# Appendix B: Salamander Example Comparing GLMMs, Zero-Inflated GLMMs, and Hurdle Models

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In this appendix, we reanalyze counts of salamanders in streams. Repeated samples of salamanders were taken at 23 sites. Some of the sites were affected by mountian top removal coal mining. The data was originally published in Price et al. (2016) and was aquired from Dryad (Price et al. (2015)).

### **Preliminaries**

### Load packages

```
library(glmmTMB)
library(ggplot2); theme_set(theme_bw())
library(knitr)
library(bbmle) #for AICtab
library(reshape)
library(plyr)
```

### Load and organize data

```
data(Salamanders)
head(Salamanders)
##
      site mined cover sample DOP Wtemp
                                            DOY spp count
## 1 VF -1
             yes -1.44
                            1 -0.6 -1.229 -1.50
                                                 GP
## 2 VF- 2
                  0.30
                            1 -0.6 0.085 -1.50
                                                 GP
## 3 VF -3
                  0.40
                            1 -1.2 1.014 -1.29
                                                 GP
                                                         0
             yes
                                                         2
     R -1
              no -0.45
                               0.0 -3.023 -2.71
## 5
                  0.60
                               0.6 -0.144 -0.69
                                                  GP
                                                         2
     R -2
## 6 R -3
                  1.34
                            1 0.6 -0.015 -0.69
Salamanders = transform(Salamanders, present = as.numeric(count>0))
```

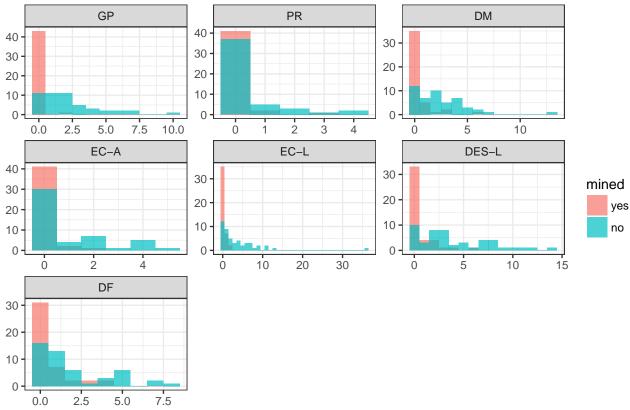


Figure B.1 – Observed count data. Histograms of count data split into separate panels for each species or life stage. Each panel contains two overlaid histograms in which color represents whether the site affected by mining or not.

# Model fitting with glmmTMB

These analyses are intended to be a simple demonstration of how to use some features of the glmmTMB package, so we do not attempt to fit all of the models that could be reasonable to try with the covariates that were collected.

#### Poisson Models

The syntax for fitting GLMMs with glmmTMB is quite similar to using glmer. In the first model, the formula, count~spp + (1|site), says that counts depend on species and vary randomly by site. We also pass it the data frame, Salamanders, and specify a Poisson distribution using the family argument. glmmTMB assumes that we want a log-link with the Poisson distribution because that's the standard.

```
pm0 = glmmTMB(count~spp + (1|site), Salamanders, family=poisson)
pm1 = glmmTMB(count~spp + mined + (1|site), Salamanders, family=poisson)
pm2 = glmmTMB(count~spp * mined + (1|site), Salamanders, family=poisson)
```

### Negative binomial models

```
nbm0 = glmmTMB(count~spp + (1|site), Salamanders, family=nbinom2)
nbm1 = glmmTMB(count~spp + mined + (1|site), Salamanders, family=nbinom2)
nbm2 = glmmTMB(count~spp * mined + (1|site), Salamanders, family=nbinom2)
```

