1 Tracking the mind's eye: Primate gaze behavior during virtual visuomotor

2 navigation reflects belief dynamics

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11 SUMMARY

To take the best actions, we often need to maintain and update beliefs about variables that cannot be directly 12 observed. To understand the principles underlying such belief updates, we need tools to uncover subjects' 13 belief dynamics from natural behaviour. We tested whether smooth eye movements could be used to infer 14 subjects' beliefs about latent variables using a naturalistic, visuomotor navigation task. We observed eve 15 movements that appeared to continuously track the goal location even when no visible target was present 16 there. Accurate goal-tracking was associated with improved task performance, and inhibiting eye 17 movements in humans impaired navigation precision. By using passive stimulus playback and manipulating 18 stimulus reliability, we show that subjects' eye movements are likely voluntary, rather than reflexive. These 19 results suggest that gaze dynamics play a key role in action-selection during challenging visuomotor 20

21 behaviours, and may possibly serve as a window into the subject's dynamically evolving internal beliefs.

22 INTRODUCTION

Rational behaviour in the real world often requires predicting latent variables from sensory observations. 23 Since latent variables cannot be directly observed, and since the utility of actions depends on the status of 24 latent variables in the future, subjects must use statistical regularities in space and in time to predict them. 25 There is a growing body of studies that not only demonstrate that humans exploit regularities in feature 26 space (Langer and Bülthoff, 2001; Miyazaki, 2005; Weiss et al., 2002), but also show how to infer the 27 associated subjective priors from data (Gosselin and Schyns, 2003; Houlsby et al., 2013; Körding and 28 Wolpert, 2004; Paninski, 2006; Smith et al., 2012; Stocker and Simoncelli, 2006; Turnham et al., 2011). In 29 contrast, we know relatively little about how physical laws that govern the temporal dynamics of inputs are 30 internalized and used to guide time-evolving beliefs in the absence of reliable observations (Lee et al., 31 2014). 32

The reasons for limited progress in understanding belief dynamics are twofold. First, psychophysics 33 continues to be dominated by experimental paradigms in which actions are discrete (e.g., binary choice) and 34 sporadic (*e.g.*, at the end of the trial). In contrast, continuous tasks (Bonnen et al., 2015; Huk et al., 2018; 35 Pitkow and Angelaki, 2017) provide subjects the opportunity to reveal more information about their beliefs 36 and predictions as they unfold in time. Second, although theoretical techniques to infer latent beliefs from 37 actions are slowly becoming available (Kumar et al., 2019; Reddy et al., 2018; Wu et al., 2018), they have 38 yet to be successfully applied to settings in which state and action spaces are both continuous. Consequently, 39 principled ways to reliably uncover subjects' belief dynamics from natural behaviour are still lacking. 40 Meanwhile, a practical way to overcome this hurdle would be by covertly 'measuring' those beliefs. One 41 candidate tool to accomplish this is eye-tracking (Spivey, 2007). Saccadic eye movements have previously 42 been used to understand mental processes underlying a wide variety of abstract tasks such as language 43 comprehension (Tanenhaus et al., 1995), reading (Rayner, 1998), mental imagery (Spivey and Geng, 2001), 44 visual search (Zhang et al., 2018), and even random number generation (Loetscher et al., 2010). 45 Furthermore, it has recently been argued that smooth-pursuit eye movements may be influenced by short-46 term memory (Deravet et al., 2018; Orban de Xivry et al., 2013). By formulating oculomotor pursuit to 47 transiently occluded moving targets as an active inference process, these eye movements have been used to 48 infer subjects' internal beliefs (Adams et al., 2012, 2015). We wanted to know whether eye movements 49 might also reflect belief dynamics for extended periods of time under more naturalistic conditions. 50

To address this, we first designed a challenging, naturalistic visuomotor task. We created a virtual 51 52 environment comprised solely of sparse optic flow cues in which subjects used a joystick to steer to a 53 memorized target location by integrating optic flow. To successfully perform the task, subjects had to continuously update an internal estimate of the relative target location by inferring their own movements 54 55 based on the sparse cues. To test whether eye movements were informative about those estimates, we recorded the gaze behaviour of humans and rhesus macaques while they performed this task. Parallel 56 experiments in the two species allowed us to test whether the observed eye movements were evolutionarily 57 conserved. We found that both humans and monkeys tend to follow the location of the unseen target with 58 their gaze until they reach it. By manipulating stimulus reliability and by using stimulus playback, we 59

- demonstrate that the eye movements are likely volitional, rather than reflexive. Furthermore, the subjects'
 success in tracking the target over time predicted their final behavioural accuracy. This latter result suggests
 that gaze dynamics reflect internal beliefs, and could help shed light on the computations that transform
- 63 visual perception to action in naturalistic settings.

64 **RESULTS**

Monkeys and humans performed a visual navigation task in which they used a joystick to steer to a cued 65 target location in a three-dimensional virtual reality (VR) environment without allocentric reference cues 66 (*i.e.* stable landmarks) (Fig 1A, Methods). At the beginning of each trial, a circular target blinked briefly at 67 a random location within the field of view on the ground plane, and then disappeared. We gave subjects a 68 joystick that controlled forward and angular velocities, allowing them to steer freely in two dimensions (Fig 69 **1B**). The subjects' goal was to steer towards the target, and stop when they believed their position fell within 70 a circular reward zone centered on the target. They received feedback about their performance immediately 71 at the end of each trial. 72

- Monkeys were first trained extensively using a staircase procedure (see **Methods**) until their performance 73 stopped improving. Here, we will focus only on their post-training behaviour. At this point, the radius of the 74 75 reward zone was fixed across trials (see Methods) and they received feedback in the form of juice reward at the end of the trial for correctly stopping within this zone (Fig 1C). In contrast, human subjects received no 76 prior training on this task. Instead, we used an adaptive feedback scheme in which the radius of the reward 77 zone was dynamically scaled using a staircase procedure to match individual subjects' abilities (Fig S1A, 78 see **Methods**). In practice, it took less than fifty trials for the performance of humans to stabilize (**Fig S1B**). 79 Therefore, we ignored the first fifty trials collected from human subjects and focused our analyses on the 80 remaining data. 81
- Target locations were uniformly distributed at random over the ground plane area within the subject's field of view (**Fig 1D** – *left*). The stimulus was nearly identical for both species except for minor details such as the range of target distances and the duration for which the target was visible (see **Methods**). All subjects were head-fixed, and we recorded each subject's movement trajectory (**Fig 1D** – *middle*) as well as eye position (**Fig 1D** – *right*) throughout each trial.

87 Behavioural performance

- **Figure 1E** shows the performance of the monkeys in this task. Both radial distance (**Fig 1E** *left*) and angular eccentricity (**Fig 1E** - *right*) of the monkeys' responses (stopping location) were highly correlated with the target location across trials (n = 3 monkeys, Pearson's $r \pm$ standard deviation, radial distance: 0.72 ± 0.1 , angle: 0.84 ± 0.1) suggesting that their behaviour was appropriate for the task. To test whether their performance was accurate, we regressed their responses against target locations. The slope of the regression was close to unity both for radial distance (mean \pm standard deviation = 0.92 ± 0.06) and angle (0.98 ± 0.1) suggesting that the monkeys were nearly unbiased (**Fig 1F** – *green*).
- We showed previously that humans are systematically biased when performing this task without feedback. 95 and that the bias was likely due to prior expectations that make them underestimate their movement 96 velocities (Lakshminarasimhan et al., 2018). Consistent with those findings, human subjects overshot the 97 target in an initial block of trials in which no feedback was provided (Fig S1C; n = 5, mean slope \pm 98 standard deviation, radial distance: 1.21 + 0.2, angle: 1.78 + 0.3), to a degree that was proportional to 99 target distance. With feedback, however, the same subjects quickly adapted their responses to produce 100 nearly unbiased performance (Fig 1F - purple, see Fig S1D for individual trials; mean slope \pm standard 101 deviation, radial distance: 0.95 ± 0.1 , angle: 1.15 ± 0.2). Notably, this improvement in performance was 102



