolated the single-unit visual activity of 1,224 individual V4 neurons (Fig. 1c), resulting in a large dataset of well-isolated single-unit activity in monkey V4.

To predict the responses of the recorded neurons and characterize the neurons’ tuning properties, we used a deep convolutional neural network (CNN) model (Fig. 1b). Based on previous work in monkey (Bashivan et al., 2019; Cadena et al., 2019, 2022), we used a pre-trained goal-directed neural network as a non-linear feature space shared across all neurons and fitted only a simple linear-nonlinear neuron-specific readout (Lurz et al., 2020). Specifically, we chose a robust and high-performing ResNet-50 (Salman et al., 2020) as goal-directed neural network, trained on an image classification task. We selected one of its intermediate layers (layer 3.0) as non-linear feature space because it resulted in the best response predictions of the recorded V4 neurons. This yielded a correlation between response predictions and mean neuronal responses across repetitions of 0.43 (Fig. 1d). Together, these results show that our modeling approach accurately captures tuning properties of monkey V4 neurons in the context of naturalistic scenes. Treating our CNN model as a functional digital twin of the population of V4 neurons, we synthesized maximally exciting images (MEIs) (Bashivan et al., 2019; Walker et al., 2019) for individual V4 neurons in silico (Fig. 1e). To this end, we optimized a contrast-constrained image to produce the highest activation in the model neuron using regularized gradient ascent. The resulting MEI corresponds to the optimal stimulus of a neuron according to the model, depicting the peak of its tuning curve. We found
that MEIs strongly differ across neurons, indicating selectivity for distinct stimulus features like texture, curvature and edges (Fig. 1f), which resemble the features found in the MEIs of V4 multi-unit activity (Bashivan et al., 2019).

Our MEIs were also consistent with tuning properties of macaque V4, such as shape, curvature, and texture selectivity, previously identified using parametric stimuli (Kim et al., 2019b; Pasupathy & Connor, 2001; Pasupathy et al., 2020). However, in contrast to these previous studies, our data-driven approach uncovers tuning properties of single V4 neurons without making any parametric assumptions about the neurons’ stimulus selectivity or the need for pre-selecting an ensemble of visual stimuli.

Closed-loop paradigm verifies model-derived optimal stimuli of single V4 neurons To demonstrate the model’s accuracy and that the computed MEIs indeed strongly drive the recorded neurons, we developed a closed-loop paradigm for acute electrophysiological recordings of single neurons (Fig. 2a). Specifically, after fitting the readout for single-unit responses recorded in a “generation” session where natural images were shown, we selected the best six units based on model prediction for in vivo verification, generated their MEIs and presented them back to the animal on the same day while recording from the same neurons in a “verification” session. Single units were matched across the generation and verification session using spike waveform similarity and functional consistency of responses to the same natural images (Suppl. Fig. 1). As a control stimulus for each selected unit, we presented the seven most exciting natural image crops identified by the model by screening 5,000 natural images not used during model training. Each crop was matched to the size, position, and contrast of the MEI of a particular neuron. These control stimuli perceptually resembled the MEI (Fig. 2b), demonstrating that visual features of modelsynthesized MEIs are representative for elements of natural scenes.

Overall, our model faithfully predicted responses of V4 neurons to full-field natural images and synthesized stimuli, and reliably synthesized strongly exciting images. Despite the high structural similarity of MEI and control images, the MEI consistently elicited higher neuronal responses than the control images, as well as MEIs and control images of other neurons (Fig. 2c,d,f), suggesting that it indeed corresponds to the neuron’s optimal stimulus. In
Fig. 2. Closed-loop paradigm verifies model-derived optimal stimuli of single V4 neurons a, Schematic illustrating closed-loop experimental paradigm for acute recordings in monkey V4. In brief, after recording and spike sorting of the “generation session”, we train a model, select neurons for experimental confirmation, generate MEIs and identify exciting natural image control stimuli, and present both MEIs and controls back to the animal while recording from the same neurons in the “verification session”. Functional and waveform matching of units across recordings is performed offline. b, MEI and the seven most exciting natural image crops, selected from 50k natural images, for four example neurons. Natural images were matched in size, location and contrast to the MEI. c, Peak-normalized recorded responses of the neurons in (b) to their MEI (orange) and control images (black; mean across n=20 repeats). d, Recorded versus predicted neuronal activity of two example neurons to their MEI and control stimuli, as well as to MEIs and control stimuli of other neurons. e, Scatter plot of model performance on the test set of natural images and the closed-loop stimuli (as shown in d, but for all neurons). Correlation to average: mean ± s.d. = 0.61 ± 0.11; Synthesized and selected stimuli: mean ± s.d. = 0.61 ± 0.20, n = 55 neurons. A paired t-test showed no significant difference \( p = 0.89 \). f, Distribution of peak-normalized mean responses to each neuron’s MEI and control stimuli, as well as MEIs and control stimuli of other neurons for all closed-loop neurons (n = 55 neurons, n = 24 sessions, n = 1 monkey). P-values for a paired t-test are: MEI-Control, 3.22e-08; MEI-OtherMEIs, 2.57e-14; MEI-OtherControls, 3.06e-19; Control-OtherMEIs, 2.86e-07; Control-OtherControls, 1.62e-19; OtherMEIs-OtherControls, 2.99e-05. P-values were corrected for multiple comparisons with Bonferroni correction.

addition, the model accurately predicted the closed-loop neurons’ average responses to their own MEIs, to control stimuli, and to the MEIs and control stimuli of other neurons of the same session (two example neurons in Fig. 2d). The absolute scale of the firing rate predictions did not always perfectly match the recorded firing rate, likely due to slow drifts in overall firing rates of some neurons (e.g. Fig. 2d, right). Nevertheless, across neurons, the model trained on the generation session made accurate predictions for the verification session, with no significant difference in prediction performance between full-field natural images and synthesized MEIs (\( \rho = 0.61 \), Fig. 2e). Moreover, the amplitude of neuronal responses to control stimuli and MEIs of other neurons only slightly differed, suggesting that there is little difference between MEIs and contrast- and size-matched natural images (Fig. 2f).

Columnar organization of optimal stimuli in macaque V4

Studying how visual selectivity is organized in a particular brain area has revealed key principles of vision, including the pinwheel of orientation columns in primary visual cortex (Bonhoeffer & Grinvald, 1991). In monkey V4, neurons are tuned to more complex visual features like shape and texture (Kim et al., 2019b; Pasupathy & Connor, 2001; Pasupathy et al., 2020; Srinath et al., 2020), but it remains unclear whether V4 tuning properties are organized in a columnar manner (Ghose & Ts'o, 1997; Hatanaka et al., 2022; Tang et al., 2020). Therefore, we next asked whether our data-driven approach reveals an organizing principle of stimulus selectivity in V4.

We noticed that MEIs from individual sessions exhibited strong mutual perceptual similarity compared to MEIs from other sessions (Fig. 3a,b). While the range of preferred stimuli we found spanned a large variety from oriented and comb-like patterns, to grid-like motifs and patterns that resembled eye-like structures, the perceived variability within many sessions was much smaller than across sessions. For example, most neurons in one example session preferred oriented and comb-like patterns (Fig. 3a), while neurons from other example sessions preferred curved edges (session 2 in Fig. 3b) and grid-like patterns (session 3 in Fig. 3b).

To quantify the perceptual similarity of MEIs within a session, we performed a simple psychophysics experiment, where human observers were presented with two sets of MEIs: (1) a selection of nine neurons recorded within one
session and (2) a set of nine neurons randomly sampled across sessions. The two sets were presented side-by-side (as shown in Fig. 3c, but without the colored frames), with each set being shown on the left or right at random. The observers then had to report in a two-alternative forced-choice paradigm which set of MEIs looked more consistent (i.e., shared the same image features). The experiment included \( n=50 \) trials/sessions. Distribution of fraction of sessions correctly identified among subjects, \( = 0.73 \); subject-variability in s.d., \( = 0.13 \); session-variability in s.d., \( = 0.21 \).