Unlike the Poisson, the negative binomial distribution has a dispersion parameter. If we expected the counts to become more dispersed (relative to the mean) as the year progresses, then we could use the dispersion formula to model how the dispersion changes with the day of the year (DOY) using disp=~DOY.

```
nbdm0 = glmmTMB(count~spp + (1|site), disp=~DOY, Salamanders, family=nbinom2)
nbdm1 = glmmTMB(count~spp + mined + (1|site), disp=~DOY, Salamanders, family=nbinom2)
nbdm2 = glmmTMB(count~spp * mined + (1|site), disp=~DOY, Salamanders, family=nbinom2)
```

#### Zero-inflated models

To fit zero-inflated models, we use the ziformula argument, or glmmTMB will also recognize zi. This is a formula that describes how the probability of an extra zero (i.e. structural zero) will vary with predictors. In this example, we might assume that absences will at least vary by species (spp), so we write zi=~spp. This formula only has a right side because the left side is always the probability of having a structural zero in the response that was specified in the first formula. The zero-inflation probability is always modeled with a logit-link to keep it between 0 and 1.

```
zipm0 = glmmTMB(count~spp +(1|site), zi=~spp, Salamanders, family=poisson)
zipm1 = glmmTMB(count~spp + mined +(1|site), zi=~spp, Salamanders, family=poisson)
zipm2 = glmmTMB(count~spp + mined +(1|site), zi=~spp + mined, Salamanders, family=poisson)
zipm3 = glmmTMB(count~spp * mined +(1|site), zi=~spp * mined, Salamanders, family=poisson)
zinbm0 = glmmTMB(count~spp +(1|site), zi=~spp, Salamanders, family=nbinom2)

## Warning in glmmTMB(count ~ spp + (1 | site), zi = ~spp, Salamanders,
## family = nbinom2): Model convergence problem; non-positive-definite Hessian
## matrix. See vignette('troubleshooting')
zinbm1 = glmmTMB(count~spp + mined +(1|site), zi=~spp, Salamanders, family=nbinom2)

## Warning in glmmTMB(count ~ spp + mined + (1 | site), zi = ~spp,
## Salamanders, : Model convergence problem; non-positive-definite Hessian
## matrix. See vignette('troubleshooting')
zinbm2 = glmmTMB(count~spp + mined +(1|site), zi=~spp + mined, Salamanders, family=nbinom2)
zinbm3 = glmmTMB(count~spp * mined +(1|site), zi=~spp * mined, Salamanders, family=nbinom2)
```

The warning messages tell us that zinbm0 and zinbm1 did not converge. However, the models with mined as a predictor of zero-inflation did converege.

#### Hurdle models

We can also fit hurdle models in a single model by using a truncated distribution for the conditional model and adding zero-inflation.

# Model comparison using AIC

We can use AICtab to compare all the GLMMs, including zero-inflated and hurdle models.

```
AICtab(pm0, pm1, pm2,
nbm0, nbm1, nbm2,
nbdm0, nbdm1, nbdm2,
zipm0, zipm1, zipm2, zipm3,
zinbm0, zinbm1, zinbm2, zinbm3,
hpm0, hpm1, hpm2,
hnbm0, hnbm1, hnbm2)
```

```
##
          dAIC df
## nbm2
            0.0 16
## nbdm2
            1.5 17
            6.3 30
## zinbm3
## zinbm2
            6.9 18
## nbm1
            9.0 10
## nbdm1
            9.6 11
## hnbm1
           12.3 18
## hnbm2
           14.4 24
## nbm0
           38.6 9
## nbdm0
           39.0 10
## zipm3 114.7 29
## zipm2 122.1 17
## hpm2
          124.0 23
## hpm1
          126.8 17
## zipm1 139.6 16
## zipm0 169.1 15
## hnbm0
         194.9 16
## pm2
          276.9 15
## pm1
          299.5 9
          313.2 15
## hpm0
## pm0
          329.3 8
## zinbm0
             NA 16
## zinbm1
             NA 17
```

The log-likelihood of the unconverged models is reported as NA so that these models appear at the end of the AIC table. The negative log-likelihood could be extracted with zipmO\$fit\$objective if it was needed.

The most parsimonious model has a negative binomial distribution with effects of species, mining, and their interaction.