Figure 1. Primates can navigate by integrating optic flow. A. Monkeys and human subjects use a joystick to navigate to a cued target (yellow disc) using optic flow cues generated by ground plane elements (brown triangles). The ground plane elements appeared transiently at random orientations to ensure that they cannot serve as spatial or angular landmarks (Methods). B. The time-course of linear (top) and angular (bottom) velocities during one example trial. Yellow shaded region corresponds to the time period when the target was visible on the screen. Time is also coded by color. C. Example trials showing incorrect (*left*) and correct (*right*) responses of a monkey. Note that subjects had to stop within the reward window (0.6m for monkeys; adaptive window for humans, see Methods) to receive reward. D. Left: Overhead view of the spatial distribution of target positions across trials. Positions were uniformly distributed within subjects' field of view. The actual range of target distances and angles was slightly larger for human subjects (Methods). Middle: Movement trajectories of one monkey during a representative subset of trials. Orange dot denotes starting location. *Right*: First-person view of the trajectories of eye movements (average of the two eyes) during the same trials. Abscissa and ordinate show horizontal version and elevation of the eyes respectively. Orange dots represent the initial eye position (when the target was turned OFF) on each trial. E. Left: Comparison of the radial distance of the monkey's response (stopping location) against radial distance of the target across all trials. *Right*: Angular eccentricity of the response vs target angle. Black dashed lines have unity slope (unbiased performance). The subject's starting location was taken as the origin. F. Subjects' multiplicative biases in radial distance (top) and angular eccentricity (bottom) were quantified as the slopes of the corresponding linear regressions and plotted for individual monkeys (green) and human subjects (purple). Horizontal dashed lines denote the value of the slope that corresponds to unbiased behaviour. Error bars denote ± 1 SEM across trials. G. Left: The proportion of correct trials of one monkey for various values of hypothetical reward window size (black). Shuffled estimates are shown in gray. Right: ROC curves for all subjects, obtained by plotting their true proportion of correct trials (from unshuffled data) against the corresponding chance-level proportions (from shuffled data) for a range of reward windows. Shaded area denotes standard deviation across subjects. Inset shows the average area under the curve (AUC) for monkeys (green) and human subjects (purple). See also Figure S1.

maintained in a final block of trials in which feedback was withheld (**Fig S1E-F**; radial distance: $1.03 \pm$

104 0.15, angle: 1.2 ± 0.2) suggesting that learning of this task was stable. To maintain consistency with 105 monkey data, we only consider human subjects' data collected during the block of trials with feedback in the 106 remainder of this work.

We wanted to know whether humans and monkeys had comparable accuracies. Because we used a slightly 107 larger range of target distances for humans (see **Methods**), we could not directly compare the mean error 108 magnitude of the subjects as it does not take differences in task difficulty into account. Instead, we used an 109 approach that is conceptually similar to receiver operating characteristic (ROC) analysis to objectively 110 compare the performance of monkeys and human subjects on a common scale. For each subject, we 111 constructed a 'psychometric function' of performance as a function of hypothetical reward window size (Fig 112 1G; see Methods). By plotting the true psychometric function against one obtained by shuffling target 113 locations across trials, we obtain the subject's ROC curve. Chance-level performance would correspond to 114 an area under the ROC curve (AUC) of 0.5, while perfectly accurate responses (zero error) will yield an 115 AUC of one. The AUCs for both monkey and human subjects were quite large and statistically 116 indistinguishable (mean + standard deviation, monkeys: 0.85 + 0.03, humans: 0.84 + 0.05; t-test: p =117 0.41) suggesting that they performed comparably. We emphasize that the individual visual elements 118 comprising the ground plane were transient and could not be used as landmarks, so the performance of 119 monkeys and human subjects in this task reflects their ability to integrate optic flow, rather than their ability 120 to visually track a ground plane element. 121

122 **Pattern of eve movements**

To understand the role of eve movements, we recorded the position of the subjects' eves while they 123 performed the task. Figure 2A shows the vertical and horizontal eye positions of one monkey during an 124 example trial. On this trial, we noticed saccades (eve movements exceeding 200°/s) before the target was 125 turned off (henceforth called *start* of the trial) and around the time when the monkey stopped moving (*end* 126 of steering), but not in-between. This pattern of saccade timing was evident across trials, as seen in the trial-127 averaged density of saccades (Fig 2B). Across all datasets from monkeys, the average frequency of saccades 128 during the trial was significantly smaller than that during the inter-trial interval (mean saccade rate \pm 129 standard deviation, during trials: 0.5 ± 0.3 Hz, between trials: 0.9 ± 0.5 Hz; paired *t*-test: p = 0.02). We 130 noticed a similar tendency among human subjects although the comparison was not statistically significant 131 (Fig S2A; during trials: 0.8 + 0.5 Hz, between trials: 1.4 + 1 Hz; p = 0.11). This suggests that subjects 132 actively suppressed saccadic eve movements while steering. Moreover, the velocity of eve movements 133 during steering was generally low, with magnitudes well below 20°/s both in monkeys (Fig 2C; mean \pm std.: 134 16.2 ± 2.1 °/s) and in humans (**Fig S2B**: 11.4 ± 3.2 °/s). 135

Because saccades were mostly confined to periods when the animal was not actively steering and subjects appeared to make slowly-varying eye movements while steering, we reasoned that they may be 'tracking' the (invisible) target with their eyes while they navigated to it. Note that as one steers towards the target location, the target would become progressively less eccentric and move downward in the visual field. Therefore, if subjects were to track the target, the magnitude of lateral version would tend towards zero and the eye elevation would become more negative with time (**Fig S3A**).

To quantitatively test whether subjects were tracking the target, we first generated ground truth theoretical predictions for the binocular position of their eyes during each trial, assuming that they maintained fixation at the center of the target throughout the trial (**Fig S3B**; **Methods** – **Equation 1**). We then compared this *prediction* against the *observed* eye position of the subject by expressing both quantities in terms of three standard components – lateral version, elevation and vergence (**Fig S3C**; see **Methods**).



Figure 2. Eye movement dynamics during the task. A. Time-course of vertical (top) and horizontal (bottom) positions of the left (*solid*) and right (*dashed*) eyes of a monkey during one example trial (in degrees). Yellow region shows the period when a target was visible on the screen. Red dashed line corresponds to the end of steering in this trial. **B.** The time-course of the rate of saccades during the trial, averaged across all trials separately for each of the three monkeys. Trial-averaging was done by aligning trials relative to target onset (*yellow region*, before break on the x-axis) and end of steering (*red dashed line*, following the break). Grey line denotes mean saccade rate across monkeys during the period between trials. **C.** Joint probability density of the distribution over horizontal and vertical eye velocities, averaged across monkeys, while they steered towards the target. Marginals are shown in black. **D.** Comparison of the two major components (lateral version and elevation) of predicted and true eye positions in a subset of trials for all monkeys at the moment when the target was just turned OFF. **E.** Time-course of the two components (lateral version and elevation) of eye positions during a random subset of trials taken from all monkeys. Blue and red dots denote the times at which the target was turned OFF and the end of steering, respectively. **F.** Target-tracking index (defined in text) when the target turned OFF for individual monkeys (*green*) and humans (*purple*). Error bars denote ± 1 SEM obtained either by averaging across recording sessions (for monkeys) or bootstrapping (for humans). **G.** Time-course of the target-tracking index, averaged across monkeys (*green*) and humans (*purple*). Grey arrow denotes the chance level tracking-index verified by shuffling procedure. Shaded region denotes ± 1 SEM across datasets. See also **Figures S2-S7**.