The resulting embedding space placed neurons with similar MEIs close to each other (neurons 1 and 3 in Fig. 4b) and neurons with different MEI features far away (neurons 1 and 2). Similarly, multiple MEIs of the same neuron, generated by starting from different initial noise images during optimization, were placed nearby in the embedding space as well (groups of the same color in Fig. 4b and Fig. 4c,d). These observations suggest that the model indeed learned to embed MEIs based on image similarity.

We next quantified whether neurons recorded within one session share tuning properties as suggested by the observed MEI similarity within sessions (cf. Fig. 3). To this end, we computed the mean pairwise distance in the embedding space across neurons from one session and compared it to a null distribution of distances obtained by computing the mean pairwise distance across randomly picked neurons from different sessions (Fig. 4c,e). While the within-session distance varied across sessions (Fig. 4f), on a population level, it was significantly smaller than the across-session distance (Fig. 4g). The percentage of sessions that showed a significantly smaller distance in MEI similarity than the null distribution increased with higher numbers of neurons recorded per session and
with higher prediction performance of the model (Fig. 4h). For more than 12 neurons per session and with the highest performance threshold (correlation to average >0.4), half of the sessions displayed a significantly smaller within- than across-session distance, indicative for high similarity of MEIs. Importantly, the within-session distances estimated based on the embedding space significantly correlated with the observer agreement (percent correct) of the psychophysics experiment ($\rho = -0.32, p=0.025$), suggesting that MEI distance in the embedding space is informative about MEI perceptual similarity. We additionally confirmed that MEIs of neurons recorded within one session are more similar to each other than to MEIs of neurons recorded in other sessions using an independent similarity metric, namely the representational similarity of MEIs in neuronal response space, which closely mimics perceptual similarity (Kriegeskorte, 2008) (Suppl. Fig. 3). Taken together, the above analyses strongly suggest that neuronal tuning properties of monkey V4 neurons are organized in a columnar structure, with neurons sharing the same tuning aligned within a vertical column.

V4 neurons cluster into distinct functional groups that resemble feature maps of artificial vision systems. At the level of retinal ganglion cells, neurons cluster into specific functional groups or output channels (Baden et al., 2016; Goetz et al., 2022). Whether a similar functional clustering persists for cortical neurons is still an open question. For instance, in V1 it is not clear whether the distinction be-
tween simple and complex cells represents two ends of a continuous spectrum or two discrete categories (Mechler & Ringach, 2002). Previous results in mouse primary visual cortex suggest that neurons cluster according to function, but not in an entirely discrete manner (Ustyuzhaninov et al., 2019). Motivated by the structure of the MEI embedding space that exhibited isolated “islands” of MEIs (cf. Fig. 4b), we asked whether tuning properties of V4 neurons fell into similar functional groups, characterized by their preferred stimulus. To address that question, we clustered the two-dimensional embedding vectors of the MEIs using hierarchical clustering (DBSCAN; McInnes et al., 2017), resulting in 17 different functional groups (Fig. 5). Different MEIs within the same group showed high perceptual similarity and exhibited similar stimulus preferences, such as for eye-like structures in group 11. In contrast, neurons assigned to different groups substantially differed with respect to their preferred visual feature, especially for groups located on opposite sides of the embedding space. For example, while MEIs in group 11 were characterized by eye-like structure, MEIs of group 3 and 8 displayed grid-like and comb-like patterns, respectively.

To ensure that the group structure in the embedding space is not an artifact of the contrastive neighborhood embedding method, we additionally used an independent method to compare within-group to across-group similarities. To that end, we computed the representational similarity of the MEIs using the predicted neuronal responses from our model. Specifically, we centered the receptive fields of all neurons in the model and compared the similarity of two MEIs via the cosine of the predicted population response vectors. Importantly, this similarity metric is unrelated to the embedding space used for clustering and, therefore, provides an independent verification of the identified functional groups. We found that MEIs of neurons assigned to the same group were significantly closer to each other in the neuronal response space than MEIs of neurons assigned to different groups (Suppl. Fig. 3): The within-group similarity in neuronal response space was significantly higher than the across-group similarity for all of the 17 functional groups.

Interestingly, the MEIs of the functional groups of monkey V4 neurons we identified closely resemble feature visualizations of single units found in modern deep neural networks trained on image recognition. For example, a similar preference for specific complex features can be found in the early layers, specifically layer mixed3a, of the InceptionV1 deep network (Olah et al., 2020; Szegedy et al., 2015). This alignment between V4 and deep network features is in line with previous results that found boundary selective units in the AlexNet deep network (Krizhevsky et al., 2012; Pospisil et al., 2018), similar to boundary neurons in monkey V4 (Pasupathy & Connor, 2002). Olah et al. (2020) manually grouped the feature visualizations into different categories like “Oriented fur,” “Eyes/circles/loops” and “Divots/boundaries” (Fig. 5b). These categories are perceptually very similar to the functional groups of V4 neurons we identified using hierarchical clustering, suggesting that there are general encoding principles that are shared among the primate visual system and artificial vision system. The resemblance between V4 neuronal and deep artificial neural network feature selectivity can be used to generate specific hypotheses about visual tuning properties of primate V4 neurons beyond spatial patterns. For example, as the artificial vision systems were trained on color images, the resulting feature visualizations also characterize model units’ color tuning and can be used to derive predictions about color boundary encoding in monkey V4 functional groups (Fig. 5c), which could subsequently be verified in in vivo experiments.

**Discussion**

Our work provides evidence for a columnar organization of tuning to spatial patterns in visual area V4, based on detailed single neuron tuning properties. This finding was enabled by employing an iterative image synthesis method based on a deep neural network model of neuronal activity. This digital twin of V4 facilitated a characterization of spatial pattern tuning that was not biased by any prior parametric assumption about the type of selectivity, and identified preferred stimuli (MEIs) that evoked stronger responses than competitive natural stimuli selected from a large set of previously unseen images. By learning a non-linear image similarity embedding space and using human psychophysics, we demonstrated that the MEIs from a single recording penetration perpendicular to the cortical surface were more similar to each other than from a random selection of neurons, and that the MEIs of neurons in V4 clustered into separate functional groups. Our findings suggest that, despite the complex stimulus preferences of V4 neurons, their preferred selectivity is organized in a columnar manner.