# Model summary

The summary of the negative binomial GLMM is similar to the familiar output from glmer, so we also present the summary from a more complicated model below to demonstrate output from zero-inflation and dispersion

models.

```
summary(nbm2)
```

```
## Family: nbinom2 (log)
                     count ~ spp * mined + (1 | site)
## Formula:
## Data: Salamanders
##
##
                       logLik deviance df.resid
        AIC
                 BIC
##
       1663
                1735
                         -816
                                  1631
                                            628
##
## Random effects:
##
## Conditional model:
## Groups Name
                       Variance Std.Dev.
## site
           (Intercept) 0.284
                                0.533
## Number of obs: 644, groups:
## Overdispersion parameter for nbinom2 family ():
##
## Conditional model:
                    Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                      -3.375
                                  0.758
                                          -4.45 8.4e-06 ***
## sppPR
                       0.931
                                  0.877
                                           1.06 0.28883
## sppDM
                       2.249
                                  0.788
                                           2.85 0.00431 **
## sppEC-A
                                           0.79 0.43003
                       0.714
                                  0.905
## sppEC-L
                       1.813
                                  0.813
                                           2.23 0.02574 *
## sppDES-L
                       2.511
                                  0.779
                                           3.22 0.00128 **
## sppDF
                                  0.780
                                           3.30 0.00096 ***
                       2.576
## minedno
                       4.162
                                  0.793
                                           5.25
                                                 1.5e-07 ***
## sppPR:minedno
                                  0.933
                                          -2.77
                                                 0.00562 **
                      -2.583
## sppDM:minedno
                      -2.150
                                  0.826
                                          -2.60
                                                 0.00925 **
## sppEC-A:minedno
                      -1.583
                                          -1.67 0.09434 .
                                  0.946
## sppEC-L:minedno
                      -1.338
                                  0.849
                                          -1.58 0.11510
                                          -2.37 0.01773 *
## sppDES-L:minedno
                      -1.936
                                  0.816
## sppDF:minedno
                      -2.743
                                  0.822
                                          -3.34 0.00084 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(glmmTMB(count~spp+mined+(1|site), zi=~spp+mined , disp=~DOY, Salamanders, family=nbinom2))
## Family: nbinom2
                     ( log )
## Formula:
                     count ~ spp + mined + (1 | site)
## Zero inflation:
                           ~spp + mined
## Dispersion:
                           ~DOY
## Data: Salamanders
##
##
                       logLik deviance df.resid
        AIC
                 BIC
##
                1755
                         -816
                                  1632
       1670
                                            625
## Random effects:
## Conditional model:
## Groups Name
                       Variance Std.Dev.
## site
           (Intercept) 0.137
                                0.37
```

```
## Number of obs: 644, groups: site, 23
##
##
   Conditional model:
##
                Estimate Std. Error z value Pr(>|z|)
##
   (Intercept)
                 -0.6397
                              0.4096
                                       -1.56
                                               0.11835
                              0.5642
                                       -1.47
##
   sppPR
                 -0.8280
                                               0.14223
                                               0.35222
## sppDM
                  0.2202
                              0.2367
                                         0.93
## sppEC-A
                 -0.2308
                              0.3376
                                        -0.68
                                               0.49410
   sppEC-L
                  0.4278
                              0.2376
                                         1.80
                                               0.07177
##
   sppDES-L
                  0.6155
                              0.2253
                                         2.73
                                               0.00629 **
  sppDF