We expect subjects' eves to be drawn to the target when it appears on the screen. So, at the very least, the 149 theoretical predictions should be precise at trial onset. Indeed, the model predictions were highly correlated 150 with the measured values of lateral version (Fig 2D – *left* and Fig S4A – *left*; Pearson's $r \pm$ standard 151 deviation, monkeys: 0.91 + 0.1, humans: 0.85 + 0.1) as well as elevation (Fig 2D – right and Fig S4A – 152 *right*: monkeys: 0.60 + 0.2, humans: 0.42 + 0.2) at the beginning of the trial. The somewhat lower 153 correlations for the latter are understandable because it is difficult to precisely fixate at the elevations for 154 distant targets since they subtend a smaller visual angle. We verified this effect using simulations (Fig S5). 155 Next, we examined the time-course of eve movements during the trial and found a striking qualitative 156 correspondence to the predicted dynamics (Fig 2E, S4B): as the trial progressed, lateral version became 157 increasingly more concentrated around zero (Fig S4C – *left*) while eye elevation was significantly lower 158 (Fig S4C - *right*). The correlation between predicted and observed values remained significantly greater 159 than zero throughout the trial for both components (Fig S4D). This is quite remarkable because the target 160 appeared only transiently at the beginning of the trial. 161

On the other hand, the correspondence between predicted and observed vergence was less clear. Doing this 162 comparison for our task was challenging because about 90% of the full range of vergence angles is known to 163 occur within gaze distances below one meter (Howard, 2012) and the predicted change in vergence is 164 negligible for gaze distances beyond 2m (Fig S3C - *bottom right*). Only two of the three monkeys exhibited 165 vergence values that weakly correlated with the predictions at trial onset (Fig S6A) and a tendency to make 166 convergent eye movements as they approached the target (Fig S6B), an effect that was also absent in human 167 subjects (Fig S6B-D). It is possible that this inconsistency is due to the previously documented difficulty in 168 executing voluntary vergence movements to imagined moving targets (Erkelens et al., 1989). Moreover, this 169 difficulty is likely exacerbated in VR where vergence eye movements must be executed without changing 170 accommodation to maintain a clear retinal image of onscreen objects (Hoffman et al., 2008; Lambooij et al., 171 2009; Shibata et al., 2011). Therefore, we did not consider the vergence component for further analyses. 172

To quantify the extent to which a subject's eyes tracked the target, we expressed the eye position as a two-173 dimensional vector comprised of lateral version and elevation, and computed a *target-tracking index* that 174 measures how precisely the subjects' eves tracked the target. Specifically, this quantity was given by the 175 square root of the fraction of variance in the observed eye position that was explained by the prediction 176 (Methods – Equation 2). An index of one implies that the subject consistently looked at the center of the 177 target, while zero denotes lack of correspondence between target and gaze locations. The target-tracking 178 index was quite high at trial onset (during the first 500ms) when the target had just disappeared (Fig 2F; 179 mean + standard deviation, monkeys: 0.73 + 0.05, humans: 0.71 + 0.05). Although this slowly dropped 180 during the trial, the index at the end of the trial (during the last 500ms) remained well above zero (Fig 2G; 181 mean + standard deviation, monkeys: 0.35 + 0.1, humans: 0.18 + 0.05), implying that subjects tend to 182 maintain gaze at the target location while they steer towards it. Alternative measures comparing observed 183 eve positions to the predictions exhibited qualitatively similar dynamics, so the above result is robust to the 184 precise definition of the target-tracking index used here. 185

Cross-correlograms revealed that subjects' eye positions did not systematically lead or lag the predictions 186 based on the contemporaneous target location (Fig S7). This suggests that eye movements were not 187 predicting future target locations, although the computations used to estimate the target location could still 188 be predictive. We also found the amplitude of the vertical (but not horizontal) component of saccades during 189 steering was correlated with the prediction error at saccade onset (i.e., difference between predicted and 190 observed eye elevation; Pearson's $r \pm$ standard deviation, monkeys: 0.27 ± 0.3 , humans: 0.11 ± 0.2). This 191 suggests that vertical saccades made during steering were similar to "catch-up" saccades typically observed 192 during smooth pursuit of visible targets (Dave et al., 2014; Orban de Xivry et al., 2008). One potential 193 reason for the lower correlations than previous studies is that catch-up saccades are typically elicited by 194



Figure 3. Accurate target-tracking is associated with increased task performance. A. Time-course of the target-tracking index for an example session computed using a monkey's actual eye movements (black solid) and its theoretical upper-bound (black dashed) determined using variability in the monkey's behavioural response (Methods, equations 3-4). B. Left: Overhead view of the spatial map showing the standard deviation of stopping positions as a function of target location for individual monkeys and the average human subject. The maps of monkey S & O, and of the humans, have been rotated solely for visualization. All subjects shared the same range of target angles ($\pm 40^{\circ}$) and distances (up to 4m for monkeys, 6m for humans). Right: Comparison of the observed target-tracking index against the corresponding theoretical upper bound (averaged over the last 500ms of the trials) across all individual datasets. Trials from human subjects were pooled together (see text for explanation). Dashed line has unity slope and error bars denote ± 1 SEM obtained by bootstrapping. C. Top: Time-course of the target-tracking index for one example monkey shown separately for trials in which he stopped within the reward zone (0.6m from the target, *blue*), or stopped outside it (*red*). Shaded regions denote ± 1 standard error estimated by bootstrapping. *Bottom*: The difference between tracking coefficients during rewarded and unrewarded trials for all subjects (monkeys in green, humans in purple). For human subjects, trials in which the subject's final position was within 0.6m of the center of the target were considered 'rewarded' for the purpose of classification. D. Top: We divided trials into five groups depending on the magnitude of the subject's error *i.e.*, final (stopping) distance to the target. Time-courses of the target-tracking index are shown for the five trial groups for one monkey (dark blue: most accurate; dark red: least accurate). Bottom: Average value of the target-tracking index during the final 500ms before end of steering (brown shaded region in the top panel) as a function of percentile accuracy for all individual subjects. Solid lines show average across subjects. Across all subjects (humans and monkeys), there was a significant correlation between accuracy and tracking coefficient (Pearson's $r = 0.68, p = 3.1 \times 10^{-5}$). E. Top: Joint distribution of the behavioural error and the target-tracking error across trials of one recording session from one monkey. Bottom: The mean correlation between behavioural and target-tracking errors of individual monkeys before (green) and after (gray) a shuffling procedure to control for the effects of trial difficulty (see text). Error bar denotes ±1 SEM obtained by bootstrapping. See also Figure S9.

unexpected jumps in target velocity (de Brouwer et al., 2002), whereas motion in the task used in this study
was self-generated and predominantly smooth. This might also explain why saccadic eye movements during
steering were, in general, quite rare (Fig 2B). Therefore, we only focus on smooth eye movements in the
following sections.

199 Eyes convey internal beliefs about target

Subjects could not have possibly been tracking the observed target location, since the target disappeared at the beginning of the trial. A plausible explanation for their pattern of eye movements is that subjects tracked the location at which they *believed* the target was present. As they integrate their movements, subjects need to continuously update their internal estimate of the relative goal location, and perhaps their eye movements reveal those estimates. If this is the case, then we should be able to better predict their eye position when their beliefs are more accurate. We tested this both across subjects and across trials within each subject.

- To test this across subjects, we used the variability in subjects' stopping positions to first quantify the level of uncertainty in their position estimates (**Methods**). Due to the low trial count of individual human subjects, we pooled trials from all humans into a single dataset. Because uncertainty in knowing one's location should
- 209 limit one's ability to visually track the target, we used the estimated uncertainties to calculate an
- approximate *upper bound* on the target-tracking index for each dataset (**Fig 3A**, **Methods equations 3**).
- 211 This upper bound serves to capture the heterogeneity in the spatial profile of uncertainty both across subjects
- 212 (Fig 3B left) and across sessions within each monkey (Fig S9A). Across all datasets, the target-tracking 213 index observed towards the end of the trial (during the last 500ms) was weakly but significantly correlated
- index observed towards the end of the trial (during the last 500ms) was weakly but significantly correlat with the theoretical upper bounds (**Fig 3B** – *right*; Pearson's r = 0.26, p = 0.029). This suggests that
- differences in the ability to track the target with the eyes is due, at least in part, to differences in the
- 216 magnitudes of positional uncertainty between subjects.