**Are our MEIs consistent with previous findings?** The idea to use neuronal encoding models to synthesize optimal stimuli for the brain is not new (Lehky et al., 1992) and has already successfully been used in mouse primary visual cortex (Franke et al., 2022; Walker et al., 2019), mouse retina (Höfling et al., 2022), and also macaque V4 (Bashivan et al., 2019). Many of our MEIs display features, such as different types of textures, that qualitatively resembled those found by Bashivan et al. (2019). However, some of our MEIs exhibited shape-like features, including curved strokes, corners, and even higher-level attributes such as individual eye-like stimuli (cluster 7 in Fig. 5a), which have not been reported before. One distinction between our study and that of Bashivan et al. (2019) is that we used silicon probes, enabling us to separate spikes from individual neurons, while they employed chronically implanted Utah arrays and optimized stimuli for single “sites” (multi-units) that likely comprise a mix of multiple neurons. Consequently, it remains unclear from their study whether the complexity of the MEIs stems
Fig. 5. V4 neurons cluster into distinct response modes that resemble feature maps of artificial vision systems. a, Position of all highly activating MEIs (n=19,688) of n=889 neurons in the 2D MEI similarity space, color coded based on cluster assignment obtained from the hierarchical clustering algorithm HDBSCAN. For n=12 clusters, we show a random selection of MEIs of different neurons assigned to this cluster. For examples of the other clusters, see Suppl. Fig. 4 and for independent verification of the clusters, see Suppl. Fig. 3. Light gray dots indicate MEIs that could not be assigned to any of the clusters with high probability.

b, Feature visualizations of early- to mid-level units in the deep neural network InceptionV1 trained in an image classification task (Olah et al., 2020). Units are grouped into distinct categories based on (Olah et al., 2020), with clusters from (a) resembling these categories indicated below.

c, Example units of the neural network trained on image classification compared with example MEIs exhibiting similar spatial patterns. The resemblance between the two can be used to generate hypotheses, such as to predict color boundary encoding in primate V4 neurons, that can be subsequently tested experimentally.
from the mixing of spikes from multiple neurons or if single neurons already prefer such intricate spatial patterns as displayed by the MEIs. Additionally, MEIs for multi-unit activity could average out specific features like shapes. Our results provide experimentally validated evidence that the complexity of MEIs is already present at the level of single neurons in macaque V4.

Our MEIs are also consistent with previously described tuning properties of V4 neurons. V4 is part of the ventral pathway which plays a major role in object and shape recognition (Felleman & Van Essen, 1991; Mishkin et al., 1983). Previously, V4 cells have been reported to be selective to complex shapes (Kobatake & Tanaka, 1994), and to be tuned to convex and concave shapes of object boundaries at specific locations in the visual field (Gallant et al., 1993; Pasupathy & Connor, 2001). In addition to shape, V4 neurons are also known to be selective to texture (Kobatake & Tanaka, 1994). Kim et al. (2019a) found that tuning of single V4 neurons can be placed along a continuum from strong tuning for boundary curvature of shapes to strong tuning for perceptual dimensions of texture. From visual inspection, our MEIs reproduce these tuning properties. On the one hand, we find MEIs that clearly exhibit curvature elements (e.g. cluster 7 in Fig. 5a) or ‘eye’-like elements (cluster 1). On the other hand, many MEIs have a texture component such as ‘fur’ (cluster 8), dots (cluster 11), or grid-like elements (cluster 6). Interestingly, generating multiple MEIs from different starting points – known as Diverse Exciting Images (DEIs; Cadena et al., 2018; Ding et al., 2023b) – resulted in multiple MEIs that had similar shape and texture features (Suppl. Fig. 2), indicating that single cells in V4 are neither texture- nor shape-invariant.

Together, our MEIs are consistent with previous results but paint a more detailed picture of the complex and diverse tuning properties of single cells in V4.

**Topological organization of MEIs in V4** One advantage of our recordings is that we can record simultaneously across layers using silicon probes. This enabled us to characterize the vertical organization of tuning selectivity to complex spatial patterns in area V4, and investigate evidence for a columnar organization. The presence of columns in V4 has been a matter of debate and controversy, predominantly studied in the domain of color (Kotake et al., 2009) or orientation (Ghose & Ts’o, 1997) because stimuli for these domains are more accessible to low dimensional parametrization. For instance, in the color domain, one study has reported weak columnar organization (Kotake et al., 2009), while another found no evidence (Tanaka et al., 1986). Beyond that, other studies using natural images or parametric stimuli for curvature found that neurons within a layer with similar tuning are locally clustered (Hatanaka et al., 2022; Tang et al., 2020). However, since these studies only focused on neurons from superficial layers, it remains unknown whether there is a columnar organization for these features that spans all cortical layers.

Moreover, it is well-established that V4 neurons exhibit selectivity for complex spatial features that extend beyond those characterized by parametric stimuli defined by orientation, or parameterized curvature (Tang et al., 2020). Consequently, in the absence of a detailed identification of the optimal stimuli, assessing the hypothesis of functional columns proves to be challenging. For example, if neurons are tuned to similar grid-like textures but with different orientations, using grating stimuli (Ghose & Ts’o, 1997) or predetermined parameterized curvature stimuli (Tang et al., 2020) will obscure the true underlying organization. Our deep learning based image synthesis method avoids these challenges by identifying most exciting stimuli in the high-dimensional pixel space.

To compare MEIs regardless of their spatial complexity, we used human psychophysics and deep learning techniques to assess the similarity between them, specifically employing contrastive learning to create a non-linear embedding based on similarity among MEIs (Böhm et al., 2023). We discovered that neurons across layers recorded in orthogonal penetrations to the cortical surface had MEIs that were perceptually more similar than those from randomly sampled neurons. However, the strength of the columnar effect varied and was not equally evident in all recording sessions. This variability in effect size could have been caused by several factors. First, despite best efforts, our electrode penetrations may not have been perfectly orthogonal to the cortical surface, because the electrodes were aligned relative to the recording chamber. The recording chamber was implanted such that its center was orthogonal to the surface of the cortex. Since the cortex is curved, penetrations further away from the center may not have been perfectly orthogonal to the cortical surface. The brain may also have moved or have been slightly compressed during insertion, potentially resulting in slightly angled penetrations. Second, if there is a topographical organization in V4, it may feature both homogeneous zones and regions with more mixed selectivity, analogous to pinwheels in orientation maps in V1. Thus, we expect a certain fraction of penetrations to be close to such heterogeneous zones. Because extracellular electrodes record the activity of neurons in a roughly cylindrical region around the electrode, we expect a fraction of penetrations to exhibit mixed tuning even if the penetrations were perfectly vertical. Estimating what fraction of penetrations should exhibit consistent tuning is difficult, because the size of the columns and the relationships between them are not yet understood. However, judging from our psychophysical results and the power analysis in Fig. 4h, we consider it likely that more than 50% of the penetrations actually contain a significant bias towards certain types of selectivity. To more accurately delineate and map the topological organization of spatial form tuning in V4, future studies need to combine recording techniques like two-photon functional imaging with deep learning and inception loop approaches.

**Similarity to tuning in deep networks** The MEIs for V4 neurons visually resemble MEIs of units in deep artifi-
cial neural networks trained on image recognition tasks. While there are differences between biological and artificial vision (reviewed in Sinz et al., 2019), deep networks trained on large-scale vision tasks are the closest human engineered system to biological visual system we know. Several previous works have found similarities between the primate visual system and deep network representations of visual stimuli (Güçlü & van Gerven, 2015; Khaligh-Razavi & Kriegeskorte, 2014; Yamins & DiCarlo, 2016; Yamins et al., 2014). On a single neuron level, previous work has pointed out similarities between tuning in early vision and selectivities of single units in deep networks (Krizhevsky et al., 2012; Olah et al., 2020; Zeiler & Fergus, 2014) and a recent investigation has shown that single units in deep networks can exhibit similar object boundary tuning as V4 neurons (Pospisil et al., 2018). The striking similarity between our single cell MEIs of V4 neurons and single units in the InceptionV1 architecture (Olah et al., 2020) provide an even stronger case for similarities in tuning in primate early vision and deep networks. What's more, by using this similarity we can derive predictions about the color selectivity of V4 neurons despite having shown only gray-scale images in the experiment and during model training (Fig. 5b).