                 -0.0673
                              0.2445
                                        -0.28
                                               0.78300
                                               0.00013 ***
##
  minedno
                  1.4180
                              0.3705
                                         3.83
##
  Signif. codes:
                      '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
                    0
##
##
   Zero-inflation model:
##
                Estimate Std. Error z value Pr(>|z|)
   (Intercept)
                   0.871
                               0.635
                                         1.37
                                                 0.170
##
                   1.352
                                         1.28
                                                 0.199
  sppPR
                               1.053
##
##
   sppDM
                  -0.865
                               0.787
                                        -1.10
                                                 0.272
##
  sppEC-A
                   1.162
                               0.674
                                         1.72
                                                 0.085
## sppEC-L
                               0.744
                                        -0.85
                                                 0.395
                  -0.633
## sppDES-L
                  -0.890
                               0.752
                                       -1.18
                                                 0.237
## sppDF
                  -2.396
                               2.012
                                        -1.19
                                                 0.234
## minedno
                  -2.541
                               0.578
                                        -4.39 0.000011 ***
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
  Signif. codes:
##
##
## Dispersion model:
##
                Estimate Std. Error z value Pr(>|z|)
##
   (Intercept)
                   0.433
                               0.245
                                         1.77
                                                 0.077 .
## DOY
                  -0.252
                               0.195
                                       -1.29
                                                 0.196
##
                    0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

This summary can be broken down into five sections. The top section is a general overview containing a description of the model specification (Family, Formula, Zero inflation, Dispersion, Data) and resulting information criteria. The information criteria are only meaningful in comparison to other models fit by glmmTMB; this is because glmmTMB does not drop any constants from the likelihood while some other packages do. The second section describes the variability of the Random effects. In this model, we only had random effects on the conditional model, but random effects from the zero-inflation model could also appear here. The third section describes the coefficients of the Conditional model including Wald z statistics and p-values. Apart from the intercept, the estimates are all contrasts as is standard in regression models. This model has a log link as stated in the top line of the summary. The fourth section describes the Zero-inflation model similarly to the Conditional model except that this model has a logit-link. The zero-inflation model estimates the probability of an extra zero such that a positive contrast indicates a higher chance of absence (e.g. minedno < 0 means fewer absences in sites unafected by mining); this is the opposite of the conditional model where a positive contrast indicates a higher abundance (e.g., minedno > 0 means higher abundances in sites unafected by mining). The last section describes the Dispersion model, which uses a log link to keep the dispersion parameter positive. This is in contrast to the summary of nbm2 above, where there is no dispersion model and the overdispersion parameter is reported on the natural (rather than log) scale.

# Plotting model results

As previously discussed in various places, there are a whole bunch of decisions to make about marginalizing over or conditioning on the random effects. See discussion at this link.

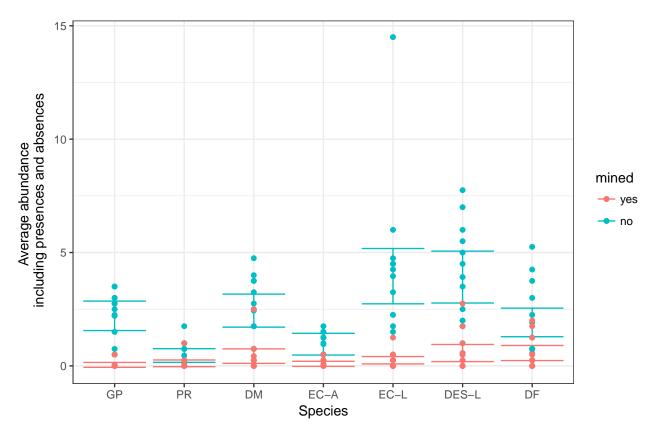
For demonstration purposes, we plot results from the top zero-inflated model zinbm3.

## Quick and dirty plot

It's easiest to see the pattern by using the **predict** function. To avoid marginalizing over or conditioning on random effects, we can refit the best model without the random effect of site; however, this is not ideal because it ignores the correlation within sites. We present a more rigorous version next.

The predict function has a parameter **zitype** that specifies whether you want predictions from the conditional model, the zero-inflation model, or the expected response that combines both parts of the model.