We also tested whether eye movements reflect fluctuations in the subject's belief about their location across 217 trials. Because subjects were more precise during rewarded (Fig S9B - left) than during unrewarded trials 218 (Fig S9B – *middle*), we expect subjects to track the target more accurately during rewarded trials (Fig S9B – 219 *right*). We computed the target-tracking index separately for the two groups of trials and found that it was 220 indeed higher during rewarded trials (Fig 3C - top). The difference between the target-tracking indices 221 during the two sets of trials grew as the trial progressed, and was significantly greater than zero at the end of 222 the trial (Fig 3C - bottom; mean difference \pm standard deviation during the period shaded in grey – 223 monkeys: 0.19 ± 0.05 , $p = 4.8 \times 10^{-3}$; humans: 0.13 ± 0.05 , $p = 3.1 \times 10^{-2}$; bootstrap test, 10,000 224 bootstrap samples). In fact, when trials were stratified based on behavioural accuracy, we found that the 225 tracking index increased with behavioural accuracy (Fig 3D). To more directly test whether there was a fine-226 grained relationship between eve movements and task performance, we estimated the correlation between 227 the behavioural error (distance between the stopping location and the target) and the target-tracking error 228 (mean absolute difference between the actual eye position and the theoretical prediction, see **Methods**) 229 across trials (Fig 3E - top). To control for possible spurious effects of trial difficulty, we computed a 230 shuffled estimate by subdividing the trials into groups based on initial target distance and then shuffling the 231 trials within each group (see Methods). We found that the behavioural and target-tracking errors were 232 significantly correlated across trials (Fig 3E - bottom, Pearson's $r \pm$ standard deviation across all datasets – 233 true: 0.14 + 0.04, controlled shuffle: 0.04 + 0.02; $p = 9.1 \times 10^{-3}$, paired *t*-test) further reinforcing the 234 view that subjects are tracking their internally estimated goal location with their eyes. 235

236 Purely reflexive eye movements do not explain target-tracking behaviour

In principle, the above results could also be produced by purely reflexive eye movements, driven solely by optic flow (ocular following response or OFR). For instance, if subjects' eye velocity is perfectly correlated with their perceived movement velocity, then oculomotor errors would be proportional to perceptual errors.

240 potentially explaining the relatively poor target-tracking in erroneous trials. However, past studies have

shown that errors in reflexive eye movements are uncorrelated with perceptual errors (Blum and Price, 2014;
Boström and Warzecha, 2010; Glasser and Tadin, 2014; Price and Blum, 2014) suggesting that the observed
eye movements may not be entirely reflexive. Two further pieces of evidence in our own monkey data
support this.

First, in a subset of sessions we recorded the stimulus movie of the complete block of trials and replayed 245 them back to the animal at the end of the session, but with the joystick withheld (see **Methods**). All aspects 246 of the task structure during this replay block were identical to the initial block of trials (e.g. the monkey still 247 received juice reward at the end of the corresponding trials), except the animal only viewed a movie of the 248 stimulus rather than actively performing the task. Importantly, monkeys were still free to move their eyes. In 249 general, eve movements were weaker during passive viewing than during active task (Fig S10A, B). Across 250 monkeys, the magnitude of eye velocity was much smaller during passive block even though both blocks 251 had identical visual stimuli (**Fig S10C**). We analysed the target tracking behaviour by computing the target-252 tracking index separately for the two blocks of trials. Figure 4A (top panel) shows the time-course of the 253 target-tracking index of one monkey during the both blocks of trials. In this monkey, the tracking index was 254 much lower during passive viewing (red vs blue). Because OFR is, by definition, involuntary and difficult to 255 suppress, this suggests that eve movements contributing to the high target-tracking index during active 256 steering must have been voluntary. Note however that the tracking index during passive viewing is poor 257 right from trial onset, perhaps because the monkey did not consistently look at the target initially when it 258 appeared on the screen. We wanted to know whether OFR dynamics, coupled with the appropriate boundary 259 condition (looking at the target when it initially appears) might be sufficient to give the impression that the 260 animal is tracking the target. We simulated this model by shifting the initial eve position on each trial of the 261 passive block to match the corresponding trial in the active block, a procedure that left the eye movement 262 dynamics unaltered (Fig 4A - black). The tracking index of this simulated model was substantially lower 263 than that observed during the active block of trials, suggesting that the target-tracking behaviour is likely to 264



Figure 4. Steering-induced eye movements are not reflexive. A. Top: Time-course of target-tracking index for one monkey during trials in which he performed the task (*blue*) or passively viewed the stimulus identical to the one generated when performing the task (red). Black trace shows the tracking index of an OFR model simulated by translating the initial eye position on each passive trial to match the corresponding active trial (see text). Tracking indices at time points with negative variance explained were clipped to zero. Bottom: The time-course of the cumulative difference between the targettracking index on active trials and the simulated OFR model for individual monkeys. B. Top: Time-course of the tracking index of one monkey during trials in which the density of ground plane elements was either high (*blue*) or low (*red*). *Bottom*: The difference between target-tracking index under high and low density conditions for individual monkeys. Brown shaded regions in the bottom panels correspond to the 500ms time-window considered for statistical testing. See also Figure S10.

- be a voluntary response. In all three monkeys, the target tracking during the active task was significantly stronger than during either the passive viewing condition or the OFR model (**Fig 4A** – *bottom*; mean difference \pm standard deviation during the period shaded in brown, active: 0.27 ± 0.1 , passive: 0.08 ± 0.1 , OFR model: 0.07 ± 0.1 ; p < 0.01, bootstrap test). The difference between conditions was small in one monkey (labelled 'Q' in **Fig 4A** – bottom; **Fig S10** – rightmost), possibly because this animal was mentally performing the task even during passive viewing.
- Second, OFR is known to be sensitive to signal strength (Barthelemy et al., 2009; Quaia et al., 2012). To test whether target tracking depends on signal strength, we manipulated stimulus reliability by randomly interleaving trials with two different densities of ground plane elements by more than an order of magnitude (see **Methods**). We analysed the two sets of trials separately, but found no significant difference between the target-tracking index (**Fig 4B**; mean \pm standard deviation across subjects, low density: 0.28 ± 0.1 , high density: 0.31 ± 0.1). Therefore, the pattern of eye movements observed during this task likely represent volitional movements, rather than reflexive ones.

279 Inhibiting eye movements worsens task performance

Since eye movements were predictive of subjects' navigational performance, we wanted to know if they were essential for performing the task. To test this, we asked five human subjects to perform a variation of the task in which we overlaid a cross on top of the target location and instructed them to fixate on this cross for as long as it appeared on the screen. In half the trials ('Eyes-moving' condition), the fixation cross disappeared along with the target so that subjects were free to produce eye movements as before. In the



Figure 5. Fixation affects task performance. A. Trial- averaged temporal variability of subjects' eye position, quantified by standard deviation (see **Methods**) during 'Eyes-moving' (*blue*) and 'Eyes-fixed' (*red*) trials. Error bars denote standard deviation across subjects (** $p = 1.2 \times 10^{-3}$, paired *t*-test). **B.** ROC curves averaged across subjects, for trials in the 'Eyes-moving' (*blue*) and the 'Eyes-fixed' condition (*red*). Inset shows the area under the two curves. Error bars denote standard deviation across subjects (* $p = 2.5 \times 10^{-3}$, paired *t*-test). **C.** *Top*: Comparison of the radial distances of the response and the target on trials in 'Eyes-moving' (*blue*) 'Eyes-fixed' (*red*) conditions. Different symbols denote different human subjects. *Bottom*: Comparison of the (absolute) angular eccentricity of the response and target under the same two conditions. **D.** *Top*: Pearson's correlation coefficient between the radial distance of subjects' response and the target under 'Eyes-moving' (*blue*) and 'Eyes-fixed' (*red*) for all individual subjects. *Bottom*: Similar comparison for the absolute angular eccentricity of target and response under the two conditions. See also **Figure S11**.