Future directions Our research highlights the power of applying deep learning to comprehensively characterize neuronal representations and helping to elucidate the relations of structure and function of the brain. The concept of cortical columns is an attractive model of the cortex, as it breaks down cortical computation into smaller building blocks of information processing. Our results support the hypothesis that distinct functional groups of neurons organized into cortical columns are not only a feature of primary sensory areas like V1 and S1, but also midlevel visual cortical area V4. Given that neuronal connections within a cortical area tend to be locally dense Gilbert & Wiesel (1989), there's a significantly higher likelihood of connection between neighboring neurons within a column, both within and across layers. Therefore, the purpose of a columnar architecture is not to set precise spatial boundaries between neurons. Instead, it serves to enhance synaptic opportunities between neurons that share similar response properties, facilitating circuit computations such as the development of new types of invariances or the creation of more complex feature selectivity. In this study, our primary focus was on MEIs, with an emphasis on the tuning similarities among neurons recorded from the same probe. However, it is crucial to emphasize that MEIs merely represent the tip of the iceberg. To decipher columnar computations, we need to characterize the full tuning function, including neuronal invariances, as well as examine the differences between neurons within a column. These differences may include variations in their invariances and distinctions in the aspects of the features they encode, which would be consistent with an increasing complexity of feature selectivity across layers. Such future studies will shed light on the transformations occurring within columns and ultimately, when combined with synaptic resolution connectomics, will reveal the underlying mechanisms by which neurons interact to compute Bock et al. (2011); Consortium et al. (2021); Ding et al. (2023a); Reid (2012).

Acknowledgements The authors thank the International Max Planck Research School for Intelligent Systems (IMPRS-IS) for supporting Konstantin Wilke and Arne Nix. The authors would also like to thank Jan Niklas Böhm, Philipp Berens, and Dmitry Kobak for their guidance with using their recently developed t-simCNE model. The authors also thank Edgar Y. Walker, George Denfield, Christoph Blessing, Mohammad Bashiri, Konstantin Klémens Luz, Max Bung, Sanghian Ma, Robert Petrovic, Elena Offenberg and Paul Fahey for technical support and helpful discussions. The research was funded by the Carls-Zeiss-Stiftung (KW, FHS), the Cyber Valley Research Fund (AN, FHS). FHS is further supported by the German Federal Ministry of Education and Research (BMBF) via Collaborative Research Center in Computational Neuroscience (CRCNS) (FKZ 01GQ2107) as well as the Collaborative Research Center (SFB 1233, Robust Vision) and the Cluster of Excellence “Machine Learning – New Perspectives for Science” (EXC 2064/1, project number 390727645). ASEE received funding for this project from the European Research Council (ERC) under the European Union’s Horizon Europe research and innovation programme (Grant agreement No. 101041669) and Deutsche Forschungsgemeinschaft (DFG, German Research Foundation), project ID 432683000 (SFB 1456, project 305). The work was also supported by the Intelligence Advanced Research Projects Activity (IARPA) via Department of Interior/Interior Business Center (DoI/IBC) contract numbers D16PC00003, D16PC00004, and D16PC0005. The U.S. Government is authorized to reproduce and distribute reprints for Government purposes notwithstanding any copyright annotation thereon. We also acknowledge support from the National Institute of Mental Health and National Institute of Neurological Disorders And Stroke under Award Number U19MH114830 and National Eye Institute award numbers R01 EY026827 and Core Grant for Vision Research R32-EY022520-37 as well as the National Science Foundation Collaborative Research in Computational Neuroscience IIS-2113173. Disclaimer: The views and conclusions contained herein are those of the authors and should not be interpreted as necessarily representing the official policies or endorsements, either expressed or implied, of IARPA, DoI/IBC, or the U.S. Government.

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AUTHOR CONTRIBUTIONS

KFW Conceptualization, Methodology, Validation, Software, Formal Analysis, Investigation, Writing - Original Draft, Visualization Conceptualization, Methodology, Validation, Software, Formal Analysis, Investigation, Experimental and analysis design, Writing - Original Draft, Writing - Review & Editing, Supervision; SAC Conceptualization, Methodology, Software; TS, CN, GR, SP Data acquisition, Data curation, Methodology; ASE Conceptualization, Methodology, Investigation, Experimental and analysis design, Writing - Review & Editing, Supervision; ANF Methodology, Software, Writing - Review & Editing; RFS Conceptualization, Methodology, Investigation, Experimental and analysis design, Writing - Original Draft, Writing - Review & Editing, Supervision, Funding Acquisition, Project administration; AST Conceptualization, Methodology, Investigation, Experimental and analysis design, Writing - Original Draft, Writing - Review & Editing, Supervision, Funding Acquisition, Project administration; AT Conceptualization, Methodology, Investigation, Experimental and analysis design, Writing - Original Draft, Writing - Review & Editing, Supervision, Funding Acquisition, Project administration; Administration, Project administration;

Materials and Methods

Ethics statement Electrophysiological data were gathered from a pair of healthy male rhesus macaque monkeys (Macaca mulatta), aged 17 and 19 years, and weighing 16.4 and 10.5 kg, respectively, at the time of the study. The research adhered to NIH guidelines and received approval from the Institutional Animal Care and Use Committee at Baylor College of Medicine (permit number: AN-4367). The experiments were conducted under protocols and guidelines approved by the Institutional Animal Care and Use Committee at Baylor College of Medicine ensuring that the monkeys received regular veterinary check-ups, balanced nutrition, and environmental enrichment. Surgical procedures involving the monkeys were performed using general anesthesia and adhering to standard aseptic techniques. Postoperative pain was managed with analgesics for seven days.

Electrophysiological recordings Non-chronic recordings were conducted using a 32-channel linear silicon probe (NeuroNexus V1x32-Edge-10mm-60-177), with surgical methods and recording protocols previously outlined (Denfield et al., 2018). In summary, custom titanium recording chambers and head posts were implanted under complete anesthesia and sterile conditions. Initially, the bone remained unaltered, and only before recordings were small trephinations (2 mm) made over lateral V4, with eccentricities spanning from 1.7 to 18.3 degrees of visual angle. Recordings took place after a week of each trephination. A Narishige Microdrive (MO-97) and guide tube were used to carefully lower the probes, penetrating the dura.

Data acquisition and spike sorting Electrophysiological data were continuously collected as a broadband signal (0.5Hz—16kHz), digitized at 24 bits. The spike sorting methods employed in this study resemble those used in (Cadena et al., 2019; Denfield et al., 2018), with the code accessible at https://github.com/aecker/moksm. The linear array of 32 channels was divided into 14 groups, each containing six neighboring channels (with a stride of two), which were treated as virtual electrodes for spike detection and sorting. Spikes were identified when channel signals exceeded a threshold equal to five times the standard deviation of the noise. Following spike alignment, the first three principal components of each channel were extracted, resulting in an 18-dimensional feature space utilized for spike sorting. A Kalman filter mixture model was fitted to monitor waveform drift, which is common in non-chronic recordings (Calabrese & Paninski, 2011; Shan et al., 2017). Each cluster’s shape was modeled using a multivariate t-distribution (degrees of freedom = 5) with a ridge-regularized covariance matrix. The cluster count was determined based on a penalized average likelihood with a constant cost for each additional cluster (Ecker et al., 2014).

Lastly, a custom graphical user interface was used to manually confirm single-unit isolation by evaluating the units’ stability (based on drifts and cell health throughout the session), identifying a refractory period, and inspecting scatter plots of channel principal component pairs.

Visual stimulation and eye tracking Visual stimuli were generated by a specialized graphics workstation and presented on a 16:9 HD widescreen LCD monitor (23.8”) with a 100 Hz refresh rate and a resolution of 1920 × 1080 pixels, positioned at a 100 cm viewing distance (yielding approximately ∼ 63 pix/°). The monitor underwent gamma correction to ensure a linear luminance response profile. A custom-made, camera-based eye tracking system confirmed that monkeys kept their gaze within roughly ∼ 0.95° around a ∼ 0.15°-sized red fixation target. Offline evaluations revealed that the monkeys typically fixated with greater accuracy.