```
zinbm3FE = glmmTMB(count~spp * mined, zi=~spp * mined, Salamanders, family=nbinom2)
newdata0 = newdata = unique(Salamanders[,c("mined","spp")])
temp = predict(zinbm3FE, newdata, se.fit=TRUE, zitype="response")
newdata$predFE = temp$fit
newdata$predFE.min = temp$fit-1.98*temp$se.fit
newdata$predFE.max = temp$fit+1.98*temp$se.fit
real=ddply(Salamanders, ~site+spp+mined, summarize, m=mean(count))
ggplot(newdata, aes(spp, predFE, colour=mined))+geom_point()+
    geom_errorbar(aes(ymin=predFE.min, ymax=predFE.max))+
    geom_point(data=real, aes(x=spp, y=m))+
    ylab("Average abundance \n including presences and absences")+
    xlab("Species")
```



 $Figure~B.2-Estimated~abundance~ignoring~correlation.~{\rm Points~represtent~site-specific~average~counts.~Error~bars~represent~the~95\%~Wald-type~confidence~intervals~for~the~predicted~average~count.}$ 

### Alternative prediction method

We can predict at the population mode, by setting the random effects to zero.

```
X.cond = model.matrix(lme4::nobars(formula(zinbm3)[-2]), newdata0)
beta.cond = fixef(zinbm3)$cond
pred.cond = X.cond %*% beta.cond

ziformula = zinbm3$modelInfo$allForm$ziformula
X.zi = model.matrix(lme4::nobars(ziformula), newdata0)
beta.zi = fixef(zinbm3)$zi
pred.zi = X.zi %*% beta.zi
```

These are estimates of the linear predictors (i.e., predictions on the link scale: logit(prob) and log(cond)), not the predictions themselves. The easiest thing to do for the point estimates of the unconditional count (ucount) is to transform to the response scale and multiply:

```
pred.ucount = exp(pred.cond)*(1-plogis(pred.zi))
```

For the standard errors/confidence intervals, we could use posterior predictive simulations (i.e. draw MVN samples from the parameter for the fixed effects). This conditions on/ignores uncertainty in the random-effect parameters.

```
library(MASS)
set.seed(101)
pred.condpar.psim = mvrnorm(1000,mu=beta.cond,Sigma=vcov(zinbm3)$cond)
```

```
pred.cond.psim = X.cond %*% t(pred.condpar.psim)
pred.zipar.psim = mvrnorm(1000,mu=beta.zi,Sigma=vcov(zinbm3)$zi)
pred.zi.psim = X.zi %*% t(pred.zipar.psim)
pred.ucount.psim = exp(pred.cond.psim)*(1-plogis(pred.zi.psim))
ci.ucount = t(apply(pred.ucount.psim,1,quantile,c(0.025,0.975)))
ci.ucount = data.frame(ci.ucount)
names(ci.ucount) = c("ucount.low","ucount.high")
pred.ucount = data.frame(newdata0, pred.ucount, ci.ucount)
```

These predicted counts should be close to the median counts, so we plot them together to compare.

```
real.count = ddply(Salamanders, ~spp+mined, summarize, m=median(count), mu=mean(count))
ggplot(pred.ucount, aes(x=spp, y=pred.ucount, colour=mined))+geom_point(shape=1, size=2)+
    geom_errorbar(aes(ymin=ucount.low, ymax=ucount.high))+
    geom_point(data=real.count, aes(x=spp, y=m, colour=mined), shape=0, size=2)+
    geom_point(data=real.count, aes(x=spp, y=mu, colour=mined), shape=5, size=2)+
    ylab("Abundance \n including presences and absences")+
    xlab("Species")
```

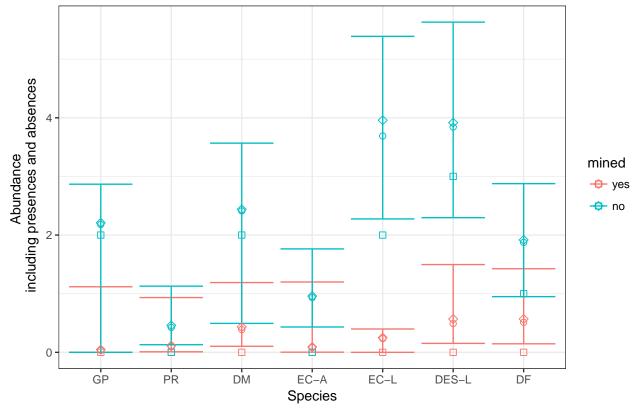


Figure B.3 – Estimated abundance at mode. Circles represent predicted unconditional counts at the mode (i.e., site effect = 0) and error bars represent the 95% confidence intervals for that mode. Squares represent the observed median and diamonds represent observed means calculated across samples and sites. In this highly skewed data, the mode is closer to the mean than the median.

# Simulating from a fitted model

We could also look at the distribution of simulated values from the best fitted model. For this we use the function simulate.glmmTMB. This function works for zero-inflated and hurdle models as well as less complex

models.