remaining trials ('Eyes-fixed' condition), the cross remained at the same location on the screen throughout 285 the trial and subjects had to perform the task without moving their eyes (see **Methods**). Although we did not 286 penalize subjects for breaking fixation, we verified offline that they maintained fixation as instructed (Fig 287 5A and Fig S11). We assessed their behavioural performance by comparing the area under the ROC curve 288 (AUC), and found that performance was significantly impaired in the 'Eyes-fixed' condition (Fig 5B; n = 5289 humans, mean AUC \pm standard deviation; Eyes-moving: 0.85 \pm 0.07, Eyes-fixed: 0.77 \pm 0.07, $p = 2.5 \times$ 290 10^{-3} , paired *t*-test). Figure 5C shows the responses of individual subjects. Although subjects were nearly 291 unbiased under both conditions, the correlation between target and response locations was significantly 292 lower in the absence of eye movements (Fig 5D; mean + standard deviation; $Corr(r, r^*)$, Eyes-moving: 293 0.71 ± 0.1 , Eyes-fixed: 0.49 ± 0.2 , p = 0.011, paired *t*-test; Corr($|\theta|$, $|\theta^*|$), Eyes-moving: 0.92 ± 0.03 , 294 Eves-fixed: 0.82+0.1, p = 0.035). These results suggest that subjects benefit when their eves can track the 295 internally estimated goal location in this task. 296

297 **DISCUSSION**

Using a virtual visuomotor navigation task that requires continuous integration of optic flow cues, we 298 showed that humans and monkeys execute slow eye movements while steering. By comparing these eye 299 movements against predictions for an agent that maintained fixation at the target, we demonstrated that 300 subjects likely tracked the imagined target location while steering towards it. Although subjects' tracking 301 index remained significantly above chance throughout the trial, it nonetheless decreased over time. This is 302 expected because the target disappears, so subjects cannot directly measure its true position but must instead 303 rely on an internal estimate computed by integrating optic flow. We have previously shown that human 304 305 subjects perform near-perfect integration in this task (Lakshminarasimhan et al., 2018). Nevertheless, due to noise in the integration process, the error in the internal estimate of target location on any given trial should 306 grow over time. Consequently, even if those estimates are unbiased, their precision worsens, leading to a 307 decrease in the target-tracking index (Fig 3A – dashed line). Therefore, the observed decrease in the tracking 308 index is an inevitable consequence of noisy observations and noisy integration. 309

310 The nature of eye movements

While steering towards the target, subjects executed slow eye movements, and tended to suppress saccades. 311 The latter is consistent with recent physiological and behavioural experiments that demonstrate that saccades 312 have a detrimental effect on both self-motion perception (Bremmer et al., 2017) and the ability to localize 313 targets in space (Klingenhoefer and Krekelberg, 2017). To understand the nature of these slow eve 314 movements, we analyzed three separate components of eve position: lateral version, elevation, and vergence. 315 In all subjects, the dynamics of the first two components were smooth and consistent with the predicted 316 dynamics for pursuing the invisible target. In contrast, only two of the three monkeys made convergent eve 317 movements as they approached the target location. Vergence eve movements also did not show clear 318 dependence on the target location in human subjects. Under natural conditions, vergence eye movements are 319 typically evoked either by binocular disparity or by a need to accommodate to blurred visual stimuli 320 (Horwood and Riddell, 2008; Howard, 2012). Accordingly, vergence responses to imagined targets are 321 unreliable (Erkelens et al., 1989). Moreover, accommodation demands are somewhat unnatural in VR 322 because objects on the screen all share the same focal length. In light of these limitations, it is not very 323 surprising that we were unable to measure vergence eye movements that varied systematically with target 324 position in all subjects. 325

By analyzing eye movements during stimulus playback, we ruled out the possibility that the smooth
dynamics correspond to pure ocular following reflex (OFR) induced by optic flow. Because these eye
movements were always preceded by fixating a visible target and occurred in parallel with computations for
mentally tracking that same target, they are functionally more similar to smooth-pursuit eye movements.
Despite ample evidence for smooth-pursuit eye movements in the absence of foveal stimulation in humans

(Becker and Fuchs, 1985; Missal and Heinen, 2017; Wyatt et al., 1994) and rhesus macaques (Ilg and Thier, 331 1999), smoothly tracking a purely imaginary object is thought to be difficult (Spering and Montagnini, 332 2011). This is because, in the absence of dynamic information about target motion, the pursuit velocity 333 gradually decays to zero (Barnes, 2008; Missal and Heinen, 2017). However, when the underlying model for 334 target motion is known, subjects can use their dynamic internal representation of the target to make 335 predictive smooth pursuit during target blanking (Adams et al., 2012; Orban de Xivry et al., 2013, 2008). In 336 our task, the dynamics of optic flow completely determine the (relative) motion of the target and can 337 subsequently drive eve movements. Furthermore, the flow fields were self-generated rather than simulated, a 338 condition that has previously been shown to improve pursuit of occluded targets (Danion et al., 2017; 339 Gauthier et al., 1988; Vercher and Gauthier, 1992). Finally, we note that a moderate contribution of OFR 340 induced by optic flow cannot be completely excluded, so it is possible that the pattern of eye movements 341 reported here is ultimately composed of a mixture of reflexive signals that encode velocity of self-motion 342 and predictive signals that encode the internal estimate of relative target location. 343

344 Possible function of tracking eye movements

The experimental task was specifically designed to ensure that subjects would attempt to *mentally* track the 345 goal location by integrating momentary sensory evidence about movement provided by optic flow. In 346 principle, this can be accomplished without *physically* tracking the believed goal location with one's eyes. 347 Yet we noticed a significant decline in task performance when eve movements were suppressed. This is 348 consistent with previous results that demonstrated that real-world driving performance is impaired when eve 349 movements are constrained (Wilson et al., 2008). Although this does not demonstrate a need to make 350 tracking eye movements, it suggests that eye movements play an important role in neural computations for 351 navigation. Indirect evidence of a role for slow eye movements in visually-guided navigation comes from a 352 recent study of path integration, in which subjects used a joystick to reproduce previously-experienced self-353 motion (Churan et al., 2018). Eye movements during the reproduction phase were similar to those during 354 initial exposure even when optic flow was removed. This suggested that eve movements constitute a form of 355 mental imagery that, if suppressed, hampered memory retrieval (Johansson and Johansson, 2014; Johansson 356 et al., 2012). Our findings extend this to naturalistic settings and argue that eve movements have a more 357 dynamic role in path integration. The precise computational advantage of the specific eve movement 358 dynamics observed in our task is unclear. Below, we propose two potential theories. 359

One possibility is that eve movements directed towards the intended goal location stabilizes the mental 360 image of the goal, and could reduce the computational complexity of estimating self-motion from optic flow 361 similar to the effect of foveal image stabilization (Lappe et al., 1999; Longuet-Higgins and Prazdny, 1980; 362 Perrone and Stone, 1994; Sandini and Tistarelli, 1990; Sandini et al., 1986). Normative mathematical 363 theories posit that maintaining gaze at a point on the intended path can greatly simplify the problem of 364 exploiting optic flow (Glennerster et al., 2001; Kim and Turvey, 1999; Wann and Swapp, 2000). Therefore, 365 the eve movements reported here may constitute a closed-loop visuomotor process in which subjects 366 integrate sense data (optic flow) to dynamically update their beliefs about the relative goal location, and in 367 turn, use them to guide future eve movements in order to acquire new sense data in a computationally useful 368 format. In this view, eye movements primarily aid optic flow processing. 369

Alternatively, the observed eye movements might simply be an embodiment of subjects' dynamically evolving internal beliefs about the goal. Humans have a well-documented tendency for externalizing their internal representations (Barsalou, 2008; Spivey, 2007), with eye movements sometimes employed as a pointing device to visible as well as invisible objects, much like one's index finger (Ballard et al., 1995, 1997; Spivey and Geng, 2001). By allowing dynamic beliefs about the relative target location to continuously modulate eye movements in this task, the brain could piggyback on the oculomotor circuit and reduce the computational burden on working memory. Consistent with this interpretation, there is

- overwhelming evidence for decision-related responses in primate oculomotor brain areas (de Lafuente et al.,
- 2015; Shadlen and Newsome, 1996), and such responses are thought to drive eye movements (Joo et al.,
- 2016). Therefore, in this view, primates use gaze as an affordance to efficiently update and store the output
- 380 of integrating optic flow.
- Although the above accounts are not mutually exclusive, simultaneously recording the neural activity from
- the primate sensory, oculomotor, and decision areas during this task might shed light on the dominant role of
- eye movements and how they link perception and action. Either way, regardless of the mechanism
- underlying these eye movements, the paradigm used here offers a useful approach to directly readout
- dynamical internal beliefs in real-time, simply by tracking subjects' eyes.