Upon maintaining fixation for 300 ms, a visual stimulus was displayed. If the monkeys sustained their gaze throughout the entire trial duration (1.8 s), they were rewarded with a...
Receptive field mapping and stimulus placing At the start of each session, we determined receptive fields in relation to a fixation target using a sparse random dot stimulus. A solitary dot, spanning $1^\circ$ of the visual field, was displayed on a uniform gray background, with its location and polarity (black or white) randomly changing every 30 ms. Each fixation trial persisted for two seconds. Multi-unit receptive field profiles for each channel were obtained through reverse correlation. The population receptive field was as close to the screen’s center as feasible. Due to the recording sites’ location in both monkeys, this positioning involved placing the fixation spot near the screen’s upper border, shifted to the left.

Natural image stimuli We selected a collection of 24,075 images from 964 categories ($\sim$ 25 images per category) from ImageNet (Deng et al., 2009), transformed them to grayscale, and cropped the central $420 \times 420$ pixels. For images that were smaller than $420 \times 420$, a central crop was taken and the resulting image was re-scaled to $420 \times 420$. Each image had an 8-bit intensity resolution (values ranging from 0 to 255). From this set, we randomly chose 75 images as our test-set. Out of the remaining 24,000 images, we designated 20% as validation-set at random, leaving 19,200 images in the train-set. Natural images were displayed during the standalone generation recordings of 1,244 units and during the generation phase of closed-loop recordings for 82 units. Specifically, $\sim 12k$ unique train-set images were displayed during the standalone generation recordings, and $\sim 7.5k$ unique train-set images were displayed during the generation phase of closed-loop recordings. Across sessions, train images were randomly sampled from the train-set such that the full set was exhausted before cycling back through the same images. The 75 test-set images were displayed in every recording session. Note that selecting images from ImageNet means that the pre-trained convolutional network (see below) has likely seen our natural stimuli (but not the neuronal responses) during training on the classification task. During standalone generation recording sessions, $\sim 1000$ successful trials ($\sim 12k$ train images and 75 repeated test images) were recorded, whereas 600 successful trials ($\sim 7.5k$ train images and 75 repeated test images) were recorded during the generation phase of closed-loop experiments. In both instances, each trial involved continuous fixation for 2.4 seconds, which includes 300 ms of a gray screen (intensity 128) at the beginning and end of the trial, as well as 15 consecutive images displayed for 120 ms each without any gaps. Trials contained either training/validation images that were presented only once or test images, which were repeated during the experiment. Throughout the recording session, all trails were randomly interleaved, with test images being repeated 40-50 times during standalone generation recordings and 20 times during the generation phase of closed-loop recordings. Training and validation images were sampled without replacement, so each image was effectively displayed once or not at all. Images were upsampled using bicubic interpolation to match the screen width (1920 pixels) while maintaining their aspect ratio. The upper and lower 420-pixel bands were cropped out to cover the entire screen, effectively stimulating both classical and beyond classical receptive fields of V4 neurons. After sorting the neurons, spikes associated with each image presentation were counted within a 70-160 ms time window after stimulus onset.

Image preprocessing for model training Starting out from an original image size of $420 \times 420$ with a resolution of $1\text{px}/^\circ$ we cropped the upper and lower bands to fit the full screen for presentation for a resulting image size of $420 \times 236$. We then cropped the images so that only the bottom center $200 \times 200$ pixels remained. Then, we down-sampled the images to either $80 \times 80$ or $100 \times 100$ pixels ($5.8px/^\circ$ or $7px/^\circ$), for the closed-loop model training and non-closed-loop model training, respectively.

Model architecture Our neural predictive model of primate V4 consisted of two main parts: A pretrained core that computes nonlinear features of input images, and a Gaussian readout (Lurz et al., 2020) that maps these features to the neuronal responses of the single neurons. As the core of our model, we used a ResNet50 (He et al., 2016) which was adversarially trained on ImageNet (Deng et al., 2009) to have robust visual representations (Salman et al., 2020), which yields improved transfer-learning performance (Engstrom et al., 2019a,b; Madry et al., 2017). Interestingly, it has been previously shown that robust features not only allow for better transfer-learning but they appear to be more similar to biological networks and also improve neural predictivity (Feather et al., 2022; Guo et al., 2022; Li et al., 2019; Safarani et al., 2021). Building on previous work (Cadena et al., 2022), we selected the first residual block of layer 3 of the ResNet, layer3.0, to read out from, and found that the adversarially robust training with $\epsilon = 0.1$ yielded the highest predictive performance, compared to all other ResNet models and layers. The corresponding size of the output feature map at layer layer3.0 was 1024.

The input images $x$ were forwarded through all layers up to a selected layer, to output a tensor of feature maps. Importantly, the parameters of the pretrained network were always kept fixed. We then applied batch-normalization (Ioffe & Szegedy, 2015). Lastly, we rectified the resulting tensor with a ReLU unit to obtain the final nonlinear feature space $\Phi(x) \in \mathbb{R}^{w \times h \times c}$ (width, height, channels) shared by all neurons.

To predict the response of a single neuron from the $\Phi(x) \in \mathbb{R}^{w \times h \times c}$ we use a Gaussian readout (Lurz et al., 2020).
For each neuron \( n \), this readout learns the coordinates \((x^{(n)}, y^{(n)})\) of the position of the receptive field on the output tensor and extracts a feature vector \( \Phi_{x^{(n)}, y^{(n)}} \in \mathbb{R}^c \) at this location from \( \Phi \). To this end, the Gaussian readout learns the parameters of a 2D Gaussian distribution \( \mathcal{N}(\mu_n, \Sigma_n) \) and samples a location in feature space \( \Phi(x) \) during each training step for every neuron \( n \). \( \Sigma_n \) is initialized large enough to ensure that the entire visual field can be covered, and then decreases in size during training to have a more reliable estimate of the mean location \( \mu_n \). At inference time (i.e. when evaluating our model), the readout is deterministic and uses the fixed position \( \mu_n \). Although this framework allows for rotated and elongated Gaussian functions, we found that for our data, an isotropic \( \sigma_n^2 \) was performing equally well as compared to a fully parametrized Gaussian. Taken together, together, number of parameters per neuron of the readout were \( c + 4 \) (number of channels, bivariate mean, variance, and bias). This extracted feature vector \( \Phi_{x^{(n)}, y^{(n)}} \), is then used in a linear-nonlinear model to predict the neuronal response. To this end, an affine function of the resulting feature vector at the chosen location was computed, followed by a rectifying nonlinearity \( f \), chosen to be an ELU (Clevert et al., 2015) offset by one (ELU + 1) to make responses positive (Eq. 1). The weight vector \( w_n \in \mathbb{R}^c \) was \( L_1 \) regularized during training.

\[
\hat{r}_n(x) = f \left( \sum_k \Phi_{x^{(n)}, y^{(n)}}(x) \cdot w_{n,k} + b_n \right) \tag{1}
\]

**Model training** We trained our model to minimize the summed Poisson loss across \( N \) neurons between observed spike counts \( r \) and the models’ predicted spike counts \( \hat{r} \) in addition to the \( L_1 \) regularization of the readout parameters.

\[
\mathcal{L} = \sum_{i=1}^{N} (\hat{r}_n - r_n \log \hat{r}_n) + \lambda \sum_{n,k} |w_{n,k}| \tag{2}
\]

We trained the models either on the full dataset of \( n=100 \) recording sessions with \( n=1244 \) neurons and an image size of 100 by 100 pixels, or on an individual sessions during a closed loop recording with a reduced image size of 80 by 80 pixels in order to save time with model training and stimulus generation. For training on the full dataset, an epoch consisted of the cycling through the whole training set of 19200 images. However, because only \( \approx 9,000 \) - 13,000 images were shown in each session, if a particular image was not shown in a session, we simply zeroed out the gradients of all neurons in the sessions that did not contain the image in question. When training models on a single closed loop recording, we cycled through all \( \approx 9,000 \) training images that were shown in that session. In all cases, we used a batch size of 64 and after each batch, we updated the weights using the Adam optimizer (Kingma & Ba, 2014). The initial learning rate was \( 3 \cdot 10^{-4} \) with a momentum of 0.1.