```
sims=simulate(nbm2, seed = 1, nsim = 1000)
```

This function returns a list of vectors. The list has one element for each simulation (nsim) and the vectors are the same shape as our response variable.

Then we can plot them with the observations summarized in the same way.

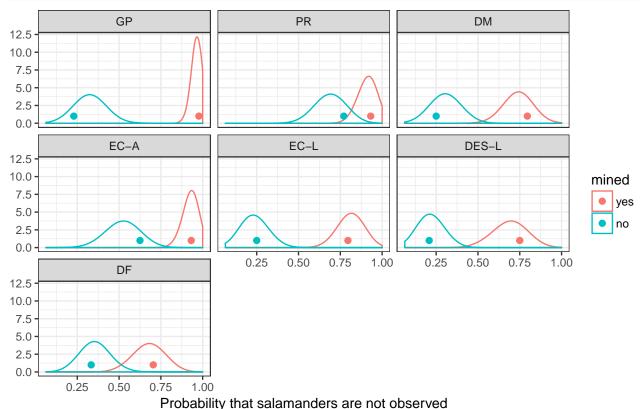
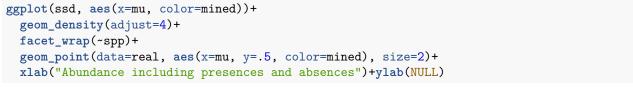


Figure B.4 – Simulated zero counts. Each panel represents a different species or life stage of a species. Densities are values from 1000 data sets simulated from our best fit model. Points represent the observed data.

We can see that this model does a good job of capturing the observed zero counts.



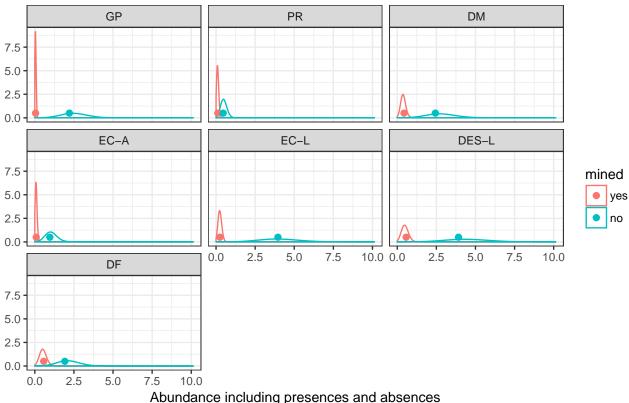


Figure B.5 – Simulated unconditional abundances. Each panel represents a different species or life stage of a species. Densities are values from 1000 data sets simulated from our best fit model. Points represent the observed data.

# References

Price, S J, B L Muncy, S J Bonner, A N Drayer, and C D Barton. 2015. "Data from: Effects of Mountaintop Removal Mining and Valley Filling on the Occupancy and Abundance of Stream Salamanders." *Journal of Applied Ecology*. Dryad Digital Repository. doi:doi:10.5061/dryad.5m8f6.

———. 2016. "Effects of Mountaintop Removal Mining and Valley Filling on the Occupancy and Abundance of Stream Salamanders." *Journal of Applied Ecology* 53 (2): 459–68. doi:10.1111/1365-2664.12585.