386 **METHODS**

387 **Subjects**

Three rhesus macaques (all male, 7-8 yrs. old) and ten human subjects (six males, all adults in the age group 18-32 yrs.) participated in the experiments. All but one subject were unaware of the purpose of the study.

- All surgeries and experimental procedures were approved by the Institutional Review Board at Baylor
- College of Medicine, and were in accordance with National Institutes of Health guidelines. All human
- subjects signed an approved consent form. In the following sections, the term subject is used to denote both
- 393 monkey and human subjects, unless specified otherwise or implied by the context.

394 **Experimental setup**

Monkeys were chronically implanted with a lightweight polyacetal ring for head restraint, and scleral coils
for monitoring eye movements (CNC Engineering, Seattle WA, USA). At the beginning of each
experimental session, monkeys were head-fixed and secured in a primate chair placed on top of a platform
(Kollmorgen, Radford, VA, USA). A 3-chip DLP projector (Christie Digital Mirage 2000, Cypress, CA,
USA) was mounted on top of the platform and rear-projected images onto a 60 x 60 cm tangent screen that
was attached to the front of the field coil frame, ~30cm in front of the monkey. The projector was capable of
rendering stereoscopic images generated by an OpenGL accelerator board (Nvidia Quadro FX 3000G).

Human subjects wore a custom-fit thermoplastic mask (CIVCO Medical Solutions) that was screwed to the back of the chair to restrain their head. The mask was mounted with a binocular eye tracker (ISCAN Inc.) to record the position of the subjects' pupils at 60Hz. All other aspects of the setup were similar to the one used for monkeys, but with subjects seated 67.5cm in front of a 149×127 cm² (width × height) rectangular screen. Although humans and monkeys were head-fixed, they were both free to move their eyes when performing the task, except under one experimental manipulation in humans (noted towards the end of the section below).

409 **Behavioural Task**

Subjects used an analog joystick (M20U9T-N82, CTI electronics) with two degrees of freedom and a 410 circular displacement boundary to control their linear and angular speeds in a virtual environment. This 411 virtual world comprised a ground plane whose textural elements had limited lifetime (~250ms) to avoid 412 serving as landmarks. The ground plane was circular with a radius of 70m (near and far clipping planes at 413 5cm and 4000cm respectively), with the subject positioned at its center at the beginning of each trial. Each 414 texture element was an isosceles triangle (base \times height: 8.5 \times 18.5 cm²) that was randomly repositioned 415 and reoriented anywhere in the arena at the end of its lifetime, making it impossible to use as a landmark. 416 The maximum linear and angular speeds were fixed to $v_{max} = 2ms^{-1}$ and $\omega_{max} = 90^{\circ}/s$ respectively, and 417 the density of the ground plane was either held fixed at $\rho = 2.5$ elements/m² or varied randomly between 418 two values ($\rho = 2.5$ elements/m² and $\rho = 0.1$ elements/m²) in a subset of recording sessions (see 419 below). The stimulus was rendered as a red-green anaglyph and projected onto the screen in front of the 420 subject's eyes. Subjects wore goggles fitted with Kodak Wratten filters (red #29 and green #61) to view the 421 stimulus. The binocular crosstalk for the green and red channels was 1.7% and 2.3% respectively. 422

Human subjects pressed a button on the joystick to initiate each trial, and the task was to steer to a random target location that was cued briefly at the beginning of the trial (**Fig 1A**). Monkeys performed the same task, but each trial was programmed to start after a variable random delay (0.5 - 1.1s) following the end of the previous trial. The target was a circular disc of radius 20cm whose luminance was matched to the texture elements. It appeared at a random location between $\theta = \pm 40^{\circ}$ of visual angle at a distance of r = 0.7 - 4m(up to 6m for human subjects) relative the subject at the beginning of the trial. For human subjects, the target disappeared after one second, which was a cue for the subject to start steering, and the joystick

- 430 controller was activated. In the case of monkeys, the target only appeared on the screen for 300ms, and the431 joystick was always active.
- Monkeys typically performed two blocks of ~750 trials in each experimental session, and received feedback 432 at the end of each trial. Monkeys performed a total of ~6,000 trials (4 sessions) each. Eve tracking was 433 performed either using scleral coils (monkey Q & B) or a head-mounted eye tracker (monkey S). In one of 434 the above recording sessions in each monkey, we saved the stimulus movie and replayed them to the animal 435 at the end of the block. Both the visual stimulus and the schedule of rewards during this replay block were 436 identical to the active navigation block, with the only difference being that the joystick was withheld and 437 monkeys passively viewed the stimulus. Furthermore, a subset of the recording sessions (two sessions in 438 each monkey) contained two randomly interleaved sets of trials that differed in terms of the density of optic 439 flow ($\rho = 0.1$ elements/m² and $\rho = 2.5$ elements/m²). 440
- Of the ten human subjects, five subjects performed a total of 600 trials spread equally across three blocks. 441 The blocks were identical in all respects, except no feedback was provided at the end of the trials in the first 442 and third blocks. The purpose of using this block structure was to study how feedback affected learning in 443 humans. Although data collected in the absence of feedback (first and last blocks) are briefly described in 444 Fig. S1, the key results of the paper are based only on data collected during the intermittent block with 445 feedback. Furthermore, during the block with feedback, the performance of human subjects typically 446 stabilized within fifty trials (Fig. S1B). Because we wanted to ensure that the performance was stable during 447 the course of testing, we ignored the first fifty trials of this block for all our analysis (Figs 1-3). The 448 remaining five human subjects participated in a version of the experiment that was designed to study the 449 effect of inhibiting eye movements on task performance (Fig 5). These subjects first performed a block of 450 fifty trials with feedback to allow their performance to stabilize. Following this pre-training block, they 451 performed a test block comprising 400 trials of a version of this task in which a fixation cross was overlaid 452 on top of the target in each trial, again with feedback. In a random subset of trials (50%), this fixation cross 453 remained on the screen even after the target disappeared and subjects were instructed to maintain fixation on 454 the cross while steering to the target. The location of the cross remained fixed in screen coordinates and thus 455 carried no dynamic information about stimulus location. 456

457 **Feedback**

Monkeys received binary feedback at the end of each trial. They received a drop of juice if, after stopping,
they were within 0.6m away from the center of the target. No juice was provided otherwise. The fixed
reward boundary of 0.6m was determined using a staircase procedure prior to the experiment to ensure that
monkeys received reward in approximately two-thirds of the trials.

Human subjects received a somewhat richer, adaptive feedback in the form of a bullseve pattern that 462 appeared on the ground at the end of steering. The bullseve was centered on the target, with the innermost 463 region having the highest luminance. The pattern comprised of five zones (Fig S1A), and the radii of the 464 rings were continuously scaled (up or down by 5%) during the experiment using a 1-up 2-down staircase 465 procedure. Additionally, an arrowhead pointing to the target also appeared on the ground in front of the 466 subjects, colored green or red depending on whether the subject's stopping position was inside or outside the 467 reward boundary. The adaptive feedback procedure ensured that human subjects, like monkeys, stopped 468 within the reward boundary in roughly two-thirds of the trials. Unlike monkeys, human subjects did not 469 receive juice at the end of each successful trial, but instead received monetary compensation that was 470 471 commensurate with their performance.