After each epoch, we computed the Poisson loss on the entire validation set. Similar to the training set, not all images were shown in all sessions, so that we again zeroed out the loss for the sessions in question. We then used early stopping to decide whether to decay the learning rate or stop the training altogether. We scaled the learning rate by a factor of 0.3 once the validation loss did not improve for five consecutive epochs. Before decaying the learning rate, we restored the weights to the best ones based on the poisson loss on the validation set. After four early stopping steps were completed, we stopped the training. On average, this resulted in \( \approx 50 \) training epochs, for a training time of 2 minutes for a closed loop session, and 15 minutes for the entire dataset on a NVIDIA 2080ti GPU.

**Ensemble models.** Instead of using a single trained model, we used a model ensemble for all of our analyses and for MEI generation. To predict the neuronal responses to individual images, we trained readout weights for each member of an ensemble of five models initialized with different random seeds and used the average prediction across the ensemble for further analyses (Hansen & Salamon, 1990). We always trained ten individual models with a different random seed, which determined the model initialization as well as the drawing of training batches. Then, we selected the five models with the highest performance on the validation set to form a model ensemble. The inputs to the ensemble model were passed to each member, and the resulting predictions were averaged to obtain the final model prediction.

**Explainable variance** As a measure of response reliability, we estimated the fraction of the stimulus-driven variability as compared to the overall response variability. More specifically, we computed the ratio between each neurons’ total variance minus the variance of the observation noise, over the total variance (Eq. 3). To estimate the variance of the observation noise, we averaged the variance of responses across image repeats for all of the 75 repeated full-field natural image test stimuli \( \sigma^2_{\text{noise}} = \mathbb{E}_j[\text{Var}[r_i|x_j]] \) where \( i \) corresponds to the repeats and \( x_j \) represents a unique image:

\[
\text{EV} = \frac{\mathbb{V}[r] - \sigma^2_{\text{noise}}}{\mathbb{V}[r]}.
\]

**Model performance measures** To measure the predictive performance of our models, we calculated the correlation to average (Cadena et al., 2022; Franke et al., 2022; Willeke et al., 2022) on the held out test set images. Given a neuron’s response \( r_{ij} \) to image \( i \) and repeat \( j \) and the model predictions \( \hat{a}_i \), the correlation is computed between the predicted responses and the average neuronal response \( \bar{r}_i \) to the \( i^{th} \) test image (averaged across repeated presentations of the same stimulus):

\[
\rho_{\text{av}} = \text{corr}(r_{\text{av}}, \hat{a}_{\text{av}}) = \frac{\sum_i (\bar{r}_i - \bar{r})(\hat{a}_i - \bar{a})}{\sqrt{\sum_i (\bar{r}_i - \bar{r})^2 \sum_i (\hat{a}_i - \bar{a})^2}},
\]

(4)
where $\bar{r}_i = \frac{1}{J} \sum_{j=1}^J r_{ij}$ is the average response across $J$ repeats, $\bar{r}$ is the average response across all repeats and images, and $\alpha$ is the average prediction across all repeats and images.

**Generation of MEIs** We used the trained model to synthesize maximally exciting input images (MEIs) for each neuron using regularized gradient ascent (Bashivan et al., 2019; Franke et al., 2022; Walker et al., 2019). Starting out with a randomly initialized Gaussian white noise image given by $x \in \mathbb{R}^{h \times w}$, with height $h$ and width $w$, we showed the image to the model and computed the gradients of a single target neuron w.r.t. the image. To avoid high frequency artifacts, after each iteration we applied Gaussian blurring with a $\sigma$ of 1 pixel to smoothen the image. Additionally, we constrained the entire image to have a fixed energy budget, which we implemented as a maximum L2 norm of the standardized image, calculated across all pixel intensities. We chose an L2 norm of 25 for all neurons such that the resulting MEIs had minimal and maximal values similar to those found in our training natural image distribution. If the MEI exceeded the allowed norm budget after any iteration, we divided the MEI by factor $f_{\text{norm}}$ with $f_{\text{norm}} = \frac{\|MEI\|_2}{b}$. Additionally, enforced that the MEI could not contain values outside of the 8-bit pixel range by clipping the MEI outside of the bounds that correspond to 0 or 255 pixel-intensity. We used the stochastic gradient descent (SGD) optimizer with learning rate of 10. We ran each optimization for 1000 iterations, without early stopping.

**MEIs with transparency masks** Furthermore, we employed a novel technique of synthesizing MEIs using a transparency channel based on the idea of Mordvintsev et al. (2018). Given an MEI optimized with a method as described in the section above, it is difficult to distinguish which of the MEI features are important, i.e. strongly activate the neuron, and which ones are not. Through our in-built L2 energy constraint, there only is finite contrast that the model is able to distribute across the image. However, this is still uninformative regarding which features of the MEI are most important. Thus, we adopted a transparency method as a differentiable parametrization (Mordvintsev et al., 2018), which jointly optimizes the MEI and a transparency mask, with the objective of making the MEI itself as transparent as possible (i.e. uninformative parts of the MEI), while still retaining the high neuronal activation of the resulting image. More specifically, we optimized an image $x \in \mathbb{R}^{c \times h \times w}$, with channels $c$, height $h$ and width $w$. We set the channels $c = 2$, treated the first channel as the MEI $x_{\text{mei}}$, and the second channel as a transparent mask $x_{\alpha}$, which we optimized jointly as follows: (1) In each iteration, we drew a random image $x_{bg}$ from the training set as a background. (2) We clip the second MEI channel, i.e. the transparent mask, between the values 0–1, with 1 meaning that the MEI is fully opaque, and 0 meaning the the MEI is not visible at all. (3) Then, we blend the background and the MEI according to the transparency mask to get the combined image $x_{\text{combined}}$ with

$$x_{\text{combined}} = x_{bg} \times (1 - x_{\alpha}) + x_{\text{mei}} \times x_{\alpha}$$ (5)

We then showed the combined image to the model to compute the neuronal response of the target neuron. With no additional constraints, the model did in fact learn to set all values of the transparent mask to 1, so that it is necessary to change the MEI objective function $L_{\text{old}}$ from simply maximizing the neuronal response $r$ to penalize alpha values of zero, as suggested by Mordvintsev et al. (2018):

$$L_{\text{new}} = r \times (1 - \text{mean}(x_{\alpha}))$$ (6)

We used the same learning rate and optimizer as for our default gradient descent MEIs. We also applied the same L2 contrast constraint of 25, but only to the MEI image channel $x_{\text{mei}}$. For our closed loop experiments, we ran the initial 16 sessions with the default gradient ascent MEIs, and the final 8 sessions with the transparency method, observing similar success for the in vivo verification. Because the transparency method seemed to generate MEIs that were less spread out and had features that were perceptually easier to identify, we used exclusively this method to generate the MEIs for the full dataset. For all the 889 out of 1244 neurons that passed our threshold of correlation to average larger than 0.3, we generated 50 MEIs per neuron for a total of 44,450 MEIs. Each MEI took on average 2 minutes on a NVIDIA 2080ti GPU, resulting in a total compute time of ~60 GPU weeks.

**Centering of MEIs** In this work, we do not further analyze the transparent MEI masks. However, we use the transparent masks to center the MEIs for the similarity quantification. After MEI optimization, the MEI is located at the approximate RF location of each neuron. To center the MEIs, we find the center of mass of the transparent mask, and move the MEI such that the center of mass is at the center. All MEIs shown throughout this manuscript are shown at the center location for ease of comparison.