472 **Stimulus and Data acquisition**

- 473 All stimuli were generated and rendered using C++ Open Graphics Library (OpenGL) by continuously
- repositioning the camera based on joystick inputs to update the visual scene at 60 Hz. The camera was

positioned at a height of 1m above the ground plane (10cm for monkeys). Spike2 software (Power 1401

476 MkII data acquisition system from Cambridge Electronic Design Ltd.) was used to record and store the

target location (r^*, θ^*) , subject's position (r, θ) , horizontal positions of left and right eyes $(\alpha_l \text{ and } \alpha_r)$,

vertical eye positions (β_l and β_r) and all event markers for offline analysis at a sampling rate of 833 $\frac{1}{3}$ Hz.

479 Model predicted eye position

To test whether subjects' eyes tracked the location of the (invisible) target, we generated predictions for subjects' instantaneous eye positions by assuming that they maintained fixation at the center of the target. (x_t, y_t, z_t) denotes the location of the target relative to the mid-point of the subject's eyes at time *t*. The *mean* predicted lateral displacement (relative to fixating at the point $(0, \infty, 0)$) of the left and right eyes $(\hat{\alpha}_l$ and $\hat{\alpha}_r)$ are geometrically related to the target location and the inter-ocular distance (2Δ) as (**Figs S3B**):

$$\bar{\hat{\alpha}}_l(t) = \tan^{-1}\left(\frac{x_t + \Delta}{\sqrt{y_t^2 + z_t^2}}\right) \quad ; \quad \bar{\hat{\alpha}}_r(t) = \tan^{-1}\left(\frac{x_t - \Delta}{\sqrt{y_t^2 + z_t^2}}\right) \tag{1.1}$$

485 Likewise, the vertical displacement of the two eyes $(\bar{\beta}_l \text{ and } \bar{\beta}_r)$ should be:

$$\bar{\hat{\beta}}_{l}(t) = \tan^{-1} \left(\frac{z_{t}}{\sqrt{y_{t}^{2} + (x_{t} + \Delta)^{2}}} \right) \quad ; \quad \bar{\hat{\beta}}_{l}(t) = \tan^{-1} \left(\frac{z_{t}}{\sqrt{y_{t}^{2} + (x_{t} - \Delta)^{2}}} \right) \tag{1.2}$$

Note that z_t is determined entirely by the camera height and hence time-invariant. In contrast, x_t and y_t change continuously as the subject steers to the target, and are both equal to zero in the special case when the subject's location coincides with the center of the target. The predicted eye positions also have *variances* associated with them, which we derive in a later section (**equation 4**).

490 Data Analysis

Customised MATLAB code was written to analyse data and to fit models. Depending on the quantity estimated, we report statistical dispersions either using 95% confidence interval, standard deviation, or standard error in the mean. The specific dispersion measure is identified in the portion of the text accompanying the estimates. For error bars in figures, we provide this information in the caption of the corresponding figure. We report exact *p*-values for all statistical tests, and describe the outcome as significant if p < 0.05.

497 **Bias estimation**

We regressed (with an intercept term) each subject's response positions (r, θ) against target positions (r^*, θ^*) separately for the radial ($r vs r^*$) and angular ($\theta vs \theta^*$) co-ordinates, and the radial and angular multiplicative biases were quantified as the slope of the respective regressions (**Fig 1F**). The intercept terms of the regression models denote additive bias. For each subject, we estimated the 95% confidence intervals for the biases by bootstrapping.

503 **Psychometric analysis**

As described in the section on feedback, reward boundaries were chosen to ensure that all subjects correctly stopped within the reward zone in about two-thirds of the trials. However, the precise radius of these boundaries varied across human subjects, as well as between humans and monkeys. To objectively compare the performance of different subjects on a common scale, we performed ROC analysis as follows. For each subject, we first constructed a psychometric function by calculating the proportion of correct trials as a function of (hypothetical) reward boundary (**Fig 1G**). In keeping with the range of target distances used for the two species, we varied the reward boundary between 0–4m for monkeys and 0–6m for human subjects.

511 Whereas an infinitesimally small boundary will result in all trials being classified as incorrect, a large

enough reward boundary will yield near-perfect accuracy. To define a chance-level psychometric function,

513 we repeated the above procedure but now by shuffling the target locations across trials, thereby destroying

the relationship between target and response locations. Finally, we obtained the ROC curve by plotting the

proportion of correct trials in the original dataset (true positives) against the shuffled dataset (false positives)
for each value of hypothetical reward boundary. We used the area under this ROC curve to obtain an

517 accuracy measure that was independent of the reward boundary used for various subject.

518 Characterizing eye position

For convenience, we express the subject's actual eye position using the following three standard degrees of 519 freedom: (i) Conjunctive horizontal movement of the two eyes or 'lateral version' quantified here as the 520 mean lateral position of the two eyes, $\alpha = (\alpha_l + \alpha_r)/2$, (ii) Conjunctive vertical movement of the two eyes 521 or 'elevation' quantified here as $\beta = (\beta_l + \beta_r)/2$, (*iii*) Disjunctive horizontal eye movements or 'vergence' 522 quantified here as $\gamma = (\alpha_l - \alpha_r)/2$. Disjunctive eye movements along the vertical direction (vertical 523 524 vergence) were an order of magnitude smaller than the precision of our measurements, and therefore we ignore them in all our analyses. We also transformed the *predicted* eye positions given by **Equation 1** 525 into the above three degrees of freedom using analogous definitions to obtain $\overline{\hat{\alpha}}$, $\overline{\hat{\beta}}$, and $\overline{\hat{\gamma}}$. 526

527 Saccade detection and pre-processing

We estimated the instantaneous speed of eye movements as $(\dot{\alpha}^2 + \dot{\beta}^2)^{1/2}$ where α and β denote lateral 528 version and elevation respectively (as defined above), and a dot denotes a time derivative. Saccades were 529 detected by identifying the time points at which the speed of eve movements crossed a threshold of 200% 530 from below (a threshold of 50% yielded similar results). Although saccades were mostly confined to periods 531 immediately following target onset and end of steering (Fig 2B), we removed a period of 100ms 532 immediately following the onset of saccades for visualizing the time-course of eye movements during the 533 trial (Fig 2E) and for all subsequent temporal analyses described below. We verified that this procedure had 534 minimal effect on the results. In approximately 10% of the trials in monkeys and ~30% in human subjects, 535 the subject travelled beyond the target. The predicted eye positions towards the end of these trials were 536 outside the range that was physically possible. Therefore, we removed time points at which any of the four 537 predicted components of eye movements in Equation 1 exceeded 60° before further analysis. Such time 538 points constituted less than 3% of the dataset, and including them did not qualitatively alter the results. 539

540 Comparing predicted and observed eye positions

Let $\boldsymbol{\varphi}_t = (\alpha_t, \beta_t)$ and $\overline{\boldsymbol{\varphi}}_t = (\overline{\alpha}_t, \overline{\beta}_t)$ denote the observed and mean predicted eye positions respectively at time *t*. For each subject, we computed the square root of the fraction of variance in their eye movements explained by the predictions:

$$\rho_t = \sqrt{1 - \frac{\langle \left\| \boldsymbol{\varphi}_t - \overline{\boldsymbol{\hat{\varphi}}}_t \right\|_2^2 \rangle}{\langle \left\| \boldsymbol{\varphi}_t - \overline{\boldsymbol{\varphi}}_t \right\|_2^2 \rangle}}$$
(2)

where $\|\cdot\|_2$ denotes the L_2 norm, $\langle \cdot \rangle$ denotes expectation across trials, and $\overline{\mathbf{\phi}}_t$ denotes the mean observed eye 544 position across trials at time t. Because the predictions are based on a model that assumes subjects' eyes 545 track the center of the target, we call ρ the '*target-tracking index*', or simply '*tracking-index*'. A value of 1 546 corresponds to perfect prediction while zero implies that the predictions were no better than the mean 547 observation. In principle, the deviation from the predictions can be larger than the intrinsic variability of the 548 data. We clipped the target-tracking index to zero whenever this happened. Since trial durations were 549 variable, we aligned all trials relative to the time at which the target was turned off (t = 0) to estimate the 550 time course of tracking coefficient $\rho_t^{\text{start}} \forall t \in [0, 1.8s]$. ρ_0^{start} corresponds to the similarity between 551 observed and predicted eye position at the moment when the target was turned off (Fig 2F). We also 552

computed the tracking coefficient by aligning trials with respect to the end of steering (t = T) to estimate $\rho_t^{\text{stop}} \forall t \in [-1.2\text{ s}, 0]$. To visualize the time-course of the tracking coefficient, we plot both ρ_t^{start} and ρ_t^{stop} with a break in the *x*-axis (**Fig 2G, 3 & 4**). To assess standard errors and statistical significance of differences between tracking coefficients from pairs of conditions (e.g. rewarded vs unrewarded trials), we used a bootstrap test with 10,000 bootstrap samples.

558 Estimation of position uncertainty

We estimated subjects' position uncertainty by binning the 2D space into 10×10 cm² bins. For each bin, we computed the variance in the subject's stopping position across trials in which targets fell in that bin. The resulting spatial map of variability was then convolved with a two-dimensional isotropic Gaussian kernel of width 40cm (equal to the diameter of the target) to yield a smooth estimate of variability as a function of space (**Fig 3B** – *left*). Because subjects aimed to stop on the target, variability in their stopping position can be interpreted as the uncertainty in subjects' posterior estimate about their own position.

565 Deriving an upper bound on the target-tracking index

Once the target disappears, subjects no longer get to directly observe it. To reach the target location, they 566 update their beliefs about the relative location of the target by integrating their self-motion, which in turn 567 must be estimated from the observed optic flow. Even if those beliefs are accurate on average, the 568 uncertainty in believed target location will grow over time on any given trial due to noise both in the 569 observations and in the integration process. Consequently, the degree to which subjects' eyes can track the 570 target (quantified by the tracking index, ρ) should decrease over time. Using the variability in subjects' 571 stopping positions to model their uncertainty in their believed location (see section above), we derived an 572 approximate upper-bound on the temporal dynamics of the tracking-index ρ_t at time t assuming inter-ocular 573 distance $\Delta \approx 0$: 574

$$\rho_t \le \sqrt{1 - \frac{\langle \left\| \widehat{\boldsymbol{\varphi}}_t - \overline{\widehat{\boldsymbol{\varphi}}}_t \right\|_2^2 \rangle}{\langle \left\| \boldsymbol{\varphi}_t - \overline{\boldsymbol{\varphi}}_t \right\|_2^2 \rangle}}$$
(3)

where $\overline{\hat{\varphi}}_t = \langle \widehat{\varphi}_t \rangle$ denotes the mean predicted eye position at time t. Note that this represents an upper-575 bound insofar as the variability in subject's stopping positions stems entirely from uncertainty in their 576 believed location. To derive this approximate bound, we first used the first-order Taylor series 577 approximation of equation (1) to express the variance of the predicted eye position $(\hat{\alpha}_t, \hat{\beta}_t)$ in terms of the 578 variance of the relative target position (x_t, y_t, z_t) as: $Var(\hat{\alpha}_t) = (\partial f / \partial x)^2 Var(x_t) + (\partial f / \partial y)^2 Var(y_t)$ 579 and $\operatorname{Var}(\hat{\beta}_t) = (\partial g/\partial x)^2 \operatorname{Var}(x_t) + (\partial g/\partial y)^2 \operatorname{Var}(y_t)$, where $f(x_t, y_t, z_t) = \tan^{-1}\left(\sqrt{y_t^2 + z_t^2}/x_t\right)$ and 580 $g(x_t, y_t, z_t) = \tan^{-1}\left(z_t/\sqrt{y_t^2 + x_t^2}\right)$ from equation (1), and we have used the fact that $\operatorname{Var}(z_t) = 0$ because 581 there is no motion component perpendicular to the ground plane. Substituting the derivatives, we get: 582

$$\operatorname{Var}(\hat{\alpha}_{t}) = \frac{(y_{t}^{2} + z_{t}^{2})}{(x_{t}^{2} + y_{t}^{2} + z_{t}^{2})^{2}} \operatorname{Var}(x_{t}) + \frac{x_{t}^{2} y_{t}^{2}}{(x_{t}^{2} + y_{t}^{2} + z_{t}^{2})^{2} (y_{t}^{2} + z_{t}^{2})} \operatorname{Var}(y_{t})$$
(4.1)

$$\operatorname{Var}(\hat{\beta}_t) = \frac{z_t^2}{(x_t^2 + y_t^2 + z_t^2)^2 (x_t^2 + y_t^2)} \left(x_t^2 \operatorname{Var}(x_t) + y_t^2 \operatorname{Var}(y_t) \right)$$
(4.2)

The above equations are based on first-order Taylor series approximation and hold as long as the higherorder terms are relatively small (**Fig S8**). Although we cannot not directly measure $Var(x_t)$ and $Var(y_t)$, we could estimate them from the data (see previous section) and use it to determine the variability in predicted eye positions given by **equation** (4). Variability in the predictions then implies a lower bound in the mean squared error achievable by any observation $\boldsymbol{\varphi}_t$: $\|\boldsymbol{\varphi}_t - \boldsymbol{\widehat{\varphi}}_t\|_2^2 \ge \|\boldsymbol{\widehat{\varphi}}_t - \boldsymbol{\widehat{\varphi}}_t\|_2^2$. Substituting this in (2), we obtain an upper bound on the tracking-index given by **equation** (3). Note that, in deriving this approximate upper-bound, we ignored the noise in generating an eye movement to an intended location (process noise). So in principle, it is possible to derive a tighter bound by incorporating it. Note that as subjects approach the target, x_t and y_t approach zero, whereas the uncertainty grows so both $\operatorname{Var}(x_t)$ and $\operatorname{Var}(y_t)$ increase. Together, this leads to an increase in the variance of the predicted eye positions (**equation 4**) and consequently, a gradual decrease in the fraction of explainable variance over time (**equation 3**).

594 Comparing behavioural and target-tracking errors

To test whether poor target-tracking was associated with poor behavioural accuracy, we estimated the 595 correlation between behavioural and target-tracking errors across trials of individual recording sessions. 596 Behavioural error was given by the Euclidean distance between the target location and the subject's 597 response (stopping location) on individual trials, while the target-tracking error was given by the Euclidean 598 distance between actual and predicted eve position, averaged over the entire time period of the trial, except 599 for the last 300ms (as the predictions typically broke down when the subject was too close to the target). 600 Because trial difficulty could affect both errors thereby inducing spurious correlations, we estimated the null 601 distribution of correlations using a shuffling procedure where we grouped the trials from each recording 602 session into ten quantiles based on target distance and shuffling only trials within the same group. The 603 results were quite robust to the number of quantiles. 604

605 Assessing performance in the fixation task

To assess the behavioural effect of inhibiting eye movements, we compared human subjects' performance 606 across 'eyes-moving' and 'eyes-fixed' trials. Because we did not control for fixation breaks that happened in 607 the 'eves-fixed' condition during the experiment, we identified and removed such trials offline. Specifically, 608 we removed the trials in which the temporal standard deviation (σ) of subject's eye position during the trial 609 (*i.e.* from the time when the target disappeared until the end of steering) exceeded 3° (roughly half-width of 610 the fixation cross), from our analysis (~10% of the fixation trials across all subjects). The standard deviation 611 was quantified as $\sigma = \sqrt{\sigma^2(\alpha) + \sigma^2(\beta)}$ where $\sigma(\alpha)$ and $\sigma(\beta)$ denote the temporal standard deviation of 612 lateral version and elevation respectively. To evaluate the role of eve movements, we compared subjects' 613 performance in the fixation trials ('eyes-fixed') with trials that did not require fixation ('eyes-moving'). For 614 both sets of trials, we computed ROC curves for distinguishing 'rewarded' and 'unrewarded' trials (see 615 section 'psychometric analysis' above) and used a paired *t*-test to test whether the mean area under the 616 curves were different. We also computed the correlation between target and response locations and then 617 used a paired *t*-test to test whether there was a significant difference between the correlation coefficients in 618 the two sets of trials across subjects (Fig 5D). 619

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