**Psychophysics** In our psychophysics experiment, the objective was to assess the perceptual similarity between MEIs originating from either a single recording session as compared to a random selection of neurons from different recording sessions. For this purpose, we devised a two-alternative forced choice task in which we showed two sets of MEIs, arranged in 3x3 grids as the basis for the similarity evaluation task. Participants were instructed to simply report which of the MEIs in the two grids looked more similar to each other. No other information apart from the displayed MEIs was provided.

To obtain the images for the task, we randomly chose 50 out of 52 sessions that had a minimum of 9 well-predicted neurons, using the threshold of correlation to average larger than 0.3. From these selected sessions, the top 9 well-predicted neurons were identified, resulting in a total pool of 450 neurons. For each session, participants were presented with images from the top 9 predicted neurons...
and a randomly selected set of 9 additional neurons from the pool, sampled without replacement. Specifically, for each neuron, we presented five MEIs, generated by starting from a different initial noise image during optimization, as images and compiled in a GIF. Participants were shown the two example sessions which were not included in the study, together with the correct solution. The subjects had unlimited time to make their choice.

Subject recruitment involved lab members that were familiar with the concept of an MEI from all research groups contributing to this article. In total, we recorded the responses of N=25 observers.

**Closed-loop procedure** Our closed loop experiments were composed of a generation and verification session. In the generation session, we recorded the electrophysiological responses of V4 neurons to full-field gray-scale natural images for 600 trials, corresponding to 9,000 unique images. After showing all of these trials, we stopped and promptly restarted the neurophysiological acquisition system to continue recording neuronal activity while we processed the data from the generation session. During this analysis period, we isolated single units and used these units to train several models to predict neuron responses to natural images. We produced an ensemble of the best five models, used this ensemble to select the six highest predicted units and generate ten MEIs per unit. We computed the mask of each MEI by calculating the z-score of each pixel value and setting a threshold (\(z = 0.35\)) to isolate the area within the mask. We then created a convex hull to close any holes and smoothed the edges with a Gaussian filter (\(\sigma = 2\)). We used this masking procedure for our natural image control selection procedure. Specifically, we screened a distinct set of 5,000 natural images, different from our training, validation, and test set images. This set was selected randomly from a database of 100k images, and we screened this same image set for all neurons across all closed-loop experiments. Each image was masked with the ten MEI masks of each unit and re-normalized to the contrast of the MEIs, resulting in 50,000 total screened images for each unit. We selected the seven highest activating masked natural images of each unit to use as controls for the verification recording.

**Closed-loop stimulation paradigm** During the verification session of the closed-loop experiment, we displayed one MEI and seven controls for each of the six units. These stimuli were centered on the RF and repeated 10 times throughout the experiment. We also showed the same full-field test set natural images 20 times each, to enable functional response matching between the generation and verification units. Each trial contained 15 images, composed of either (i) randomly interleaved generated stimuli (i.e. MEIs and masked controls) or (ii) full-field test set natural images, as described previously. Trials were randomly interleaved. In total, 100 trials of full-field images and 180 trials of generated stimuli were shown.

**Closed-loop unit matching** To assess the stability of our closed-loop neurons, we developed a procedure for spike waveform matching single units between the generation and verification session recordings. To do this, we performed a post hoc spike sorting of the full recording session, which was produced by stitching together the raw data files of the generation and verification recordings. The verification recording includes the analysis period immediately after the generation recording, during which we isolate single units and generate their MEIs. This continuity of recording allows us to more easily track single units throughout the experiment. Furthermore, spike sorting the full session allows us to use a drift correction of the spike sorting model based on a kalman-filter across the entire experiment, which aided the accuracy of our single unit tracking.

We then executed a two-step matching procedure using the spike sorting results of both the generation and full sessions. To determine potentially matched units, we first took the spikes of the generation session units and assigned them to full session units. We then calculated the proportion of spikes that were assigned exclusively to one unit in both the generation and verification sessions. If a unit in the generation session had at least 95% of its spikes assigned to only one single unit in the full session, this was considered a possible match. To confirm true matches, we assigned the full session spikes to the generation session units. If a unit in the full session had at least 95% of its spikes assigned to the potentially matched single unit in the generation session, these units were verified to be a match, and thus certified as stable. We additionally assessed neuron stability by computing the functional consistency of each unit. To compute this measure, we used the test set of 75 full-field natural images that were shown in both generation and verification session and calculated the Pearson correlation to the repeat-averaged responses in both sessions. We set a minimum functional consistency threshold of 0.5. Taken together, we were able to waveform match 82 neurons from 24 closed-loop sessions, with 27 of these failing to meet the functional consistency criterion, resulting in n=55 neurons for the analysis of the closed-loop paradigm.

**MEI similarity quantification using contrastive learning** We used a recently proposed method of contrastive learning (Böhm et al., 2023) to quantify the perceptual similarity of our neurons’ MEIs. The method is based on SimCLR (Chen et al., 2020), a method of self-supervised contrastive learning of visual representations in which images are embedded in a high-dimensional space. In this space, augmentations of the same image are learned to have small distances while simultaneously training the model to increase the distance to all other images. Böhm et al. (2023) adapted this procedure for a two-dimensional space by combining the ideas of contrastive learning with 2-d neighbor embeddings as used in t-SNE (van der Maaten & Hinton, 2008). Their new method, called t-SimCNE, achieves this by changing the similarity function...
between image embeddings from cosine-similarity used in SimCLR, which would constrain the embeddings to the unit circle, to Euclidean distance $d_{ij} = \|z_i - z_j\|$ between the embeddings $z_i$ and $z_j$ of two augmentations $i$ and $j$ of the same image. We use this method to train a model end-to-end to embed our MEIs using the loss function as proposed by Böhm et al. (2023):

$$
\ell_{t-SimCNE}(i,j) = -\log \frac{1}{\sum_{k \neq i} 1/(1 + d_{ik}^2)}.
$$

(7)

In our adaptation, $i$ and $j$ correspond to two data augmentations of the same MEI, and $z$ denotes the 2-d embedding, which is the model output. For a given batch size $b$, the resulting batch size is $2b$ because each MEI is augmented twice. As pointed out by the authors of SimCLR (Chen et al., 2020), this approach requires careful selection of data augmentations, as well as choosing the largest batch size possible.

Taken together, our training procedure consists of these steps: We first select all 889 neurons above the model performance threshold of correlation to average larger than 0.3, as described earlier. For each neuron, from the 50 MEIs that we optimized per neuron, we select only the MEIs that elicited at least 90% of the predicted firing rate of the highest-activating MEI, which resulted in anywhere from 3 to 42 MEIs per neuron, with a total of $n=19,688$ MEIs used in this and subsequent analyses. This selection was important as there can be failures during optimizing MEIs, resulting in noisy images which the contrastive learning algorithm was very sensitive to. Next, from all the MEIs that we selected, we assembled a batch of size $n=889$, by randomly drawing one MEI for each neuron.

Subsequently, we preprocessed the MEIs and applied the data augmentations in the following order: (1) centering the MEIs as described above, (2) center cropping to resize the MEIs from 100x100 to 75x75 pixels, (3) random rotation between 0 and 30 degrees, (4) random rescaling between 32x32 and 75x75 pixels, (5) random cropping from the resulting image to a final size of 32x32 pixels. Steps (2) to (4) were applied twice to each MEI to obtain two augmentations per MEI. The resulting training batch thus consisted of a randomly drawn MEI per neuron, augmented twice, for a total batch size of 889^2=1,778 images, with the model's objective being to minimize the distance between each pair, and to maximize the distance from all-to-all images which are not pairs. It is important to point out that with this training scheme, the trained model was given no information about recording sessions or which neurons' identity of each MEI. Therefore, an important sanity-check for the trained model is to analyze the 2-d embedding distances of all MEIs that we optimized for a single neuron. We perform this analysis by simply calculating all pairwise distances and taking the average of all MEIs per neuron.

Contrastive learning: Session distances We first averaged all pairwise distances across neurons recorded within one session to obtain a within-session distance in the 2-d embedding space. We then compared this within-session distance to a shuffled control. For this control, we used bootstrapping to sample at random the same number of neurons as in a given session, with the constraint that they cannot be from the session in question and that all randomly drawn neurons originate from different sessions. We then computed the mean pairwise distance for these shuffled neurons, and repeated this process 25,000 times for each session to get the null distribution. We then calculated the percentile of the true within-session distance against each sessions' null distribution to obtain a p-value.

Contrastive learning: HDBSCAN cluster cutting After we obtained the 2-d embedding space of MEIs, we clustered this entire two-dimensional space using hierarchical density-based spatial clustering of applications with noise (HDBSCAN McInnes et al., 2017), the same clustering that was employed by the t-simCNE authors (Böhm et al., 2023). We searched over the parameter grid minimum cluster size $\in \{100, 125, \ldots, 400\} \times$ and minimum...
samples, which indicates the minimum number of samples to be considered non-noise, \( \in \{5,15,\ldots,145\} \) with the constraint \( \text{min-samples} \leq \text{min-cluster-size} \). The resulting clusterings will create one clustered group labelled -1, for MEIs that were unable to be clustered. We selected the parameters \( \text{min-cluster-size} = 200 \) and \( \text{min-samples} = 10 \) which resulted in the lowest number of unassigned MEIs. Using this approach, the MEIs of each neuron get assigned a label, with the possibility that not all MEIs of single neuron were assigned to the same cluster. We assigned a cluster ID to a neuron if more than half of its MEIs had the same cluster ID. Furthermore, we excluded neurons for which the more than half of the MEIs were in the unassigned category -1 of the HDBSCAN algorithm. Based on these two criteria, 828 out of 889 neurons were given a valid clustering ID.

**Representational similarity of MEIs** As an independent way to verify the similarity of MEIs, we computed their representational similarity. For this purpose, we used the centered MEIs, and computed the responses of all 889 well-predicted neurons from our neural predictive model to each MEI. We controlled for the different RF positions of each *in silico* neuron by artificially centering the *in silico* neuron’s RF to the center by setting the readout location of the Gaussian readout to the center of the core output. We used this approach for each model ensemble member individually and again took the model ensemble average as the predicted neuronal activity. Consequently, for each MEI, we obtained a response vector of length 889, which we then used for pairwise comparisons using cosine similarity. We then compared the average cosine similarity either within clusters or within recording sessions to the average similarity across sessions/clusters. To obtain a p-value for the similarity within vs. across clusters, we computed the similarity matrix 100 times. In each of the 100 runs, per neuron we drew at random one of the neurons MEIs and computed the population response vector for that MEI. We thus ended up with 100 similarity matrices, for which the pairwise comparisons were thus computed based on different MEIs. For each cluster, we then computed the average similarity across the 100 runs, and compared this similarity. We then took (1) the average cosine similarity within each cluster across the 100 runs, and (2) for each of the 100 runs, for each cluster we average the similarity to all other clusters. We report the p-value as percentile of the within-session similarity to the distribution of across-session similarity.

**Data and code availability**

The analysis code will be publicly available in an online repository latest upon journal publication. Our coding framework uses Pytorch (Paszke et al., 2019), NumPy (Harris et al., 2020), scikit-image (Van der Walt et al., 2014), matplotlib (Hunter, 2007), seaborn (Waskom et al., 2017), DataJoint (Yatsenko et al., 2015), Jupyter (Kluyver et al., 2016), and Docker (Merkel, 2014). We also used the following custom libraries and code: neuralpredictors (https://github.com/sinzlab/neuralpredictors) for torch-based custom functions for model implementation, nnfabrik (https://github.com/sinzlab/nnfabrik) for automatic model training pipelines using DataJoint, nnvision (https://github.com/sinzlab/nnvision) for specific model definitions, analysis, and figures.
Supplementary Information

Supplemental Fig. 1 - Waveform and functional matching of single units across recordings
Supplemental Fig. 2 - Diverse model-derived stimuli of individual monkey V4 neurons
Supplemental Fig. 3 - Similarity of optimal stimuli in neuronal response space
Supplemental Fig. 4 - Overview of optimal stimuli of V4 response modes
Supplemental Fig. 1. Spike waveform and functional matching of single units across recordings. 

a. Schematic illustrating spike sorting of the closed-loop experimental paradigm. The "generation session" is spike sorted directly after the recording, resulting in "Sorting 1". This data is then used for model training and optimization of MEIs, which are presented back to the animal during the "verification session". The verification session recording starts immediately after the generation session recording ends, to ensure a continuous monitoring of the recorded units over time. After the experiment, the generation and verification session recordings are concatenated ("full session") and spike sorted, resulting in "Sorting 2".

b. Unit matching based on spike waveforms across Sorting 1 (generation session) and Sorting 2 (full session) for an example session. The left plot shows the percentage of spikes of the Sorting 1 units assigned to the units of Sorting 2. Units were assigned by passing the principal components of each spike, extracted using the Sorting 1 Gaussian Mixture model (GMM), to the Sorting 2 model. For a potential match (orange), at least 95% of the spikes of a single unit of Sorting 1 had to be assigned to an individual unit of Sorting 2. The right plot shows the percentage of spikes of Sorting 2 units assigned to the units of Sorting 1. For a final match (red), at least 95% of the spikes of a single Sorting 2 unit had to be assigned to the potential match of Sorting 1.

c. Distribution of correlations of mean test set responses for all final matches. We only included matched units into the analysis, if their functional correlation was at least 0.5.
Supplemental Fig. 2. Diverse model-derived stimuli of individual monkey V4 neurons. a, For a set of 14 example neurons, we show 10 MEIs per neuron, generated from different starting points (random seeds) during the MEI optimization. The different MEIs exhibit the same visual feature but somewhat differ with respect to orientation, scale and position. b, Same as (a), for another set of 14 neurons.
Supplemental Fig. 3. Similarity of optimal stimuli in neuronal response space. 

**a,** MEIs of three example neurons. Right shows a schematic illustrating how we compared the similarity of MEIs using representational similarity. In brief, each MEI was presented to the trained CNN model that was used to produce the MEIs to obtain a response vector. The response vectors were then compared using cosine similarity.  

**b,** Mean cosine similarity of MEIs within a single recording session (diagonal) and across recording sessions for n=88 sessions, peak-normalized for each row.  

**c,** Distribution of percentiles of within-session similarity. For example, a percentile of 0.05 means that the MEI similarity within the session was larger than the MEI similarity to 95% of the other sessions. For n=30/55 sessions, the percentile was <0.05.  

**d,** Cosine similarity of MEIs of n=889 neurons, sorted based on cluster assignment (cf. Fig. 5).  

**e,** Mean cosine similarity of MEIs within a cluster (diagonal) and across clusters, peak normalized per row. The matrix depicts the mean across n=100 similarity matrices, each generated based on a different random selection of MEIs per neuron. Top shows distribution of cosine similarity within an example cluster (black) and the mean similarity to all other clusters (gray).  

**f,** Mean within-cluster and across-cluster similarity for all clusters.
Supplemental Fig. 4. Overview of optimal stimuli of V4 response modes. a, MEIs of example neurons for five response modes not shown in Fig. 5.